

# PDFS of Tropospheric Humidity: Measurements and theory

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# *Outline*

- Introduction
- Examine Observed of Tropical and Subtropical Humidity (AIRS + MLS measurements).
- Theory for PDFs of Relative Humidity (RH)
- Analysis of climate model (very preliminary).

# OBSERVATIONS

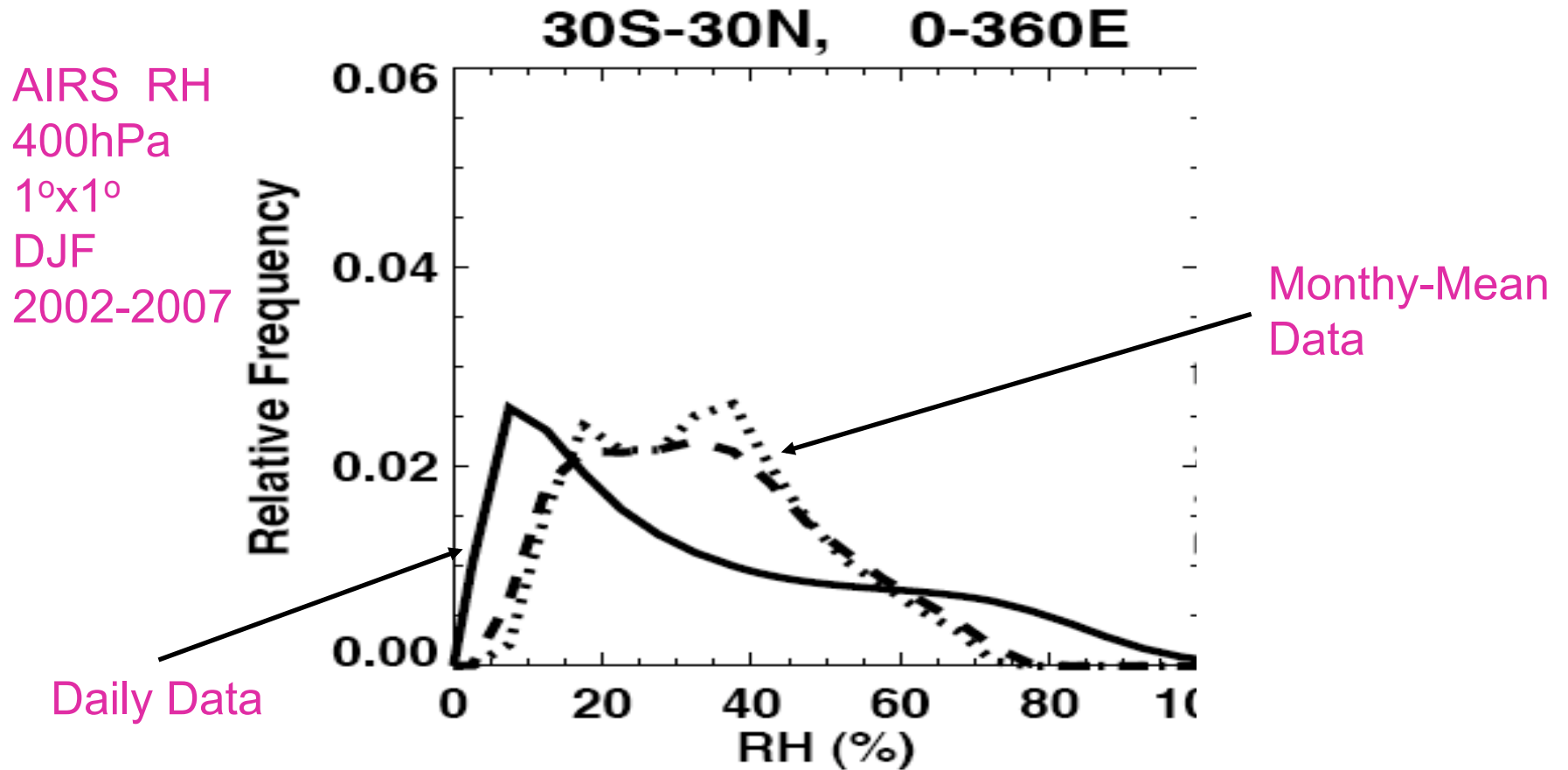
Examine Probability Distribution Functions (PDFs) of Relative Humidity (RH) measurements from satellite instruments:

- AIRS (2002-2007)
- Aura MLS (2004-2007)
- UARS MLS (1992-2004)

Focus on PDFs for  
10° latitude x 20° longitude regions  
NH winter (Dec-Mar).

# Probability Distribution Functions

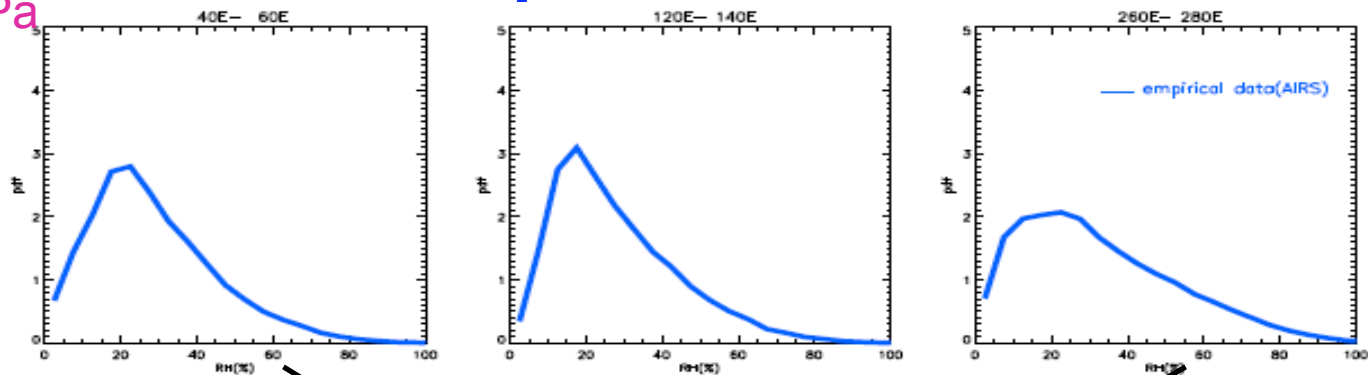
PDFs depend on the space and time scales considered. E.g.,



We focus on daily data ... extremes important for radiative considerations.

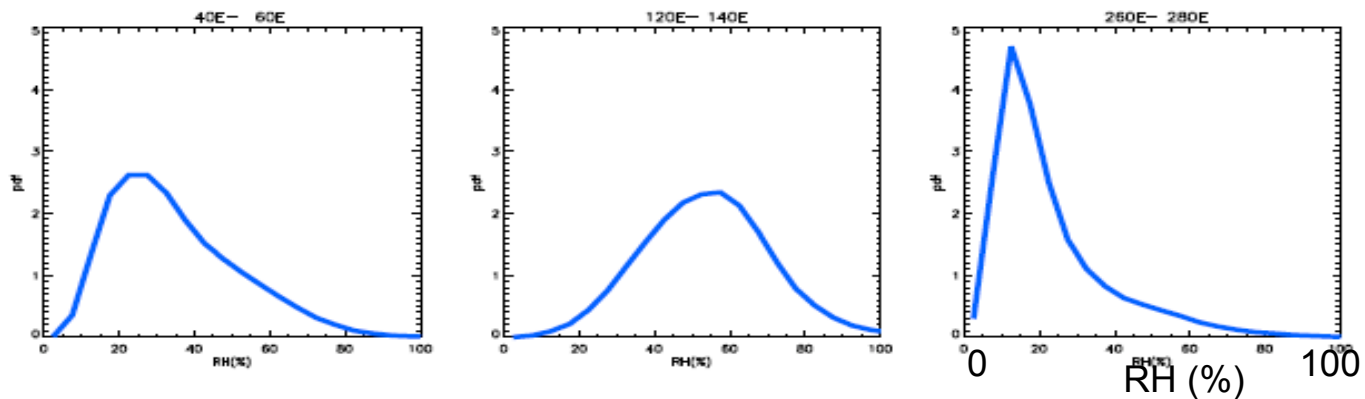
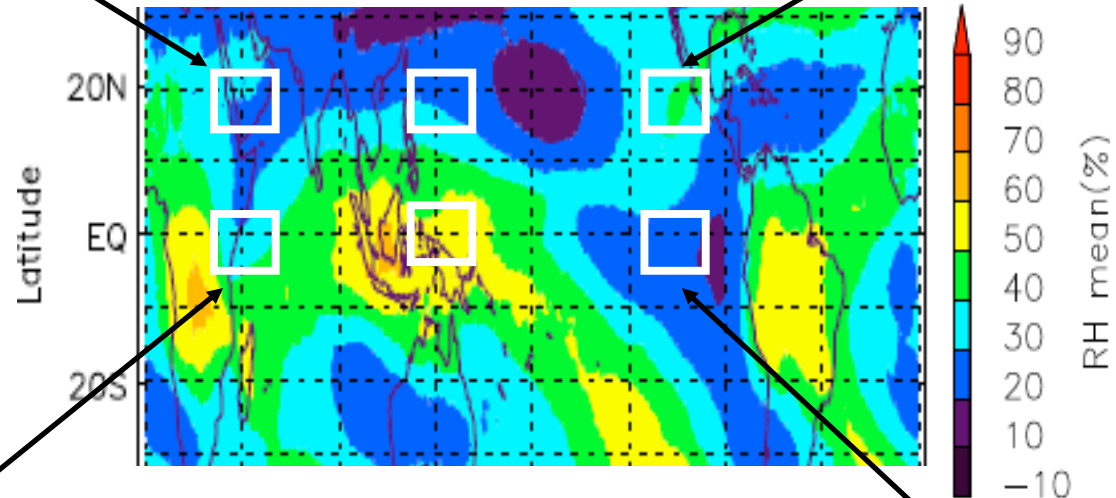
AIRS RH  
200-250hPa

## PDFs: Spatial Variations



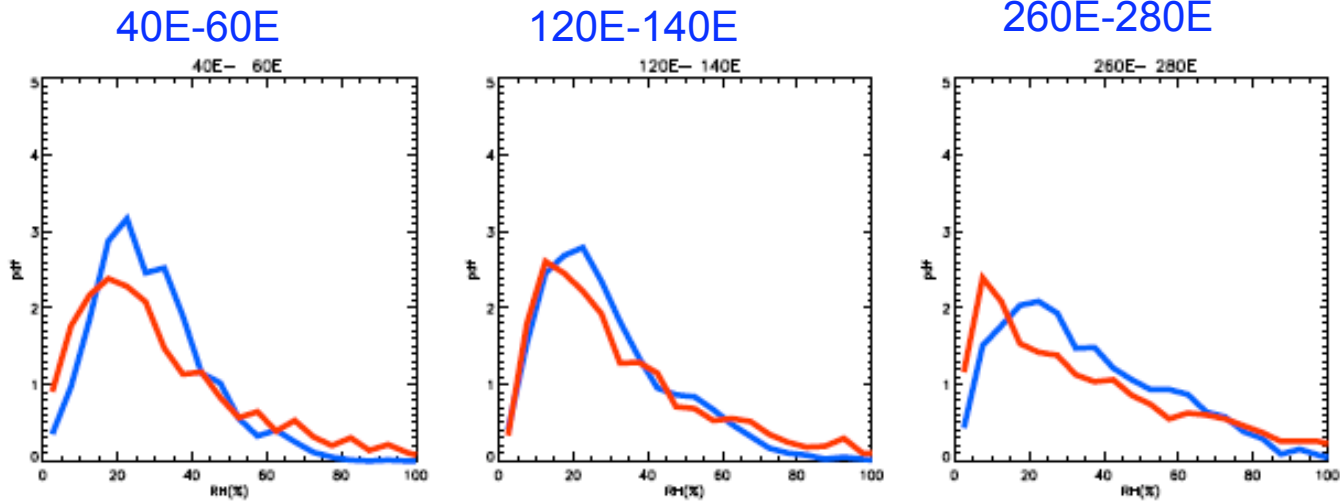
PDFs are

- non-Gaussian,
- very broad, and
- **shape varies with location.**



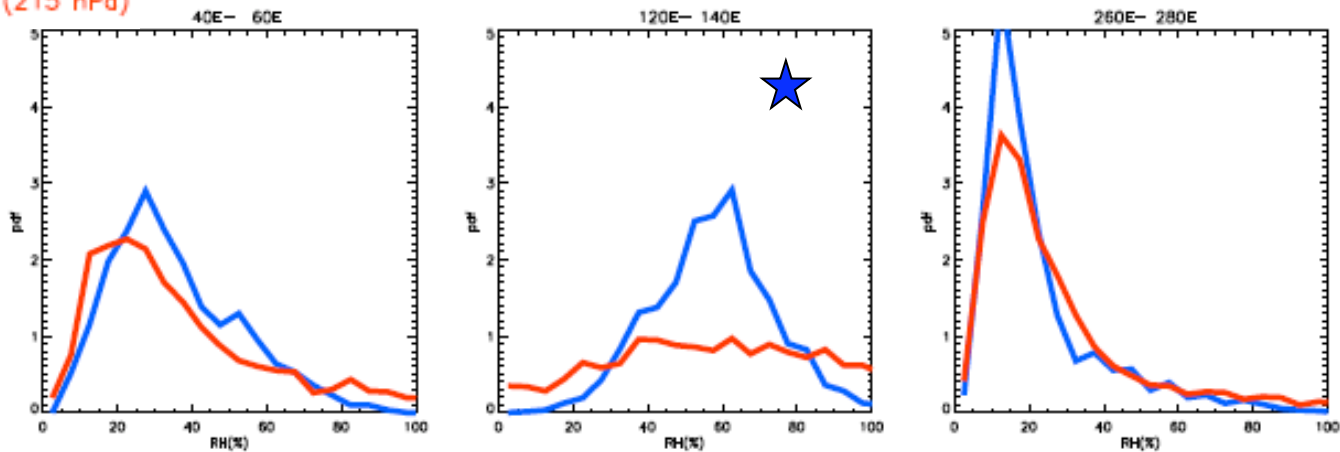
# PDFS: AIRS - Aura MLS Comparison

Subtropics  
(15-25N)



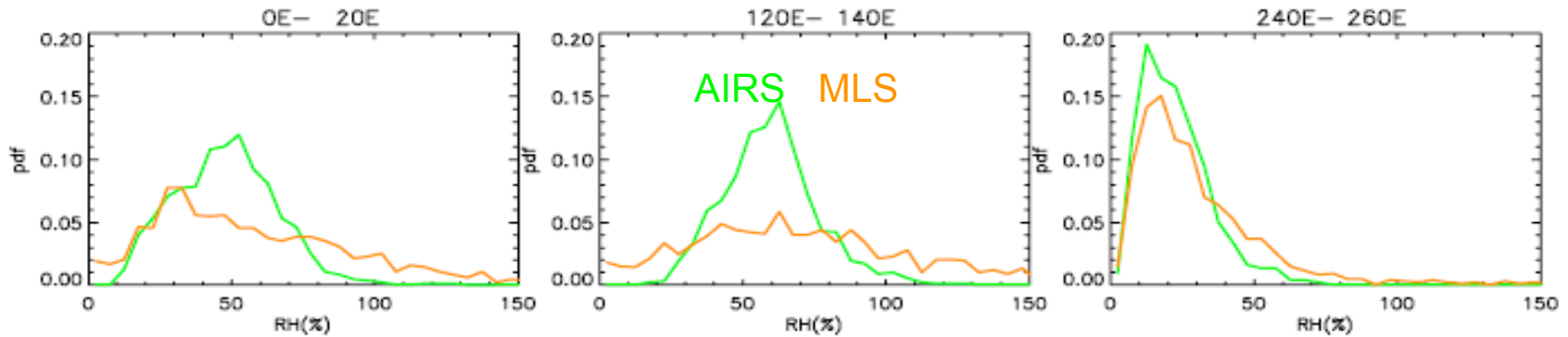
— AIRS RH (250 hPa)  
— Aura MLS RH (215 hPa)

Tropics  
(5S-5N)



Good agreement between AIRS and Aura MLS,  
with some exceptions.

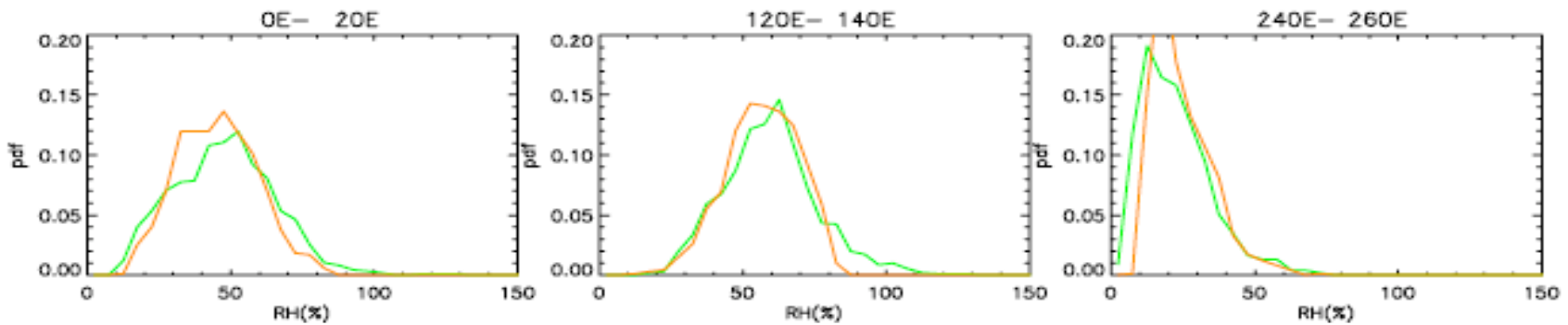
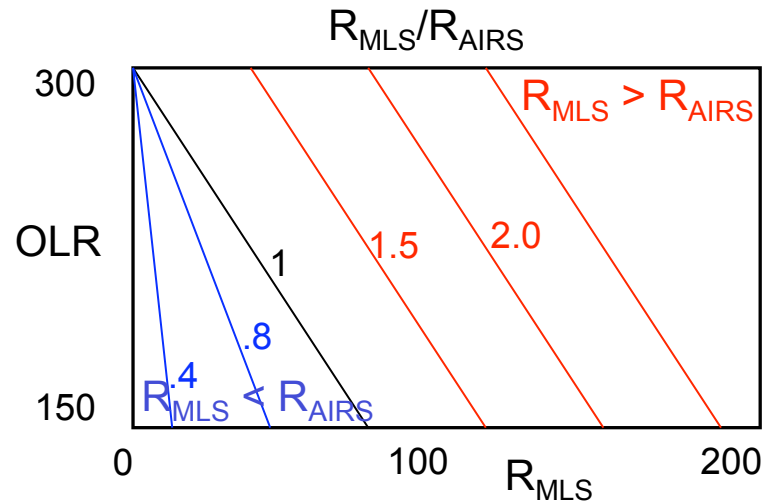
# Aura MLS - AIRS bias



Transform  
MLS Data



$$R_{\text{MLS}}/R_{\text{AIRS}} = f(R_{\text{MLS}}, \text{OLR})$$



# Theoretical Model

Generalization of Sherwood et al (J. Clim, 2006) model for PDFs of Relative Humidity (R). Based on "time since last saturation" paradigm: Parcel's humidity = lowest saturation value experienced.

Two main assumptions:

1. Uniform subsidence between remoistening events.

$$R(t) \approx \exp\left(-\frac{t}{\tau_{Dry}}\right)$$

$\tau_{Dry}$  is drying time by subsidence,  
t is time since last saturation.

2. Random remoistening events models as Poisson process:  
PDF of time since last saturation is

$$P(t) = \frac{\left(\frac{1}{\tau_{Moist}}\right)^k \exp\left(-\frac{t}{\tau_{Moist}}\right) t^{k-1}}{\Gamma(k)}$$

$\tau_{Moist}$  is mean time between remoistening events.

k is a measure of variability of moistening events (larger k => less random).

k=1 is Sherwood et al (2006) model.



# *Generalized Model for PDFs*

Combining 1 and 2 yields PDF for Relative Humidity:

$$P(R) = \left( \frac{r^k R^{r-1}}{\Gamma(k)} \right) (-\log R)^{k-1}$$

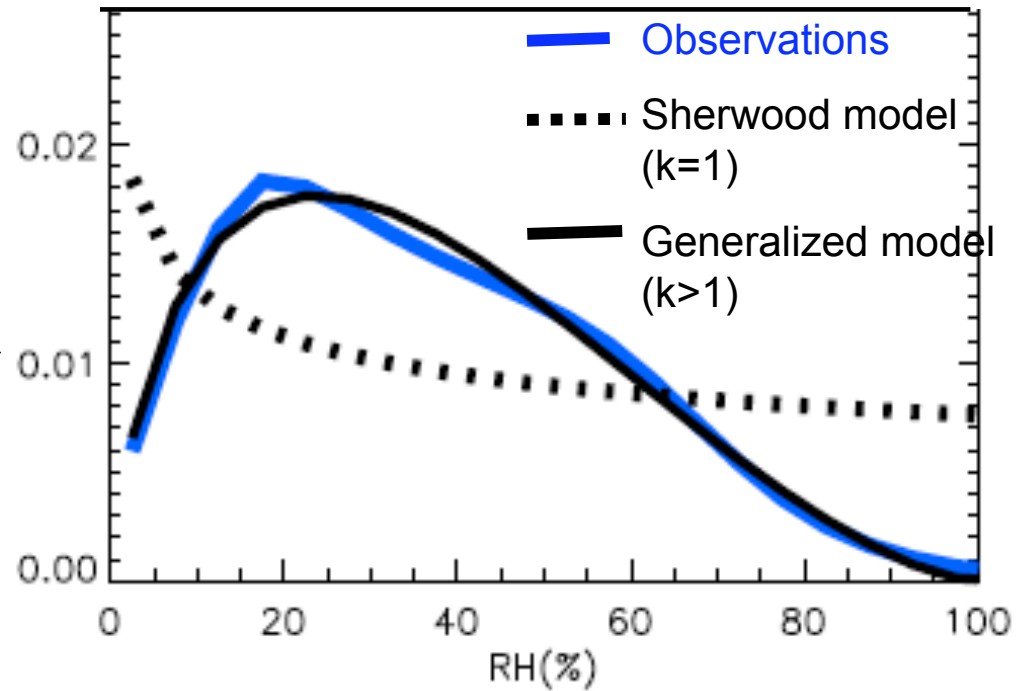
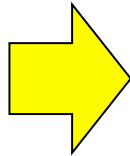
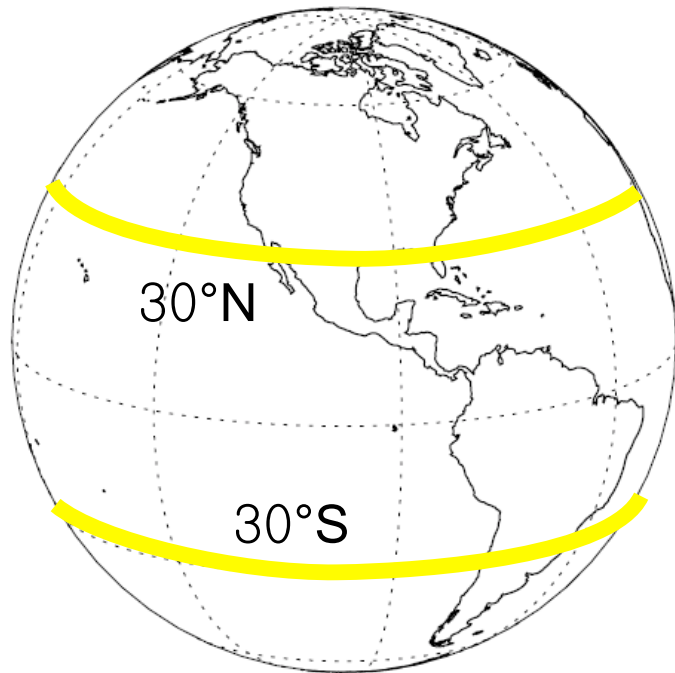
$$r = \tau_{\text{dry}} / \tau_{\text{moist}}$$

k=1 is original Sherwood et al. model.

- Larger r implies more rapid remoistening
- Larger k implies less random remoistening processes.

## Comparison with Data

The Generalized model can reproduce AIRS 250hPa PDF for whole tropics (30S-30N).



What about subregions?

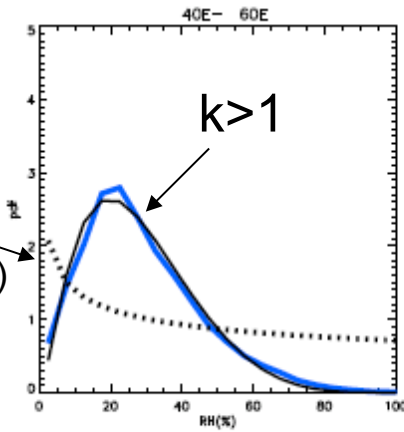
# Comparison with Data II

Generalized Model can also fit the observed PDFs for all  $10^\circ \times 20^\circ$  regions, with  $r$  and  $k$  varying with location.

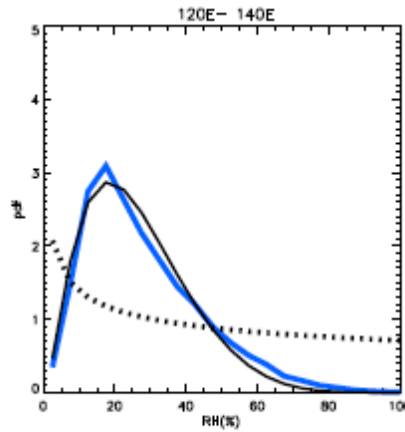
Subtropics  
(15-25N)

$k=1$   
(Sherwood)

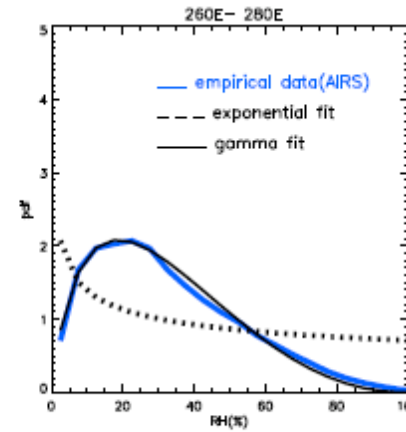
40E-60E



120E-140E



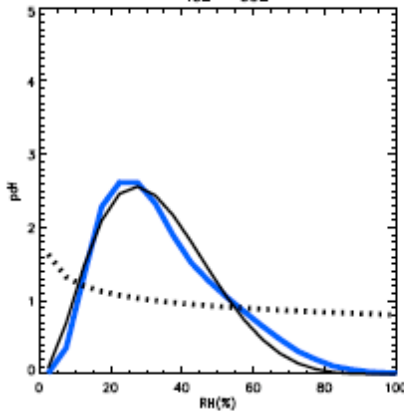
260E-280E



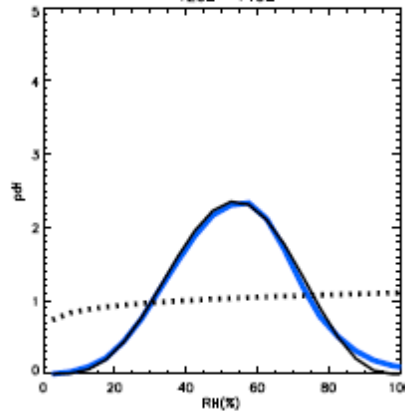
(b) Tropics (5S-5N)

Tropics  
(5S-5N)

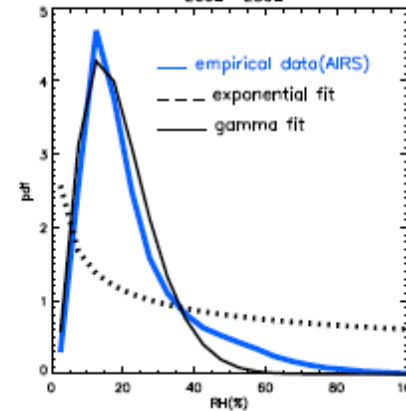
40E-60E



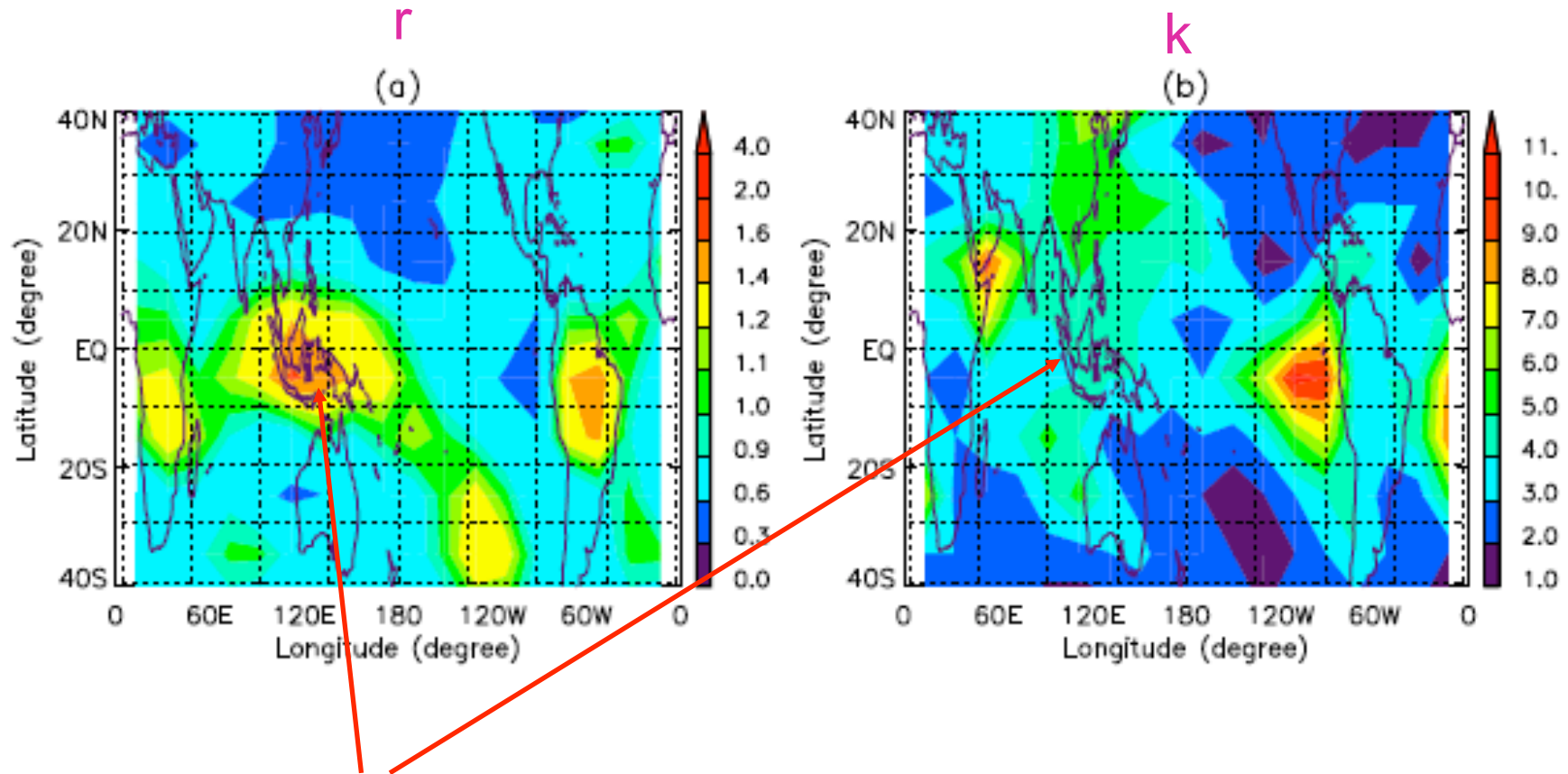
120E-140E



260E-280E



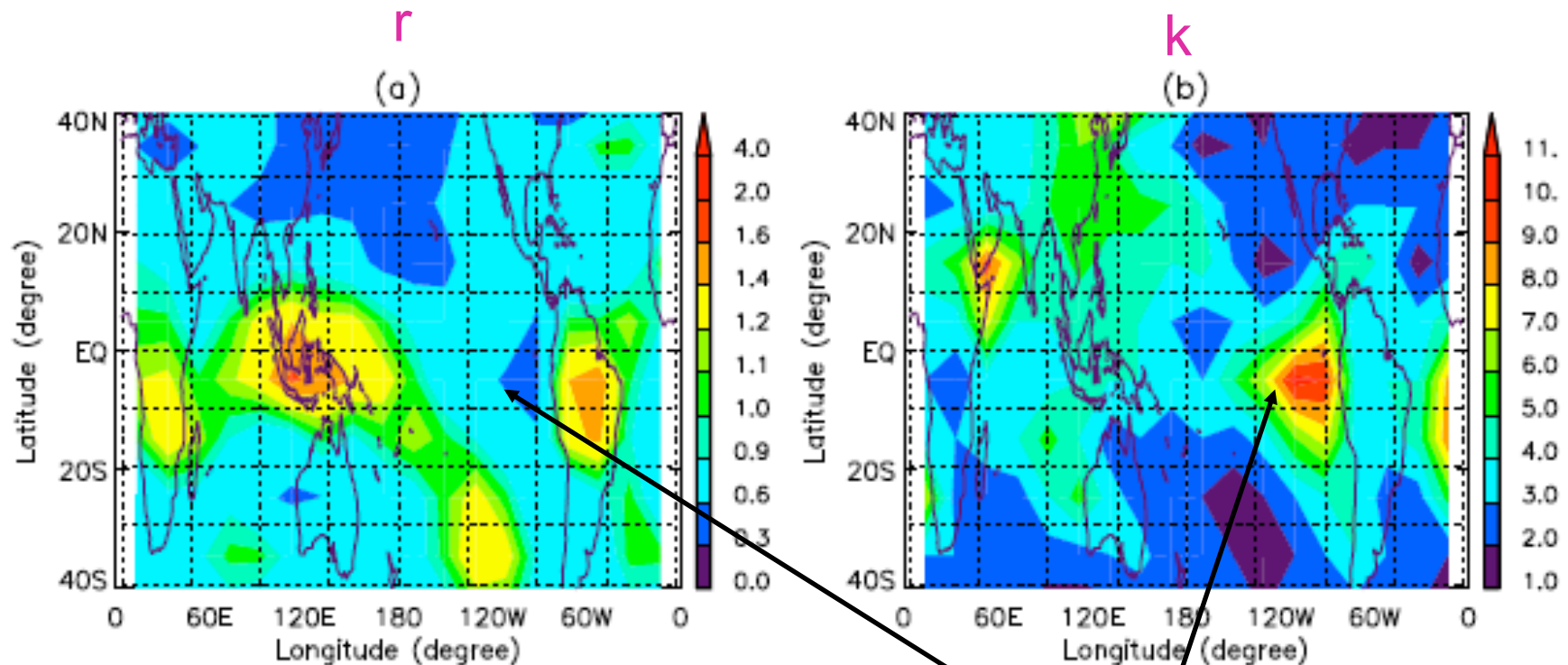
# Spatial Variations of $r$ and $k$



## Convective Regions:

- $r > 1$  and low  $k$
- Rapid, random remoistening
- Consistent with remoistening by rapid vertical mixing.

# Maps of $r$ and $k$



## Convective Regions:

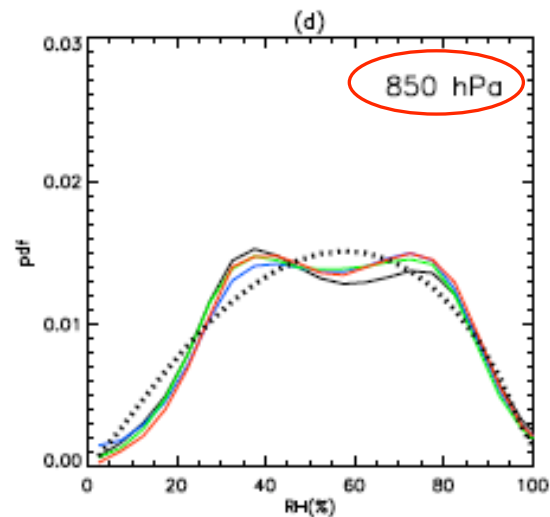
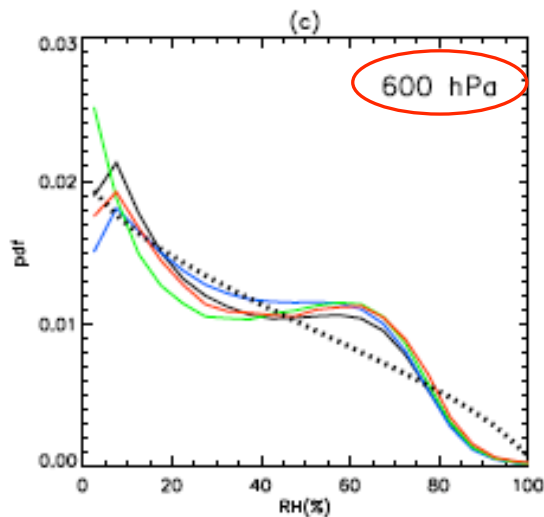
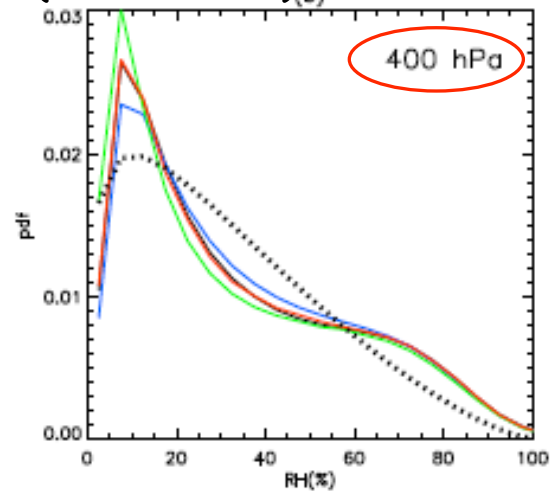
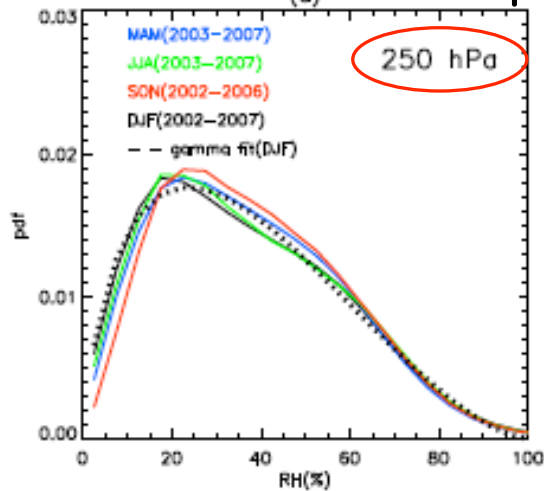
- $r > 1$  and low  $k$
- Rapid, random remoistening
- Consistent with remoistening by rapid vertical mixing.

## Non-convective Regions:

- $r < 1$  and high  $k$
- Slower, more regular remoistening
- Consistent with remoistening by quasi-horizontal transport

# PDFs: Different Seasons and Altitudes

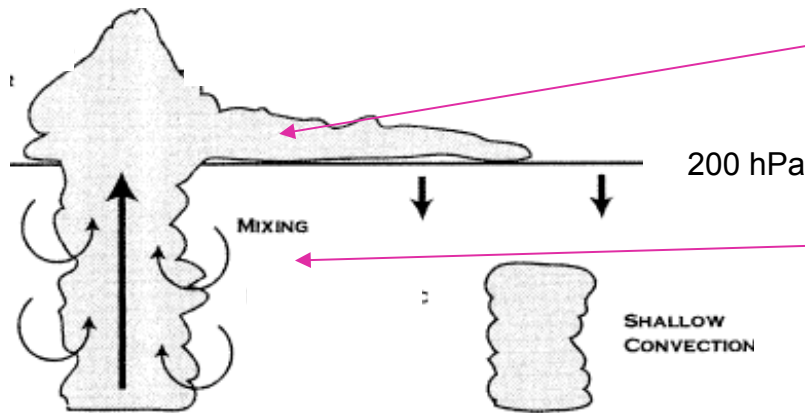
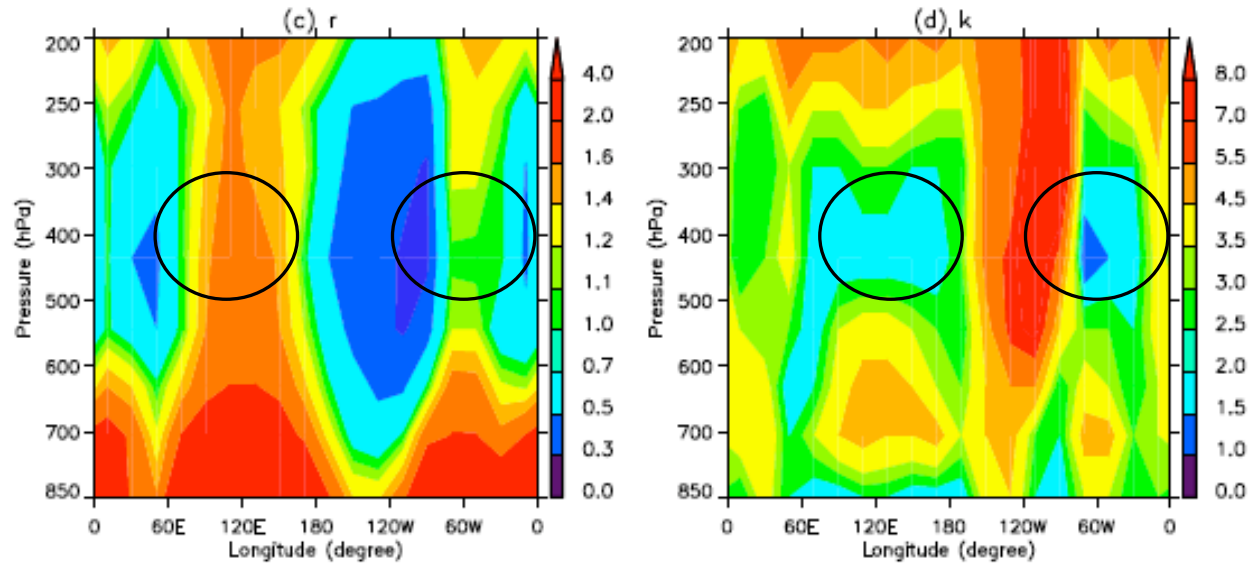
whole tropics (30S-30N)



- Only weak seasonal variations, but large vertical variations.
- PDFs for whole tropics are bimodal below 400hPa (but not in general for 10°x20° regions).
- Generalized model is unimodal, but still reasonable fit to observed PDFs.

# Vertical Variation of $r$ and $k$ in convective regions.

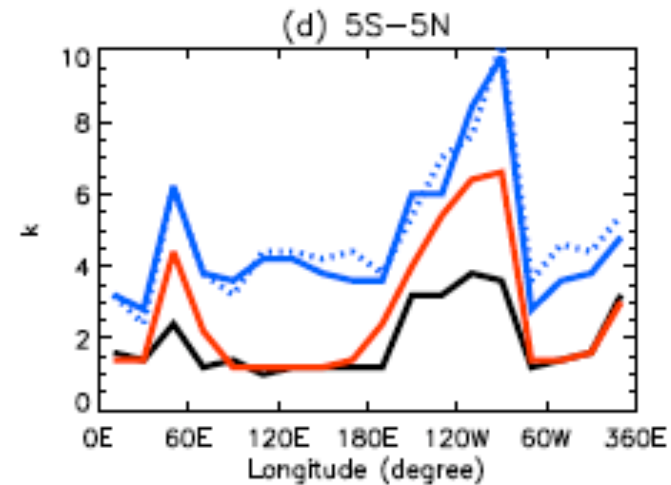
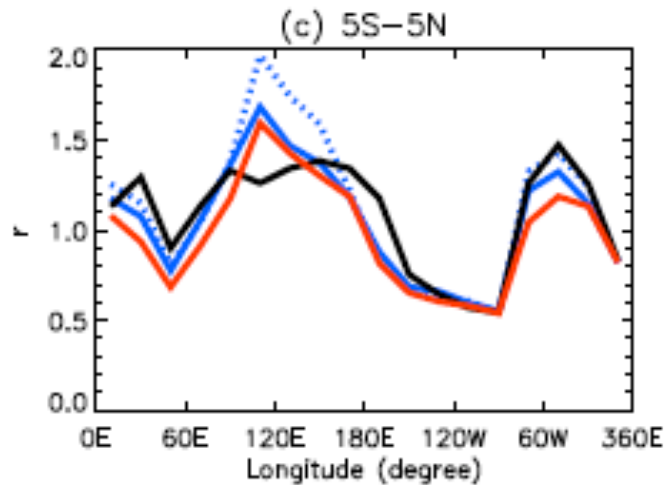
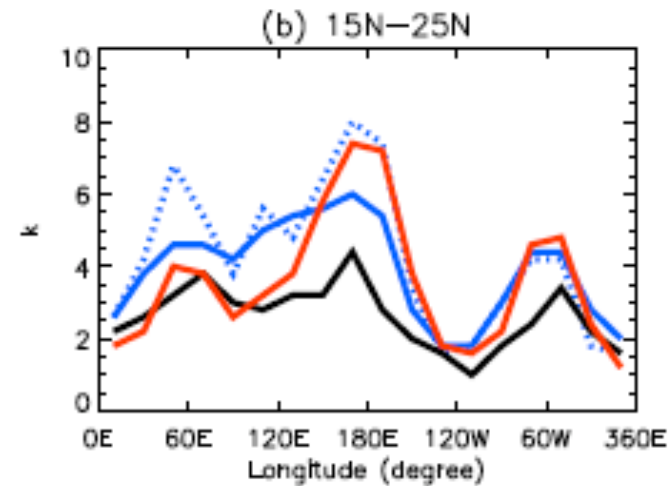
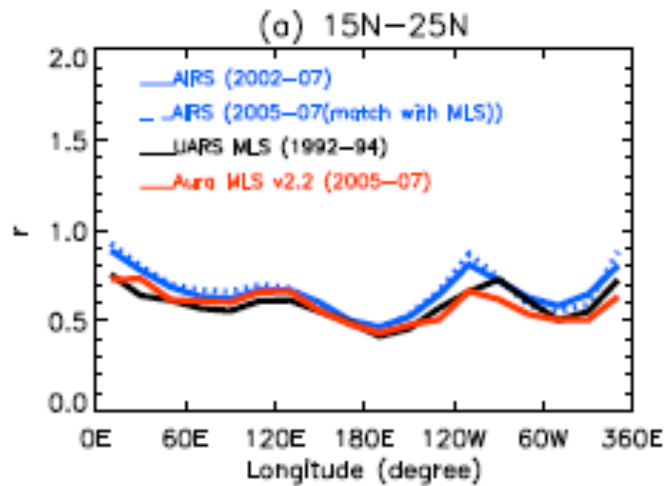
(B) Tropics (5S–5N)



Strong detrainment ( $>200\text{hPa}$ )  
→ large  $r$ , large  $k$ .

Weak detrainment, subsidence  
and mixing ( $\sim 400\text{hPa}$ )  
→ small  $r$ , small  $k$ .

# *r and k: AIRS - MLS*





## *Conclusions*

- PDFs of tropical and subtropical RH are non-Gaussian and very broad, with large spatial variations in characteristics of the PDFs.
  - PDFs can be well fit by a generalized version of the Sherwood et al. (2006) theoretical model, with 2 parameters "r" (ratio of drying and moistening times) and "k" (variability of moistening process).
  - Spatial variations in r and k can be related to variations in the physical processes controlling the RH distributions.
- ⇒ r and k provide a concise way to characterize the spatial variations in the PDFs and characteristics of processes controlling tropospheric RH.

## *Work in Progress*

Compare PDFs from climate models with observations:  
How well do they reproduce observations?  
How do PDFs change with increased well-mixed GHGs?

Examine RH from the GEOS Chemistry-Climate Model (Pawson et al. 2008). Atmospheric only model (prescribed SSTs), with chemistry coupled to radiation/dynamics.

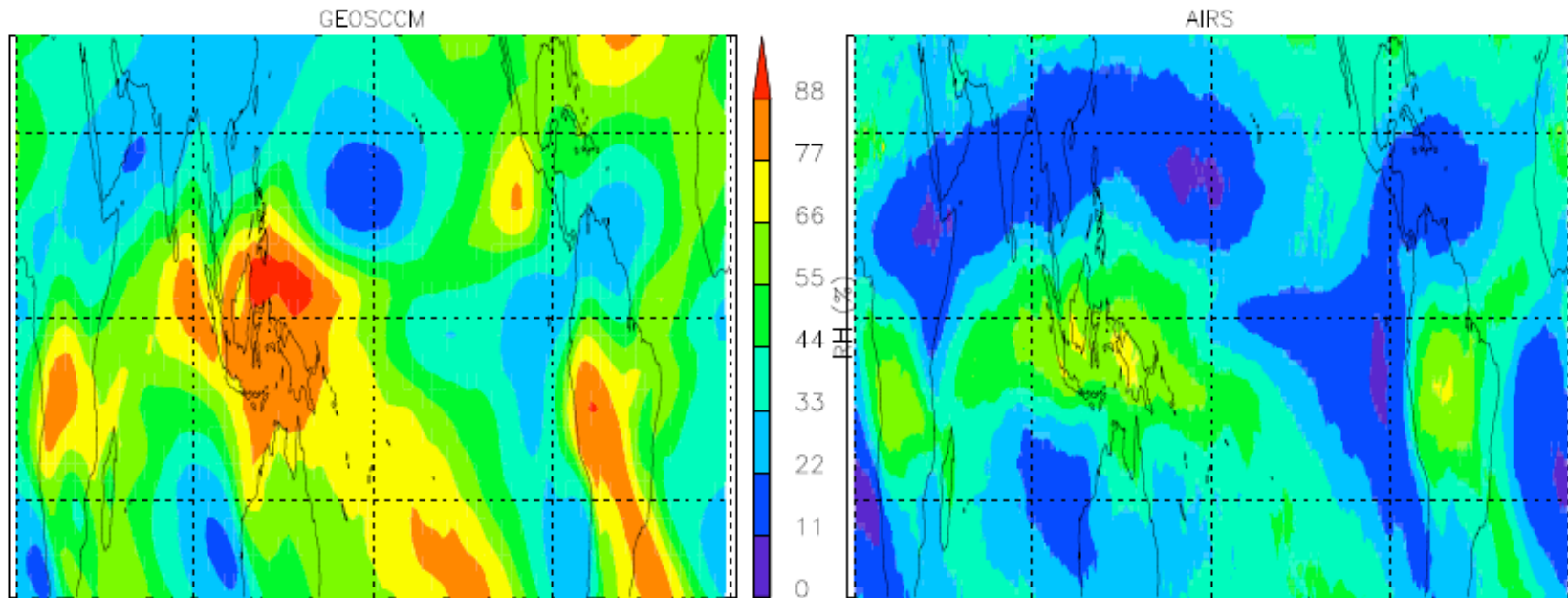
Daily RH @ 300 hPa for January and February, 1960 to 2040.

# GEOS CCM - AIRS

Jan-Feb Mean RH @ 300 hPa for present conditions

GEOSCCM 2000-2004

AIRS 2004-2007



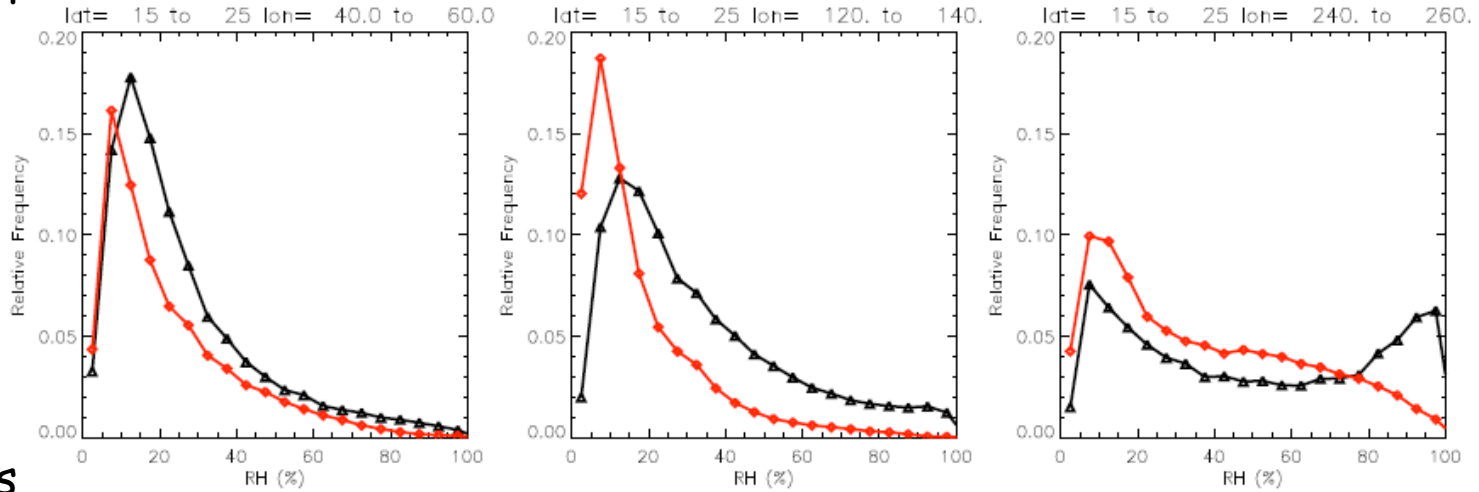
Model moister than AIRS, as found in other models.

# GEOS CCM PDFs

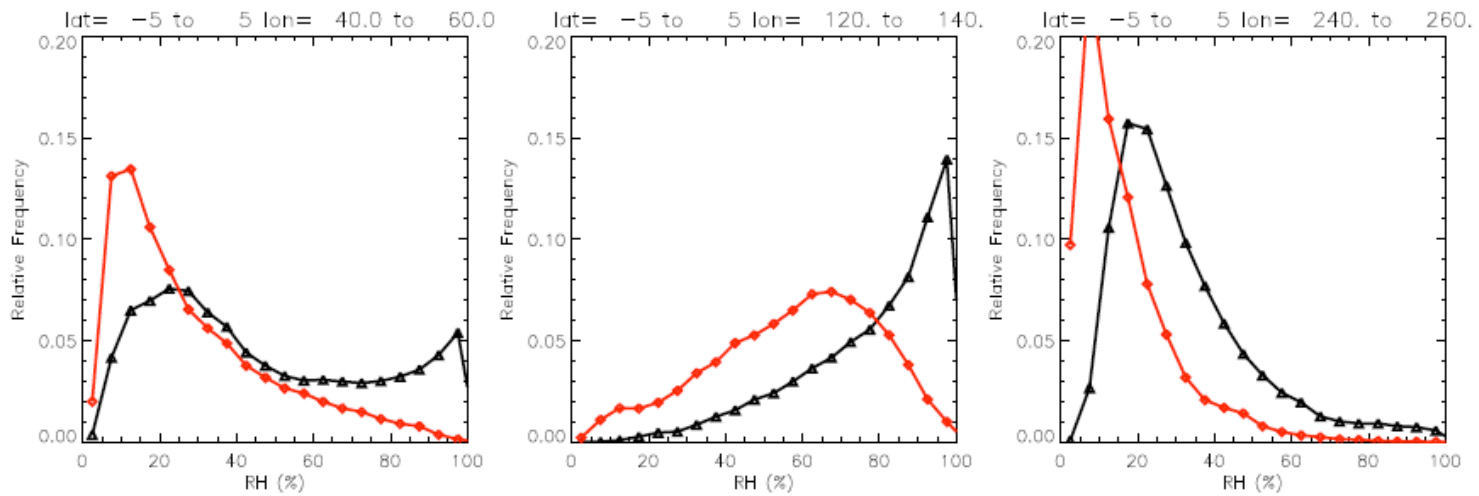
r and k larger in  
GEOSCCM

GEOSCCM      AIRS

subtropics



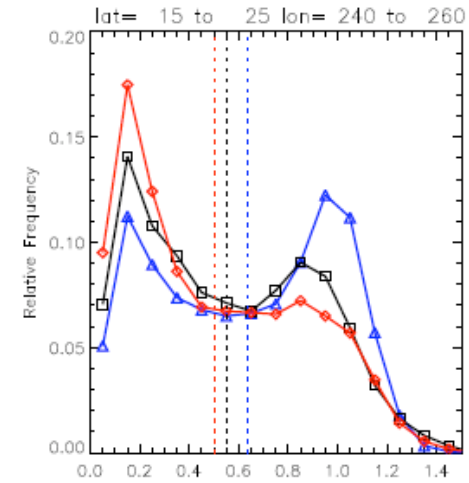
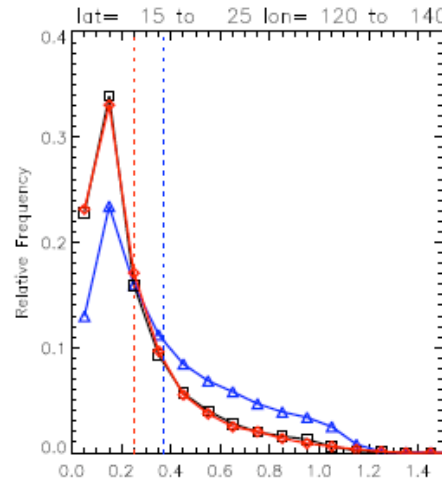
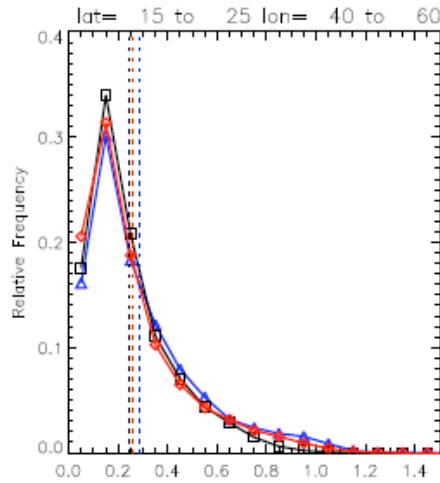
tropics



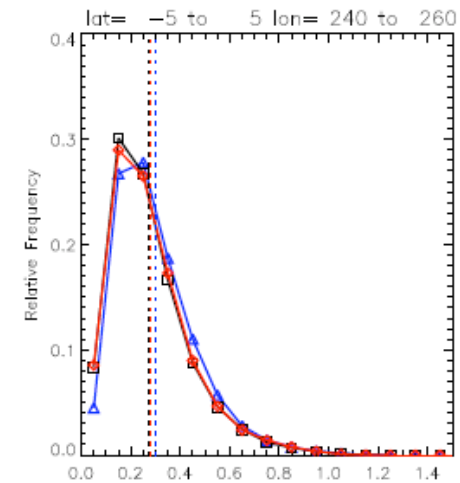
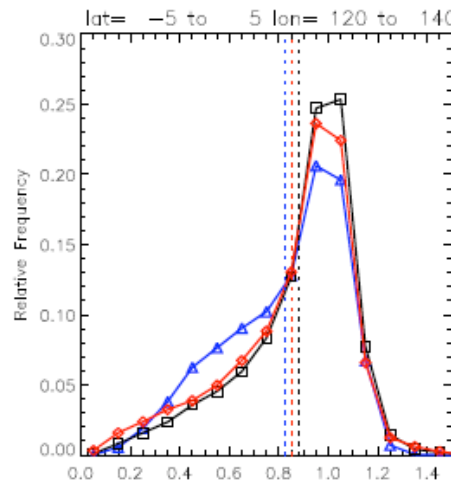
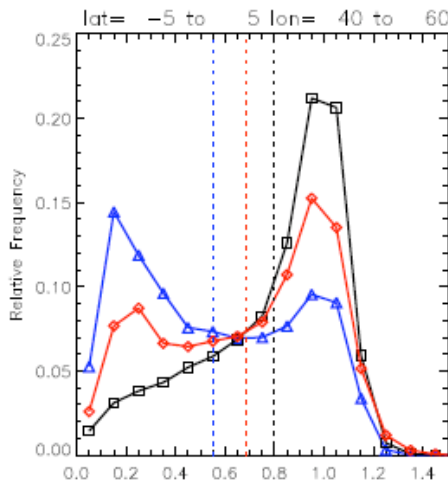
# GEOSCCM PDFs: 1960 to 2050

1960s - 2000s - 2040s

subtropics



tropics



PDFs of RH ~ constant

*THE END*