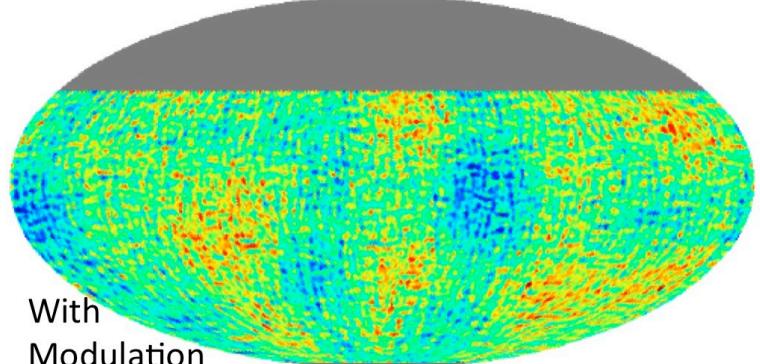
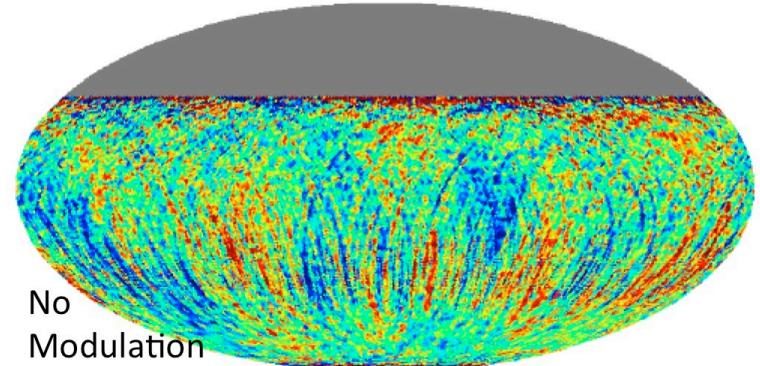
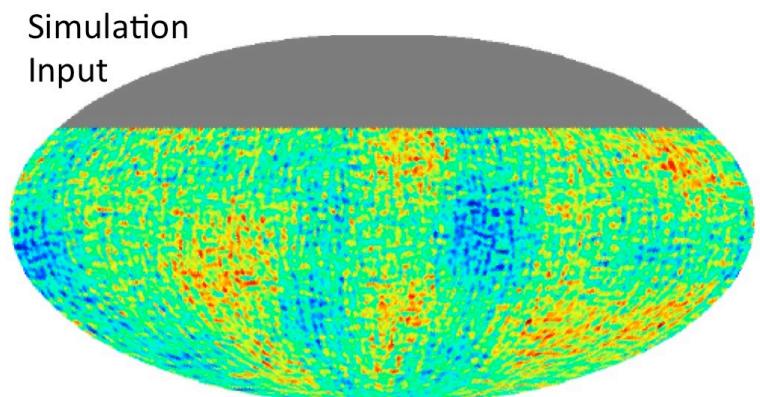
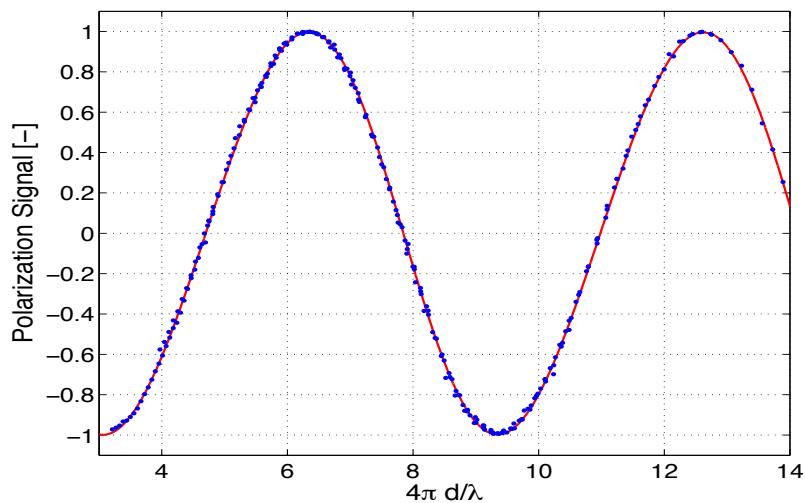
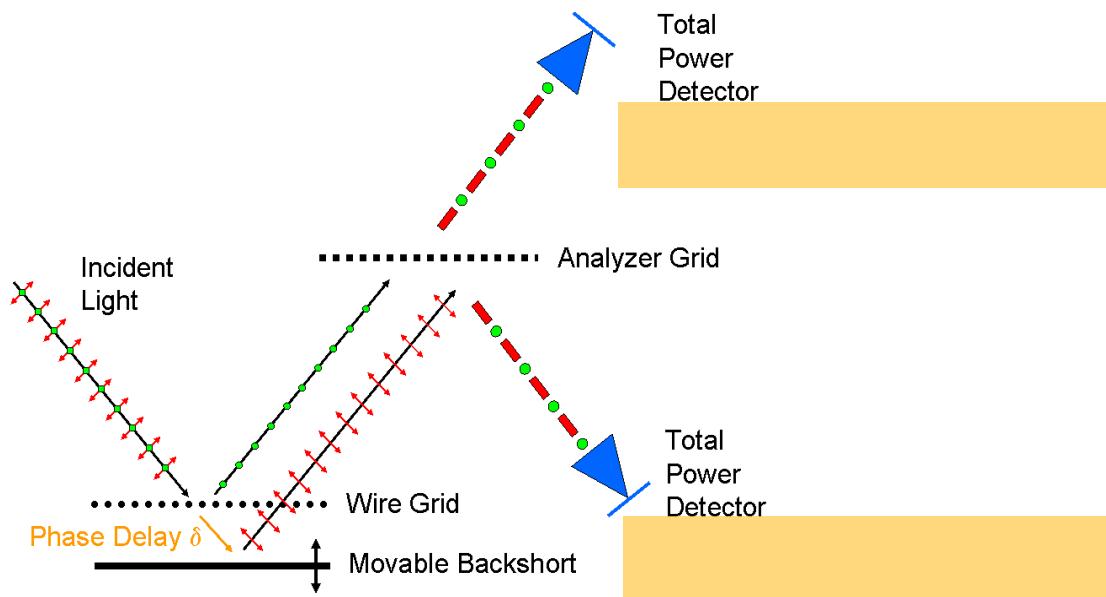
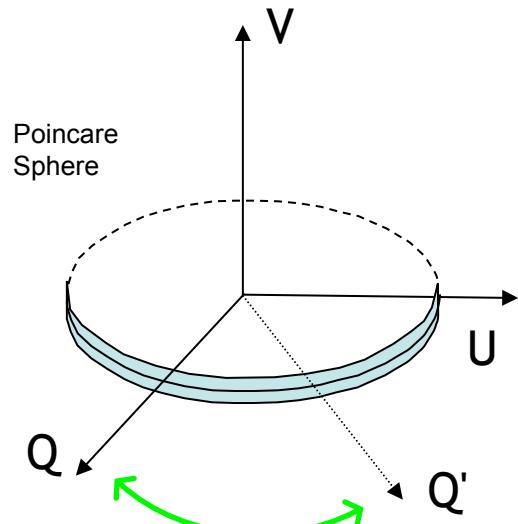


Variable-Delay Polarization Modulator (VPM)

Measure linear and circular polarization



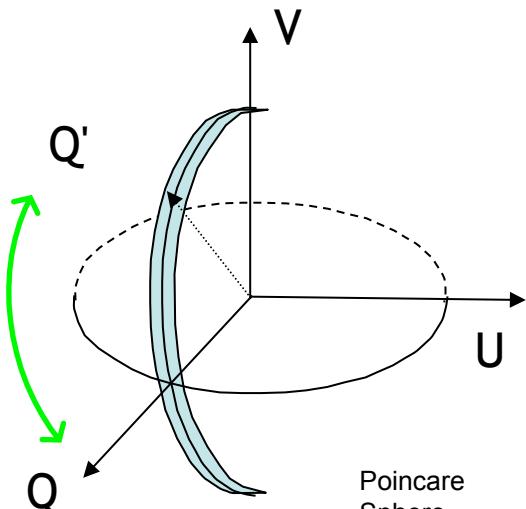
VPM Mitigates Cross-Polar Beam Mixing



HWP rotates $Q \leftrightarrow U$

$$\begin{bmatrix} I' \\ Q' \\ U' \\ V' \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos 2\alpha & \sin 2\alpha & 0 \\ 0 & -\sin 2\alpha & \cos 2\alpha & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} I \\ Q \\ U \\ V \end{bmatrix}$$

Modulation in same direction as mixing: Systematics!



VPM rotates $Q \leftrightarrow V$

$$\begin{bmatrix} I' \\ Q' \\ U' \\ V' \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos \delta & 0 & \sin \delta \\ 0 & 0 & 1 & 0 \\ 0 & -\sin \delta & 0 & \cos \delta \end{bmatrix} \begin{bmatrix} I \\ Q \\ U \\ V \end{bmatrix}$$

Modulation orthogonal to mixing: Efficiency!

Problem: Sky is bright in Q and U

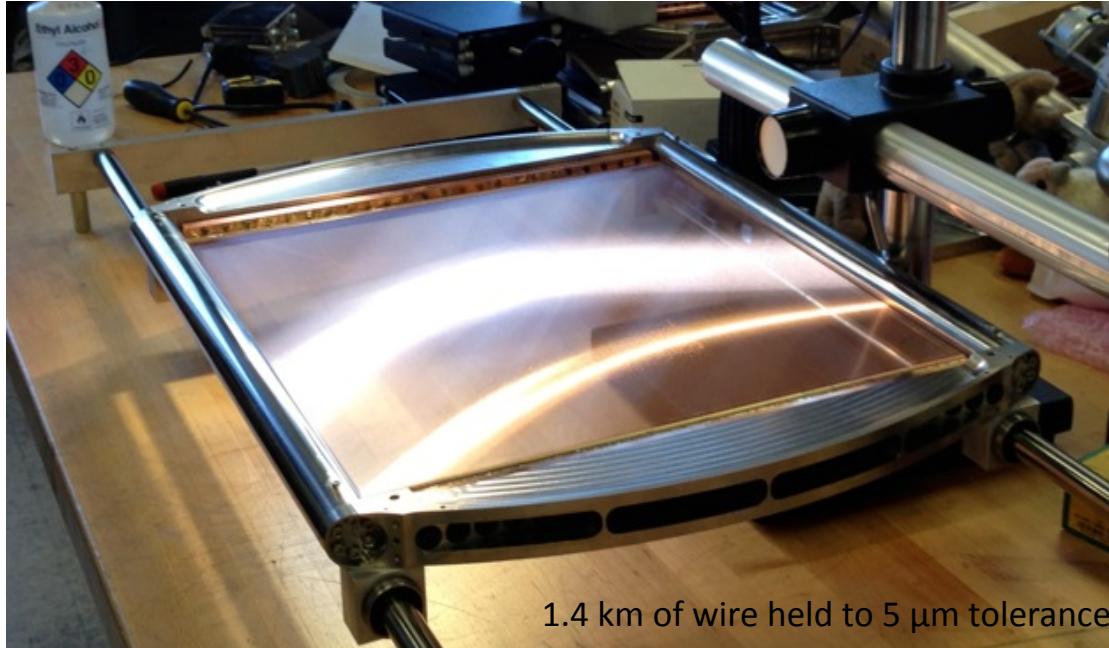
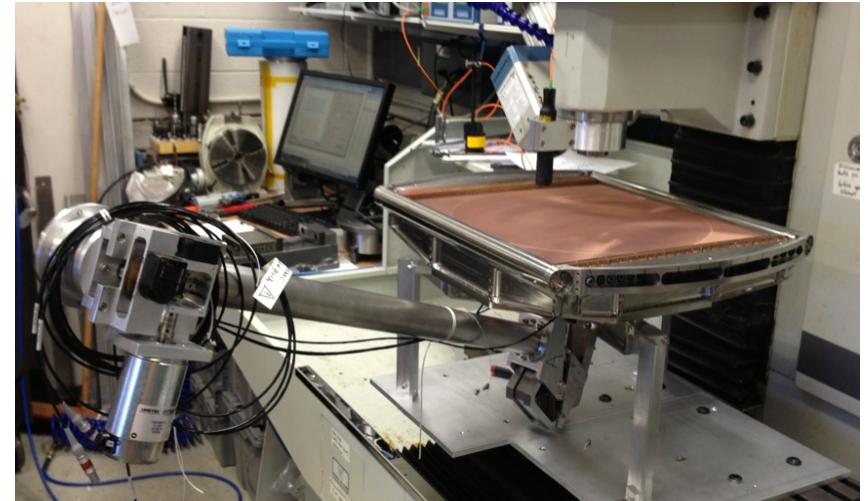
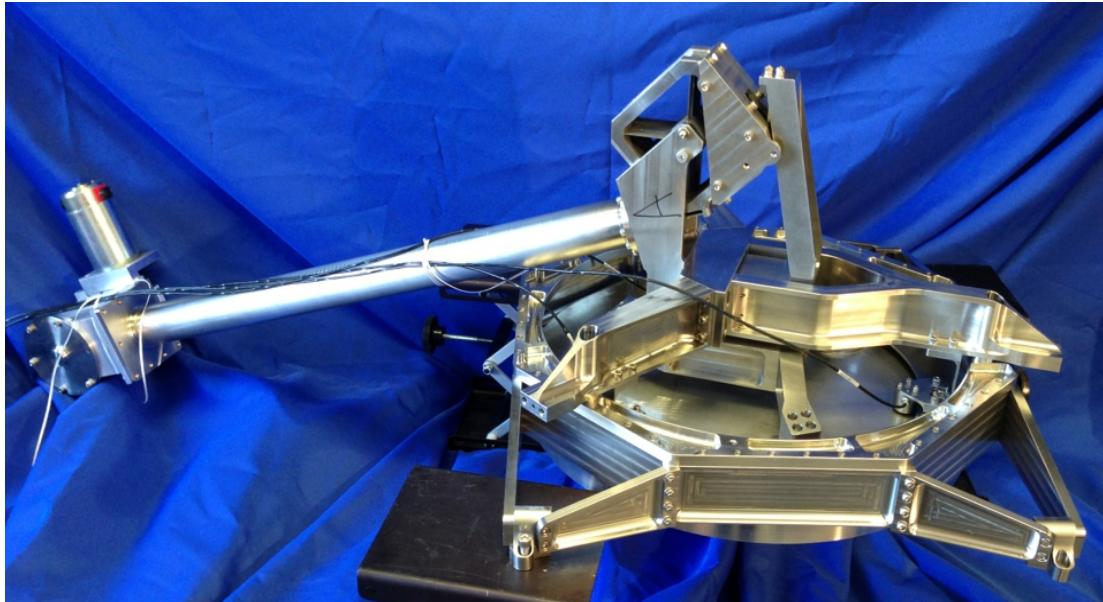
Any other QU mixing (e.g. cross-pol) can then project bright [QU] foregrounds into false B-mode signal

Solution: Modulate $Q \leftrightarrow V$ instead!

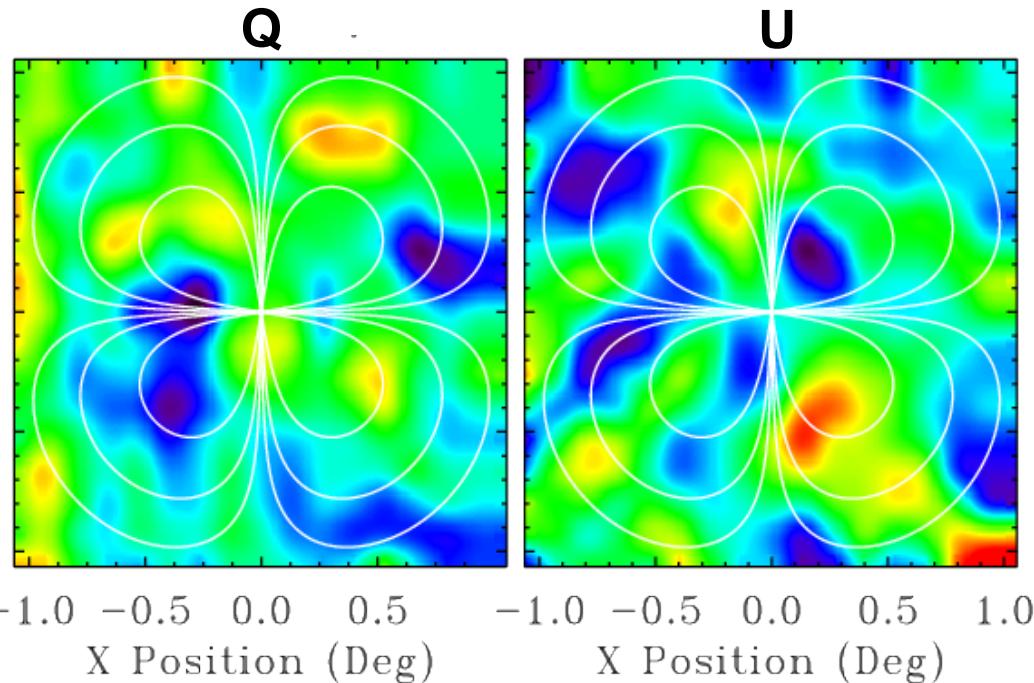
No celestial signal in V, so $Q \leftrightarrow V$ mixing simply reduces amplitude of detected Q modulation.

Efficiency, not systematic error!

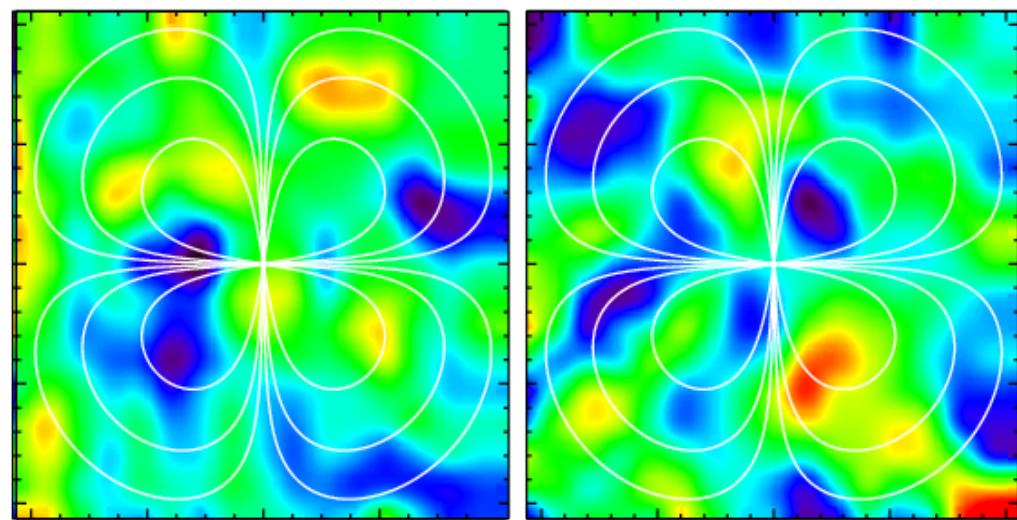
Polarization Modulator



Cross-Polar Beam Systematics

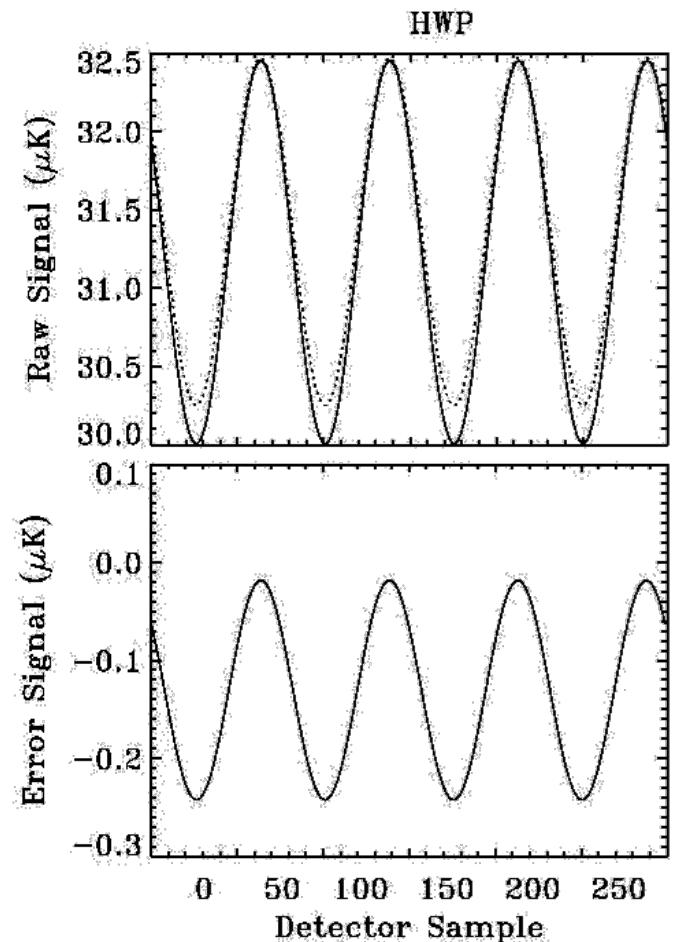


True
Sky

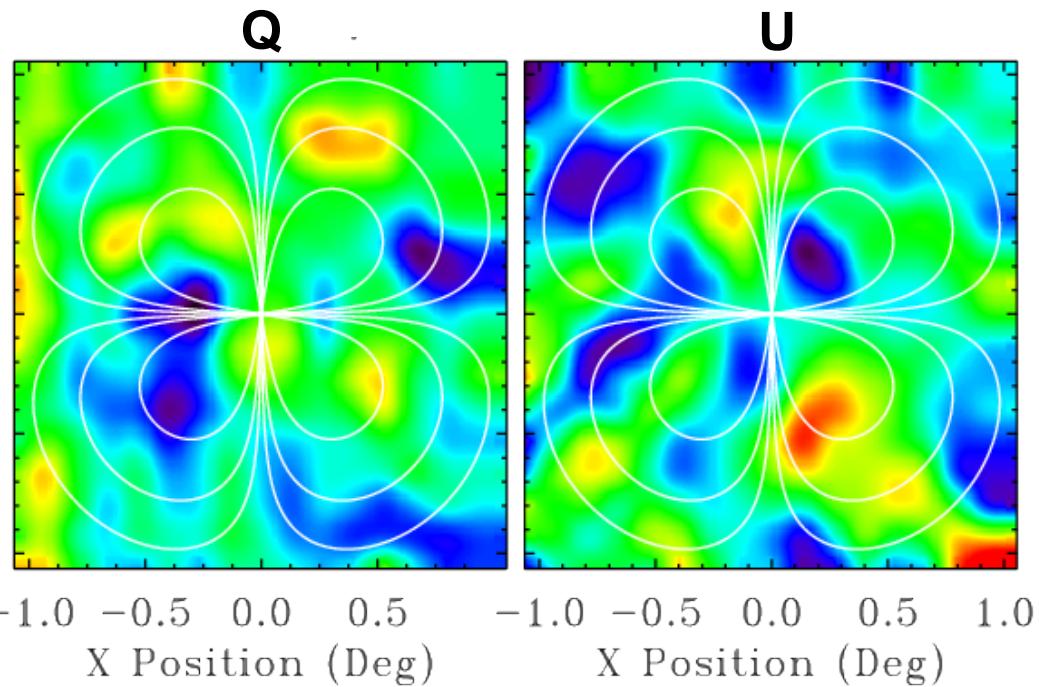


After
HWP
Modulation

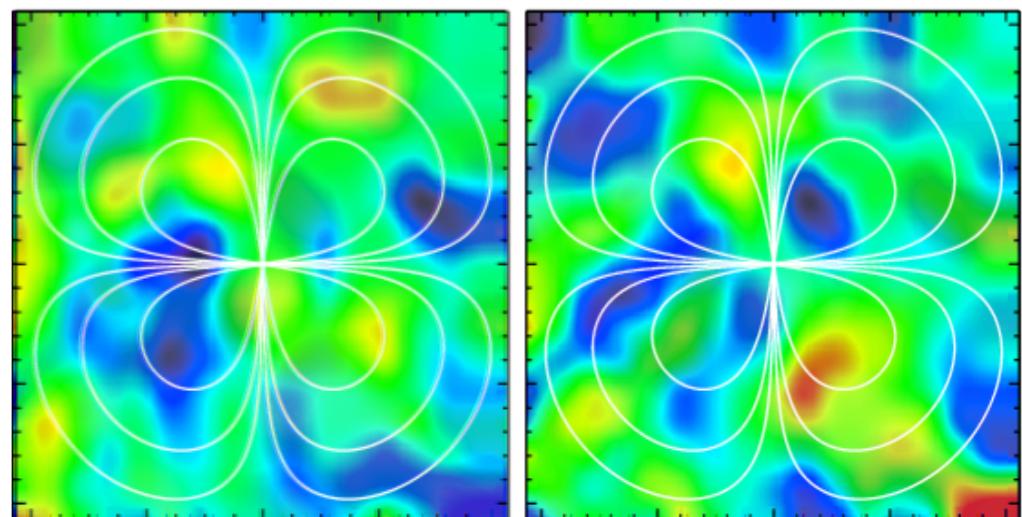
Wave Plate:
 Q/U mixing
plus
 Q/U modulation



Cross-Polar Beam Systematics

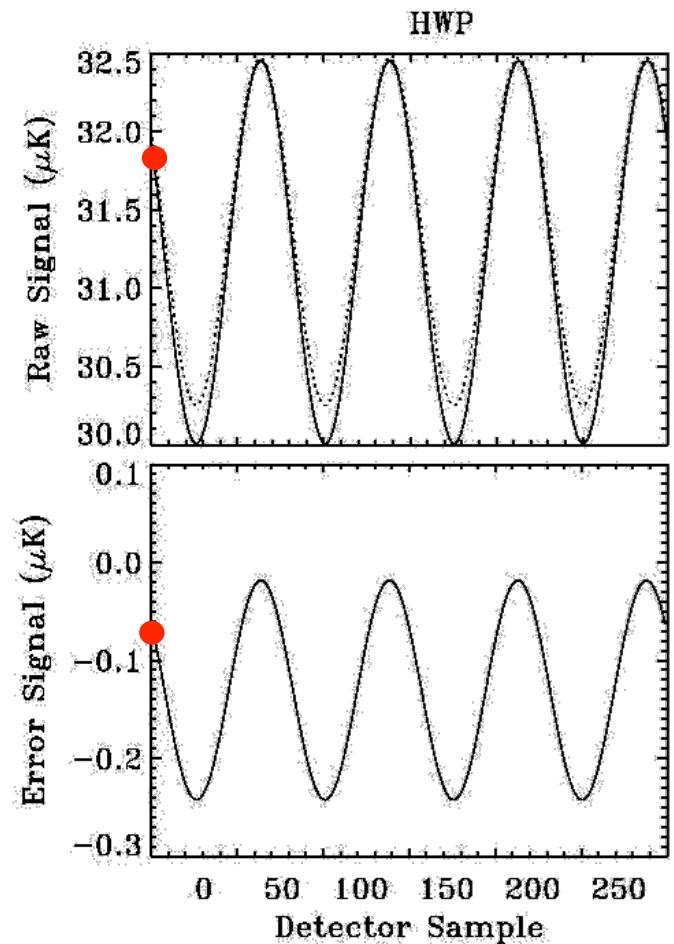


True
Sky

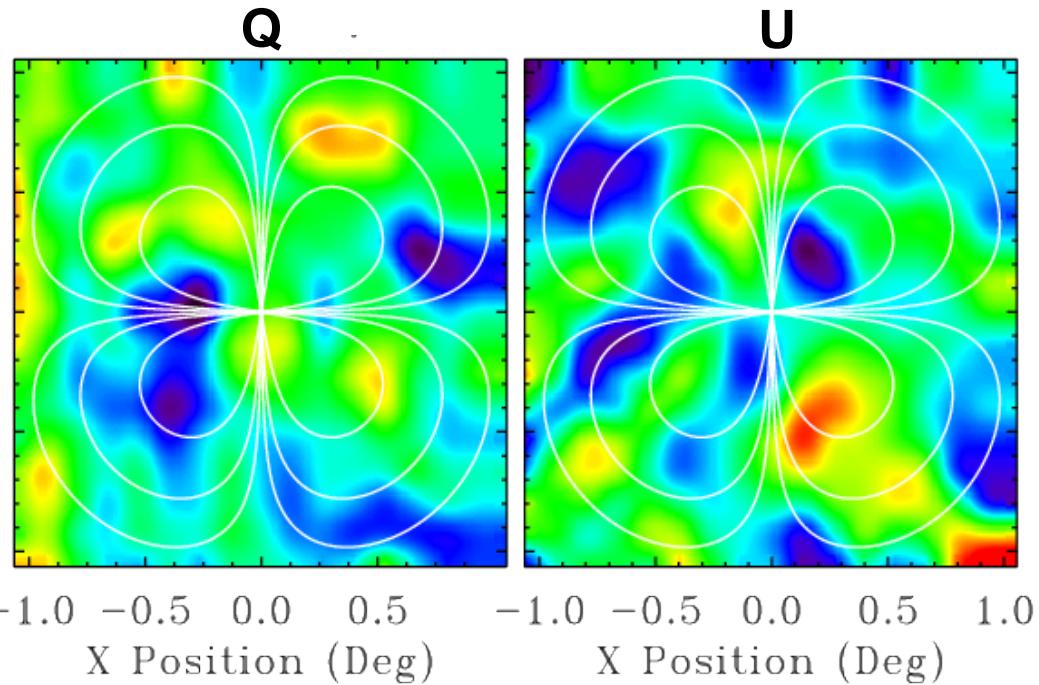


After
HWP
Modulation

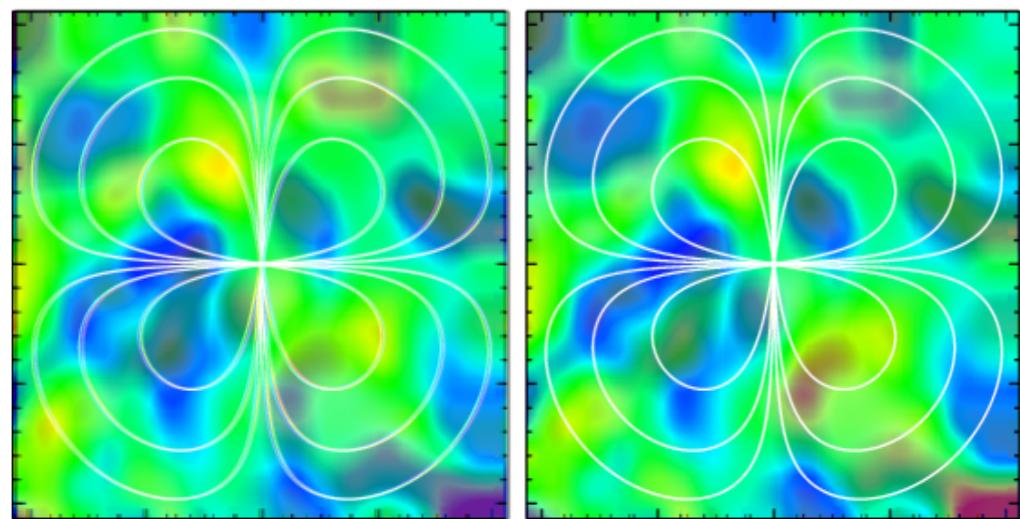
Wave Plate:
 Q/U mixing
plus
 Q/U modulation



Cross-Polar Beam Systematics

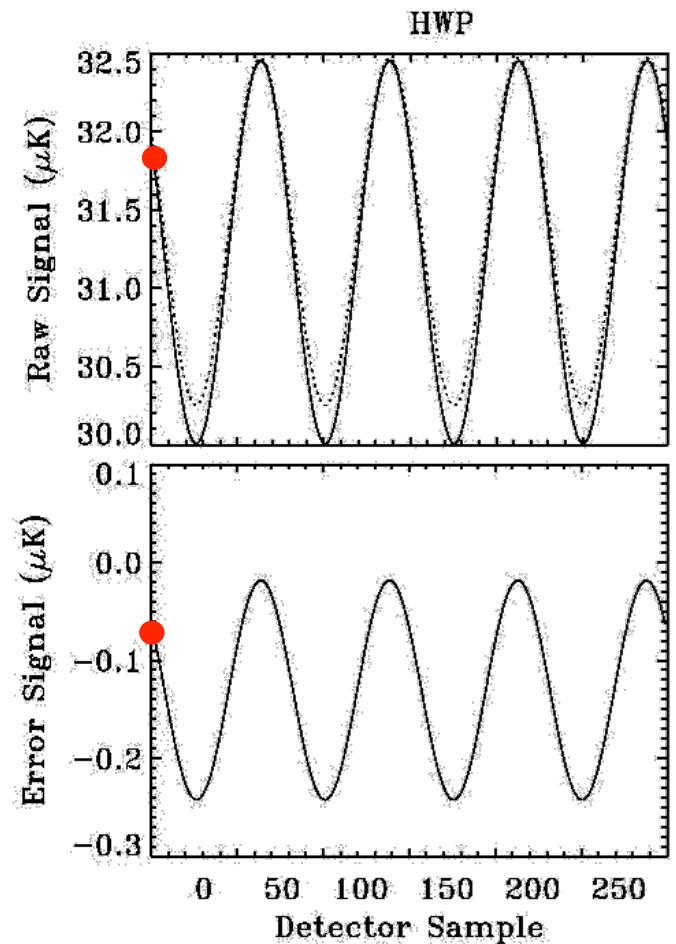


True
Sky

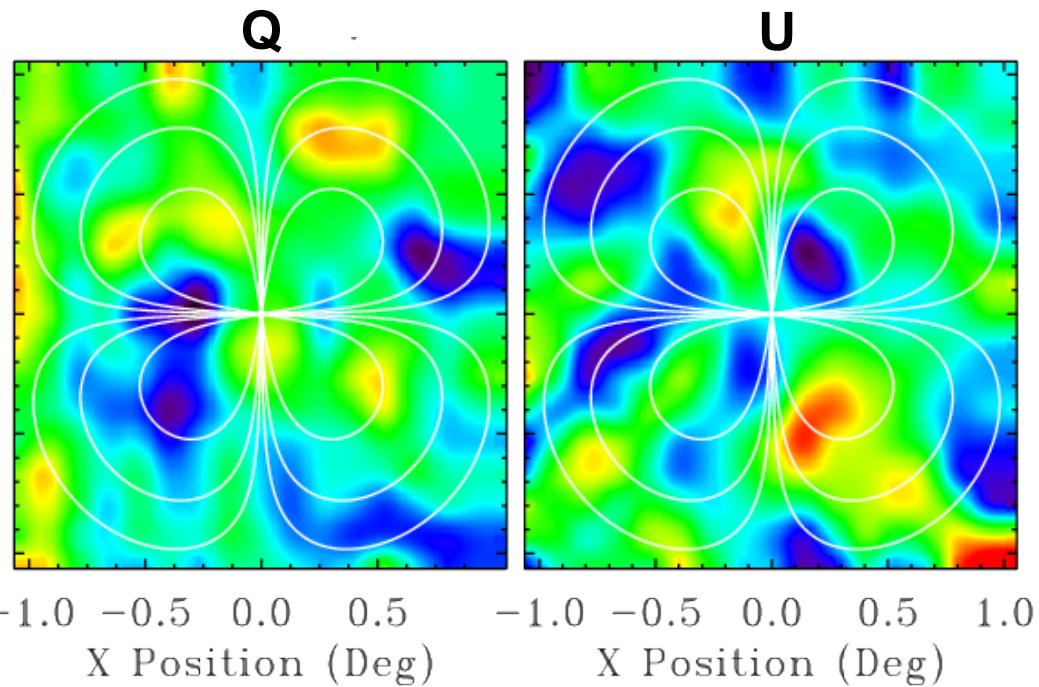


After
HWP
Modulation

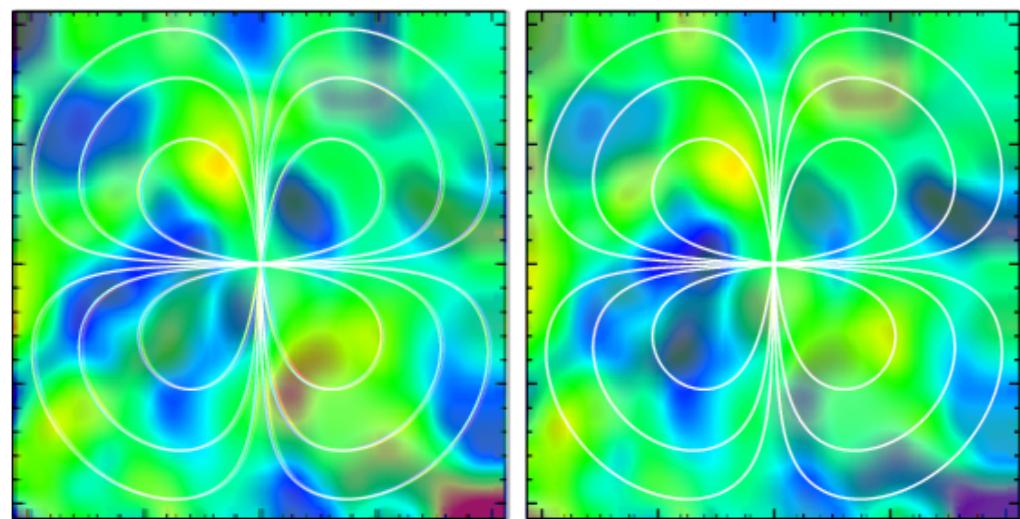
Wave Plate:
 Q/U mixing
plus
 Q/U modulation



Cross-Polar Beam Systematics

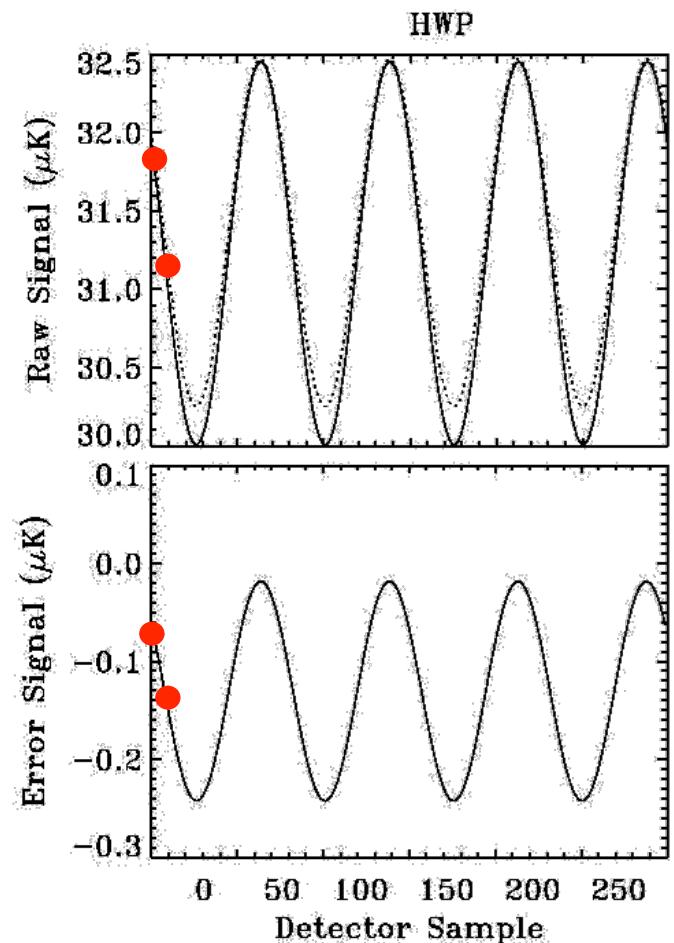


True
Sky

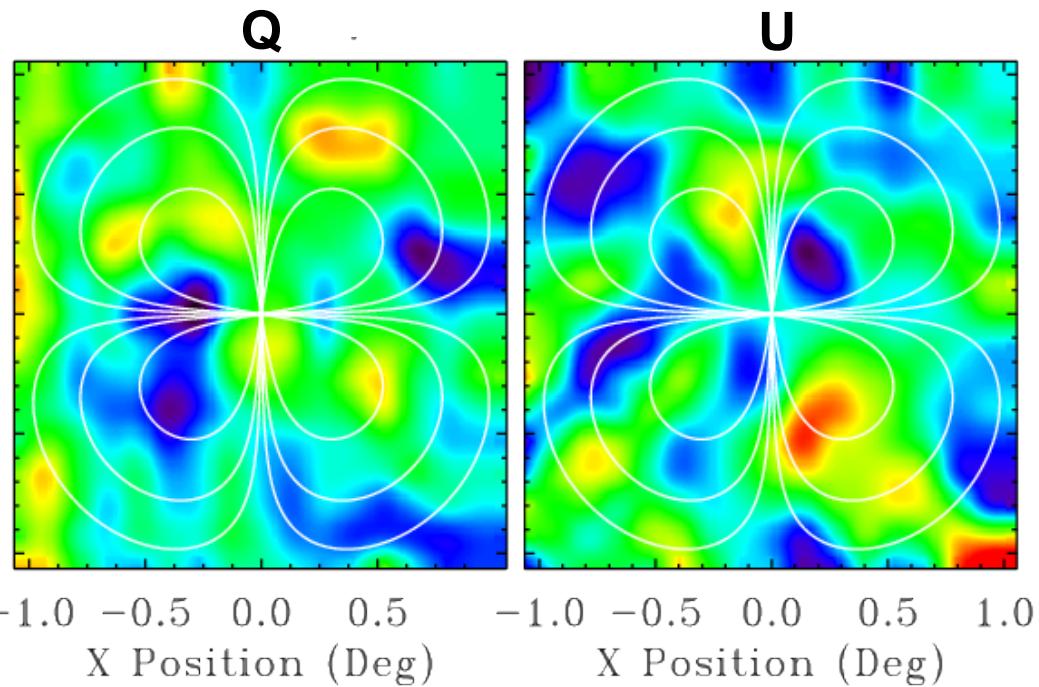


After
HWP
Modulation

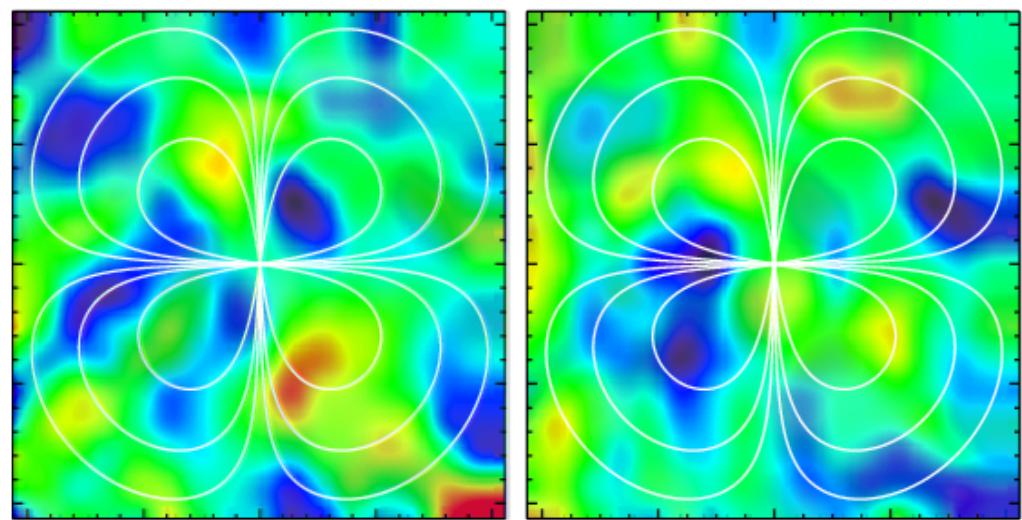
Wave Plate:
 Q/U mixing
plus
 Q/U modulation



Cross-Polar Beam Systematics

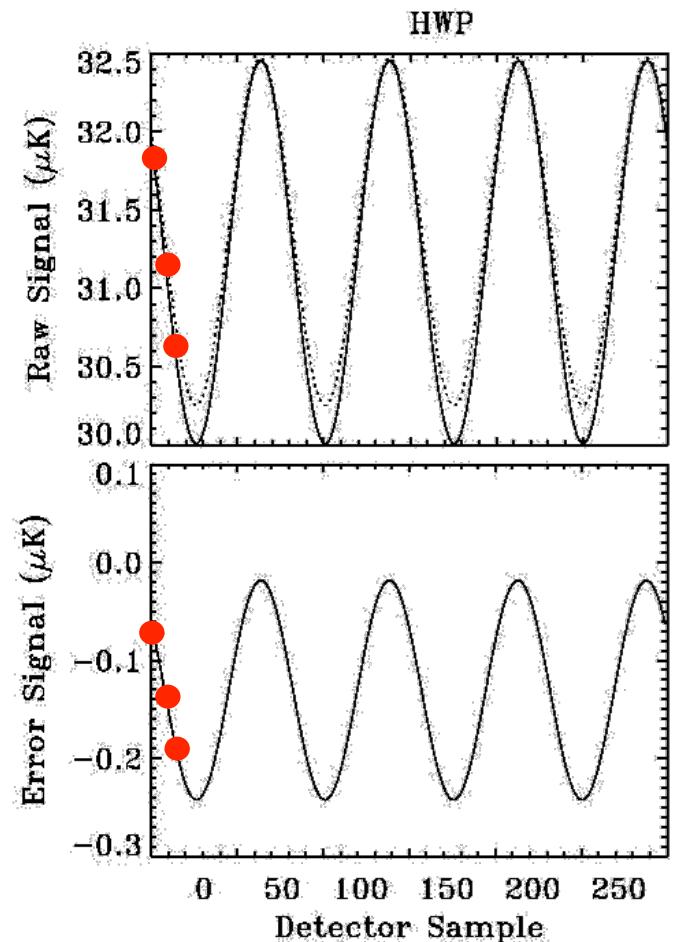


True
Sky

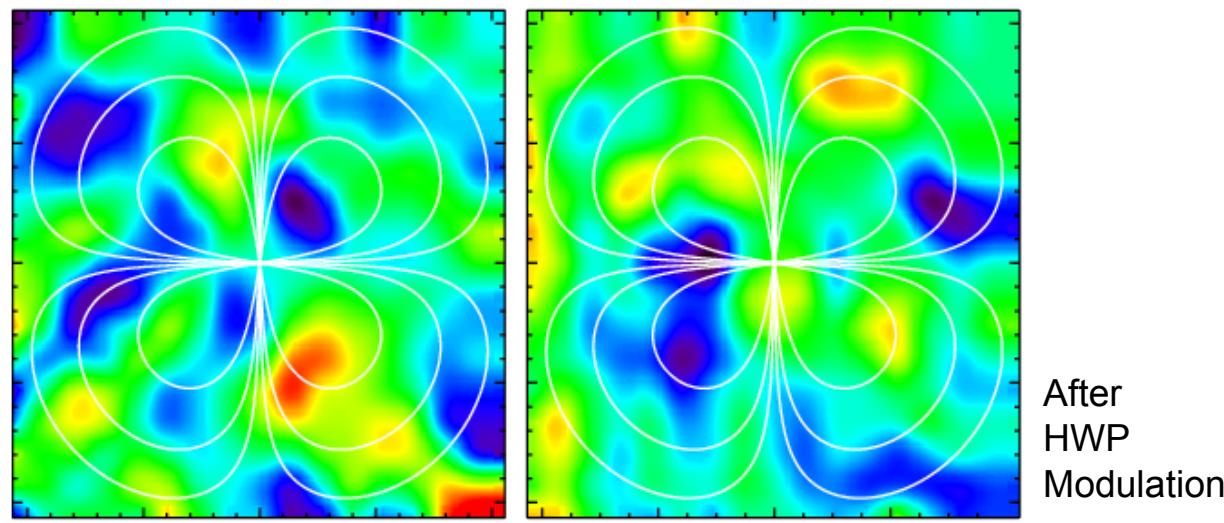
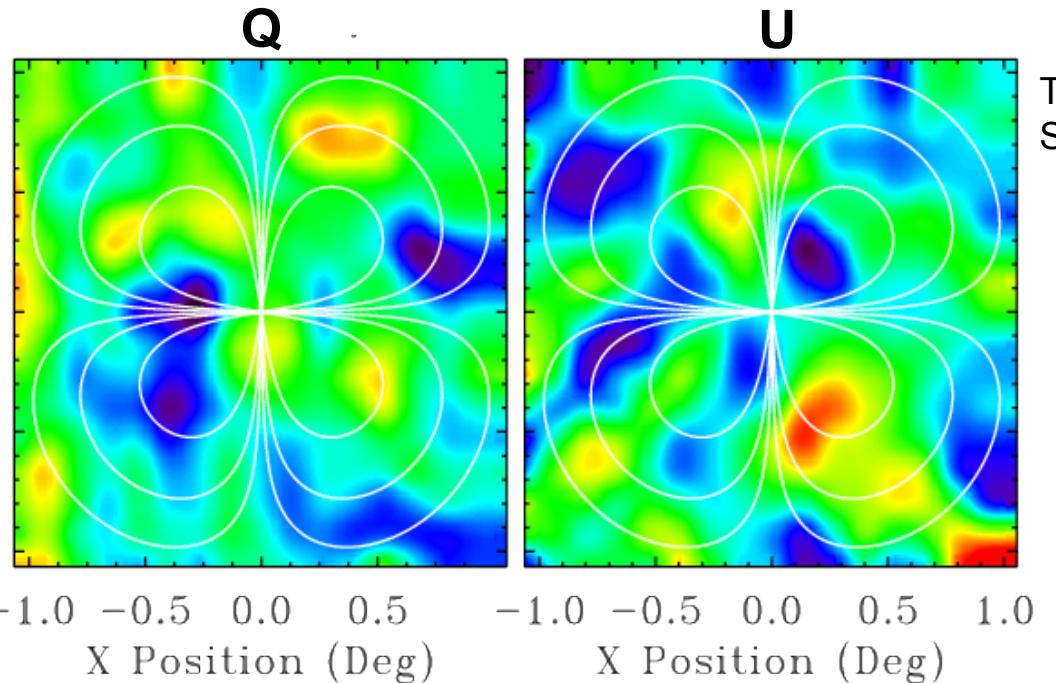


After
HWP
Modulation

Wave Plate:
 Q/U mixing
plus
 Q/U modulation

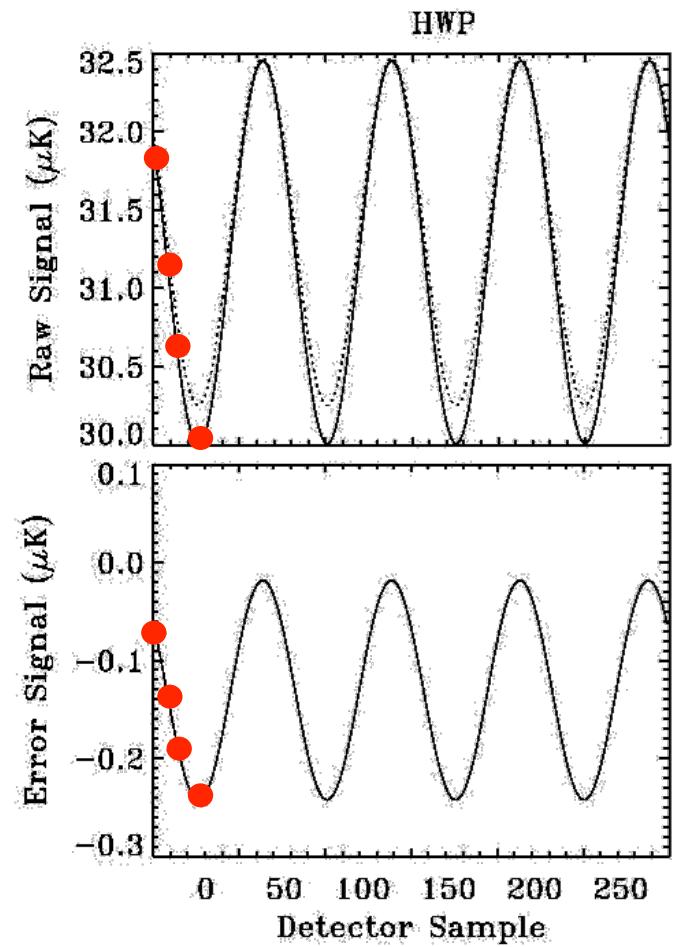


Cross-Polar Beam Systematics

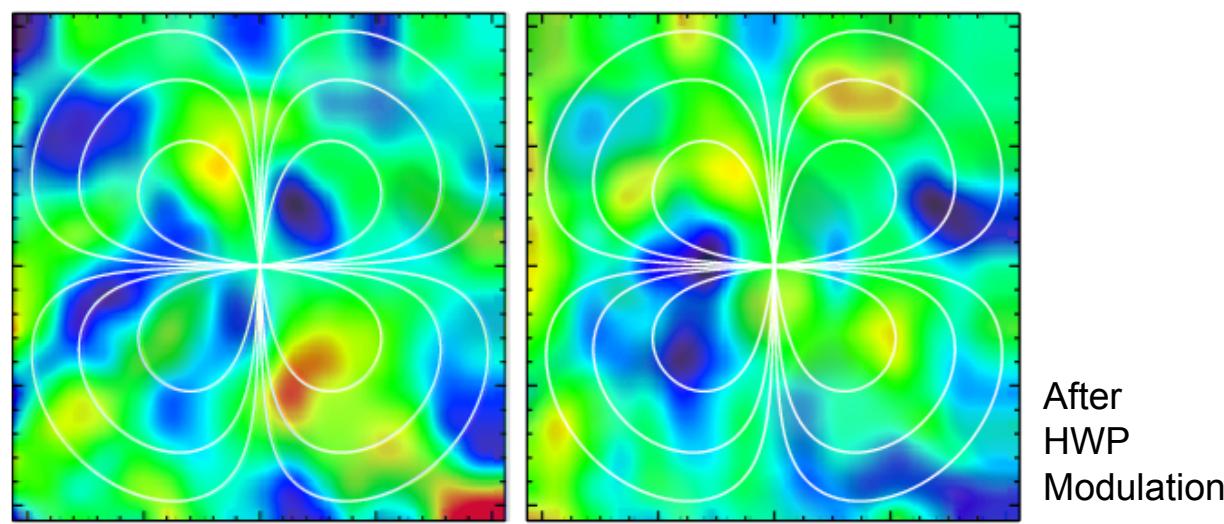
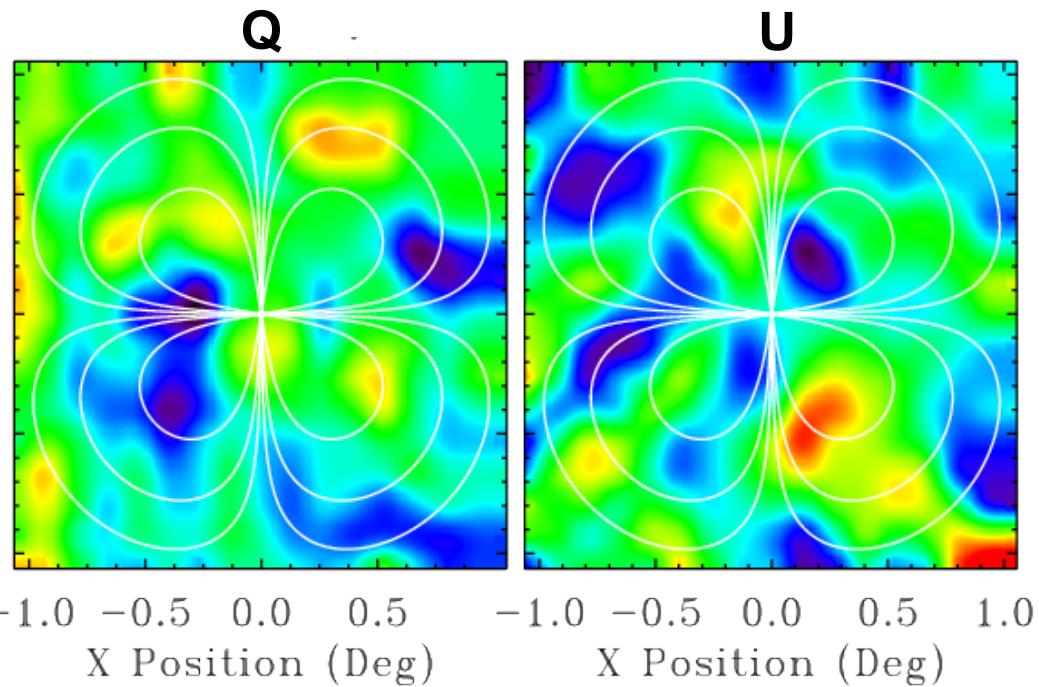


True
Sky

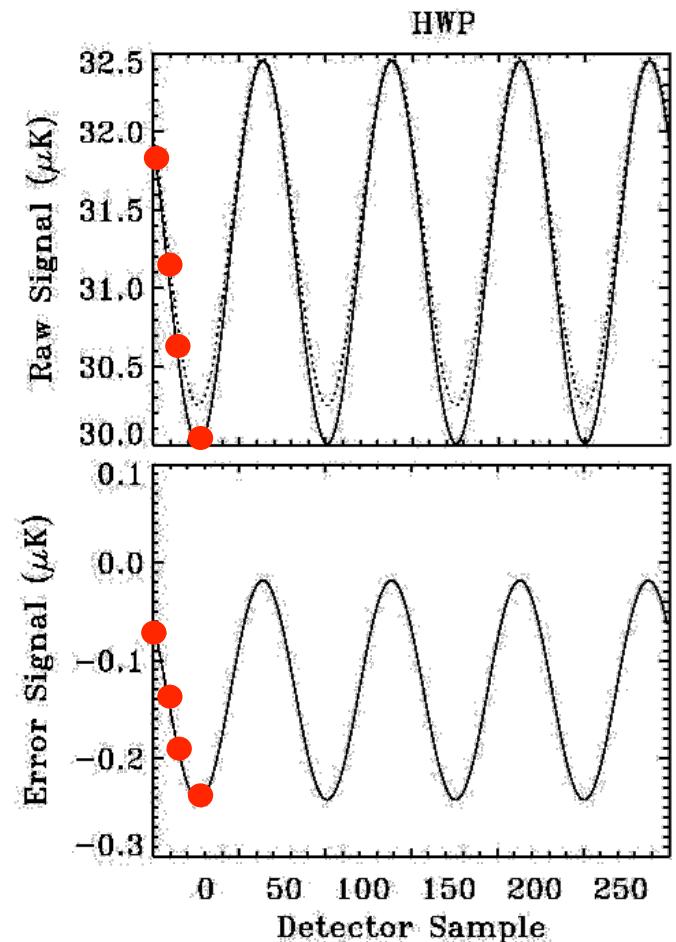
Wave Plate:
 Q/U mixing
plus
 Q/U modulation



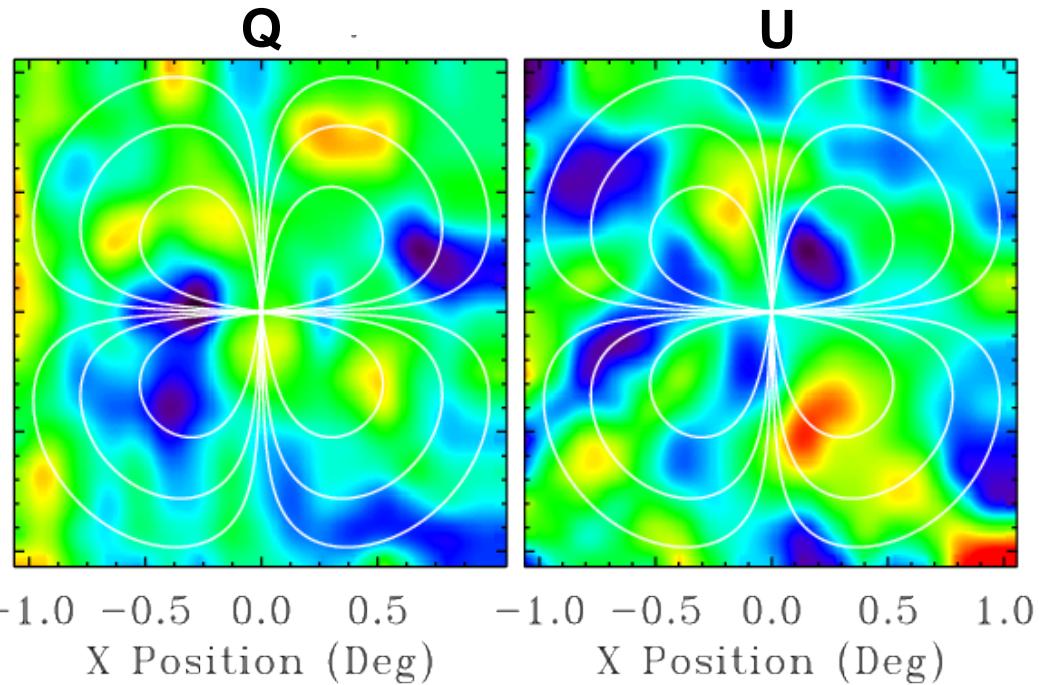
Cross-Polar Beam Systematics



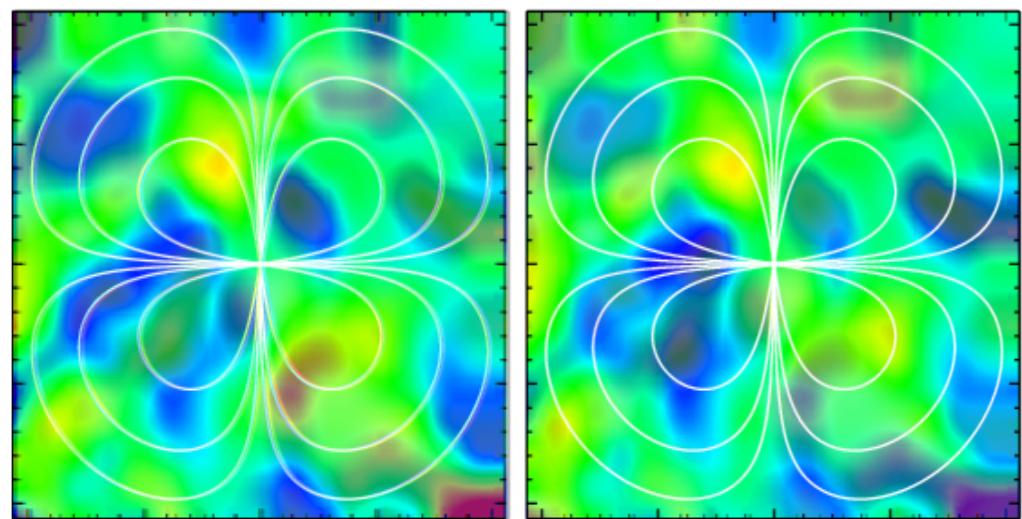
Wave Plate:
Q/U mixing
plus
Q/U modulation



Cross-Polar Beam Systematics

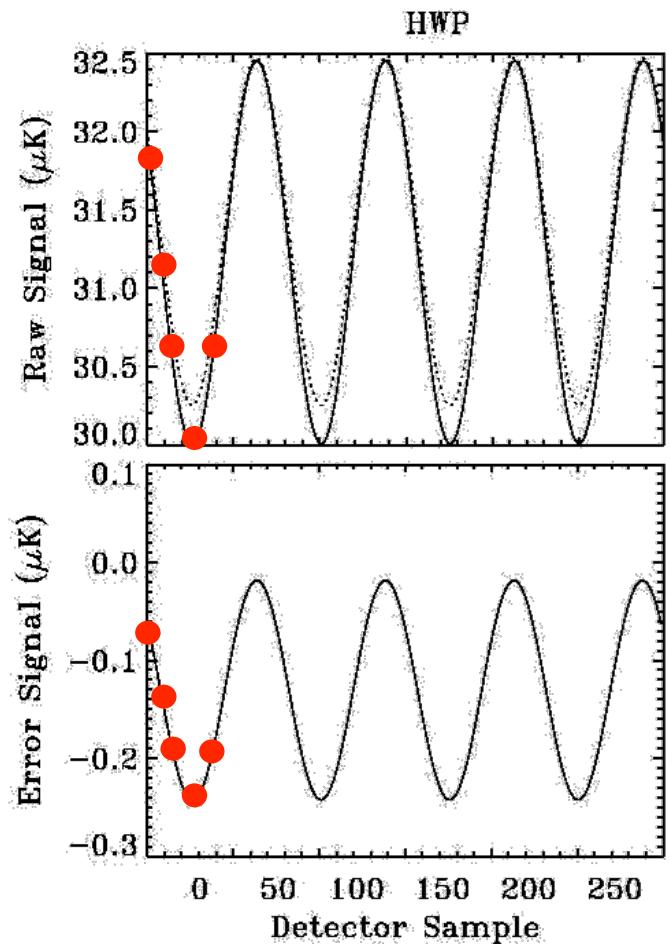


True
Sky

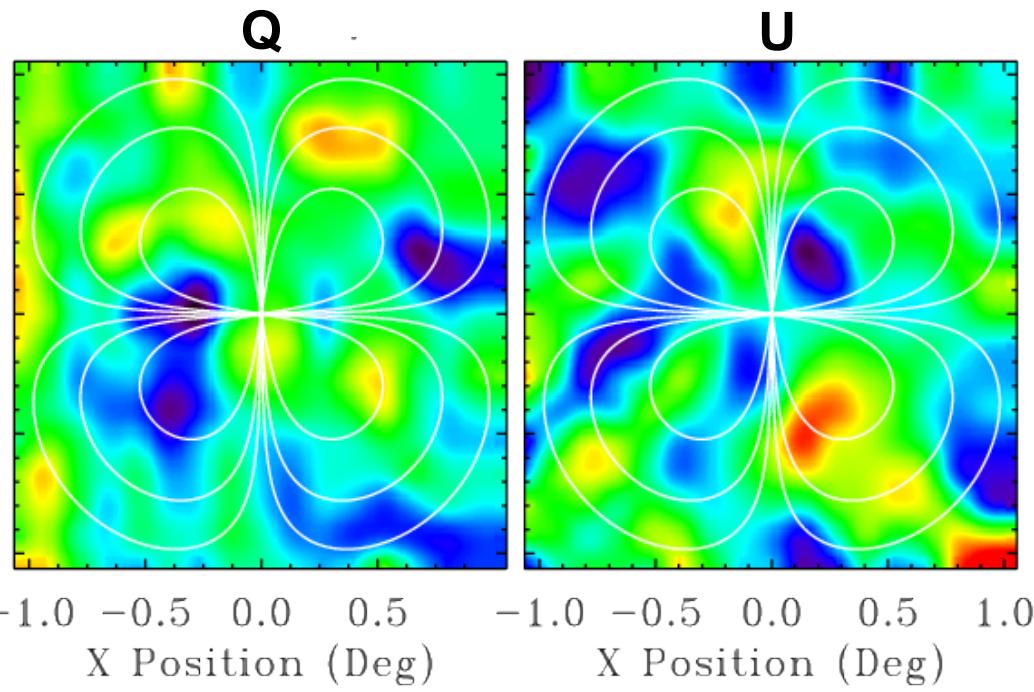


After
HWP
Modulation

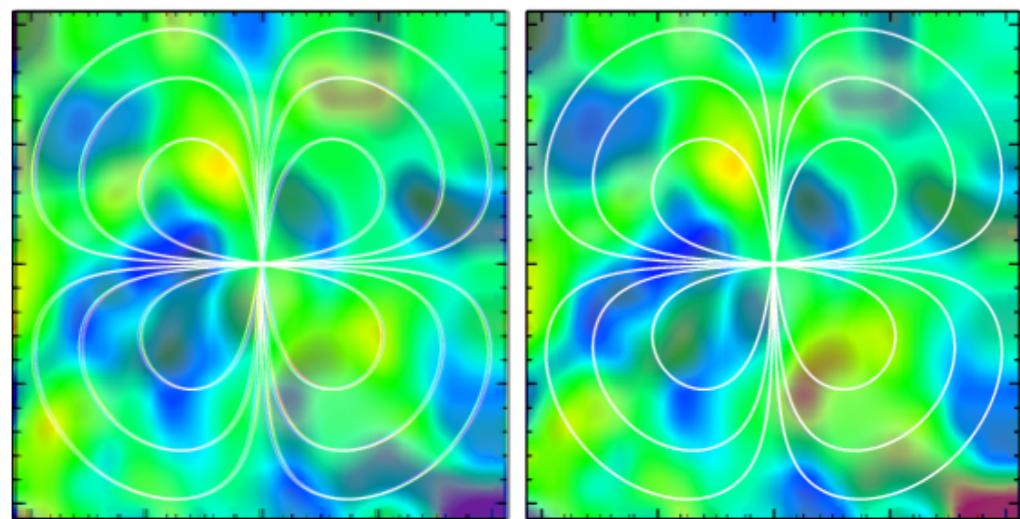
Wave Plate:
 Q/U mixing
plus
 Q/U modulation



Cross-Polar Beam Systematics

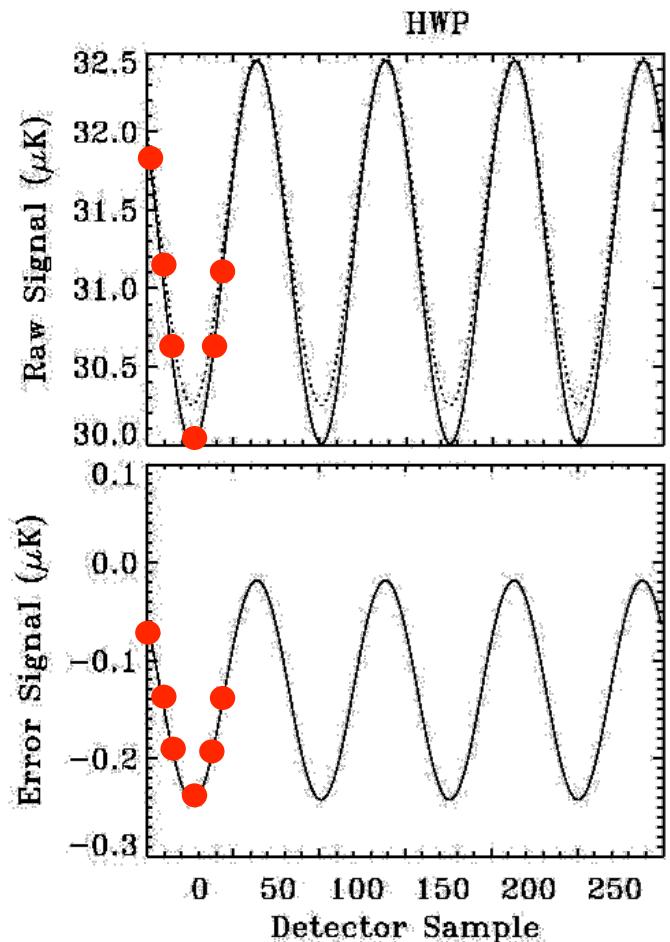


True
Sky

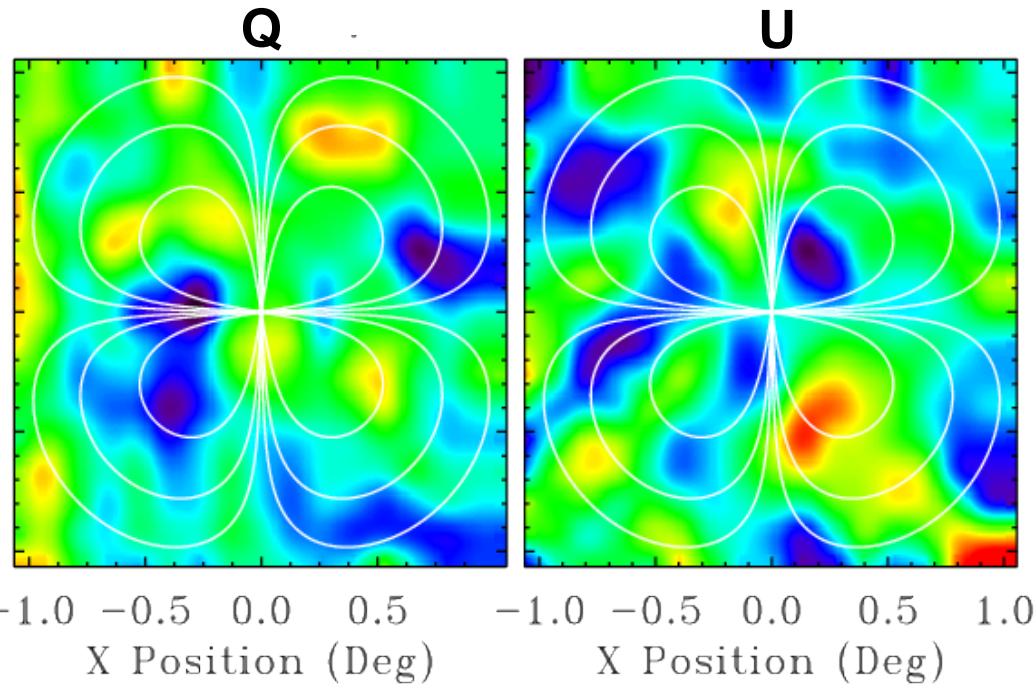


After
HWP
Modulation

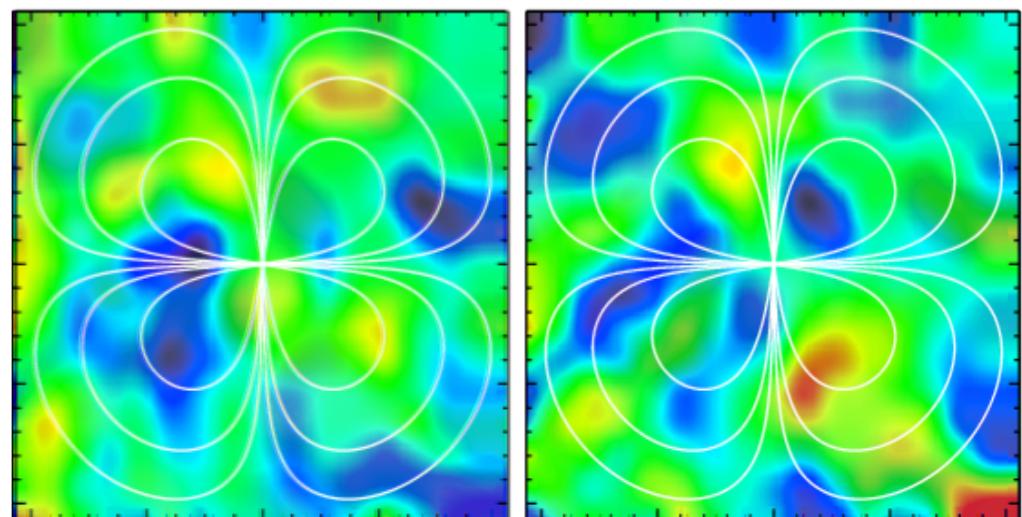
Wave Plate:
 Q/U mixing
plus
 Q/U modulation



Cross-Polar Beam Systematics

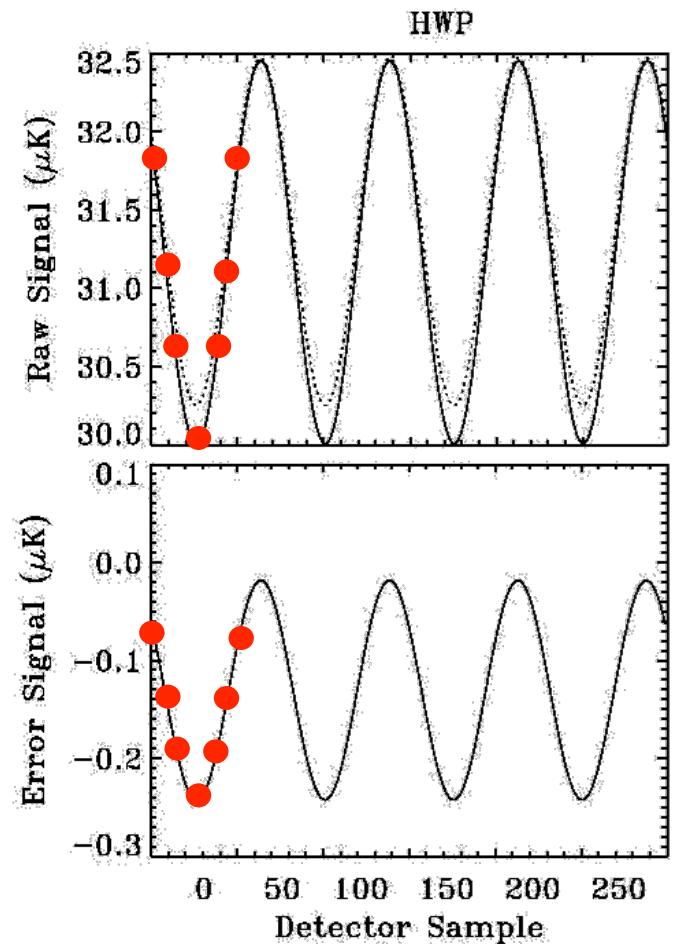


True
Sky

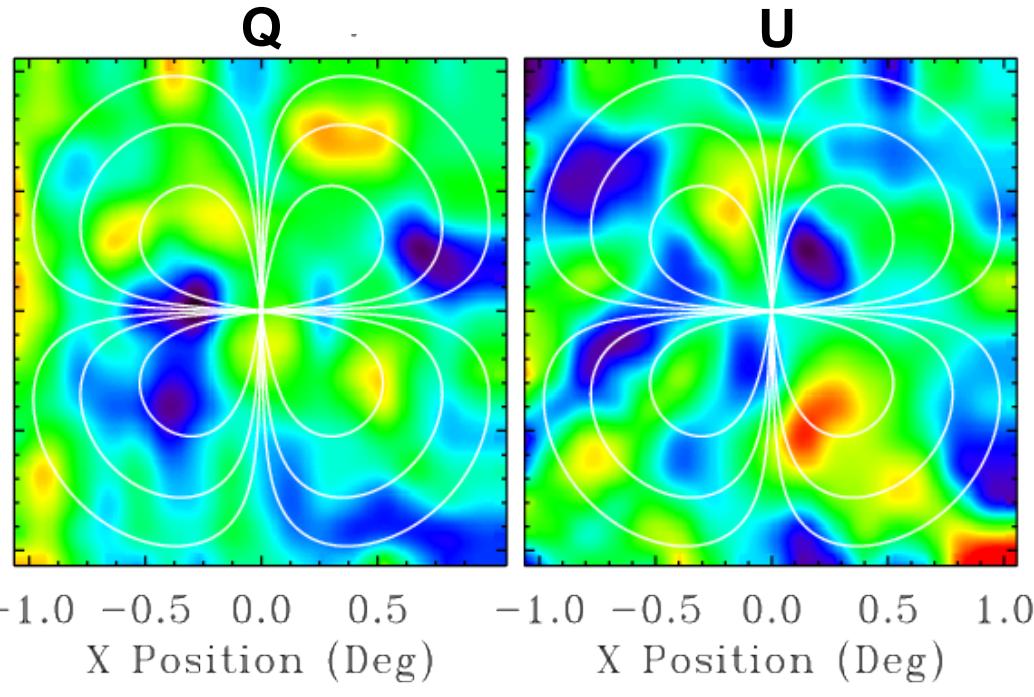


After
HWP
Modulation

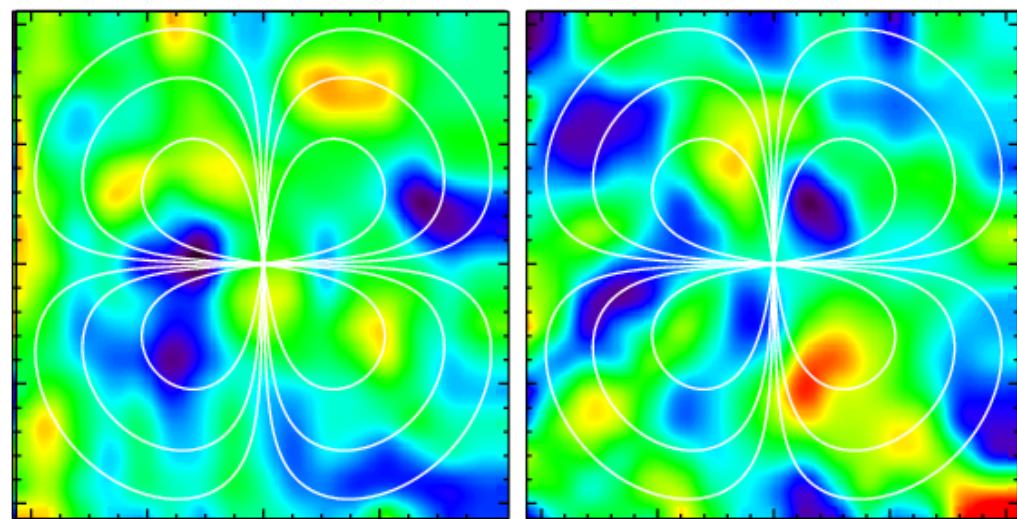
Wave Plate:
 Q/U mixing
plus
 Q/U modulation



Cross-Polar Beam Systematics

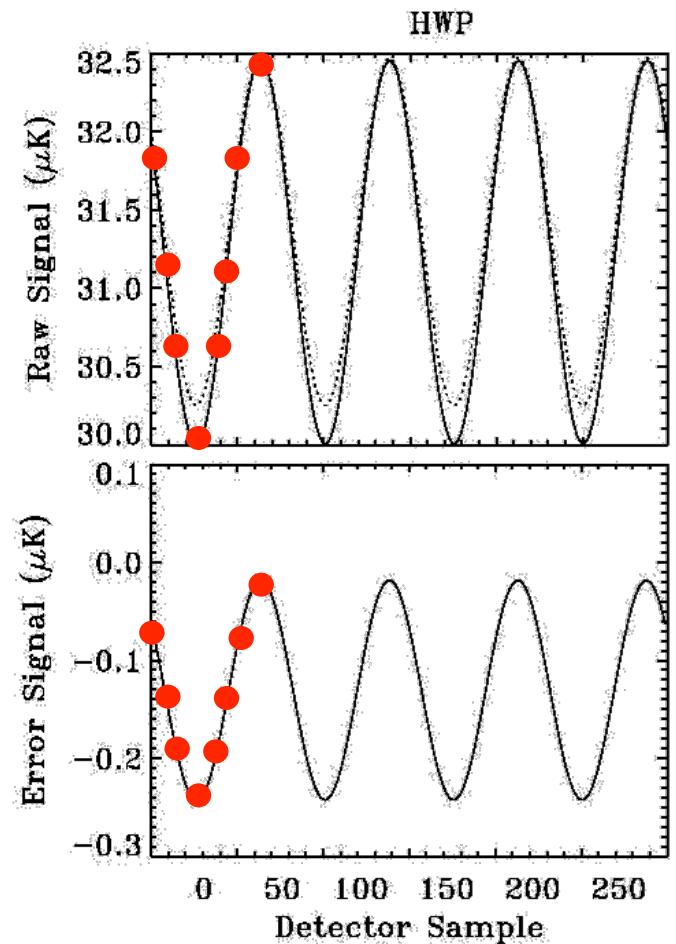


True
Sky

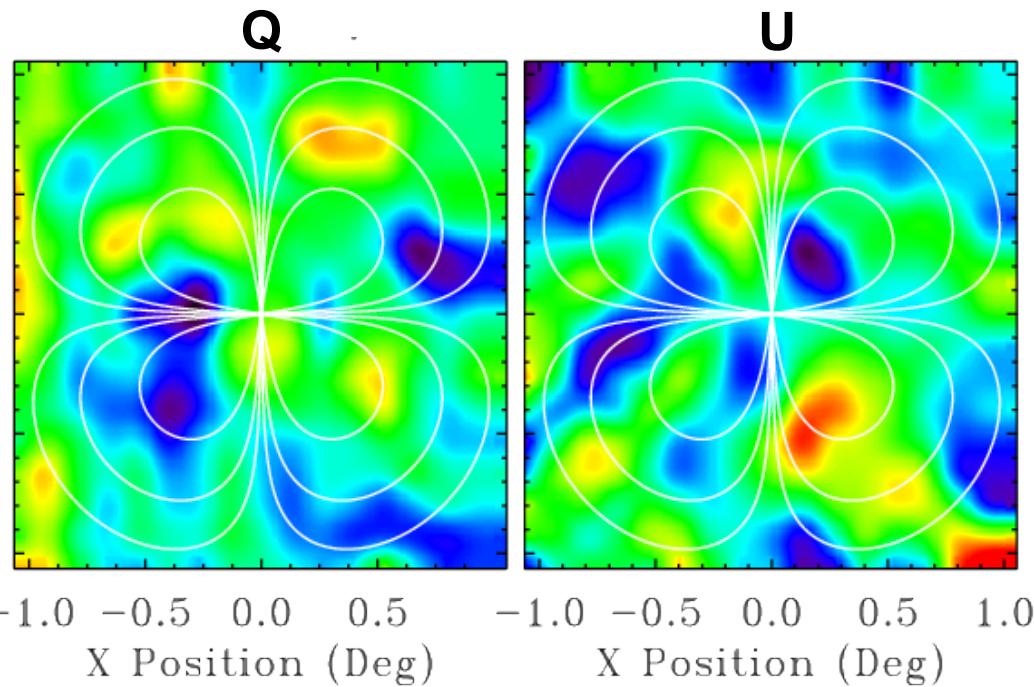


After
HWP
Modulation

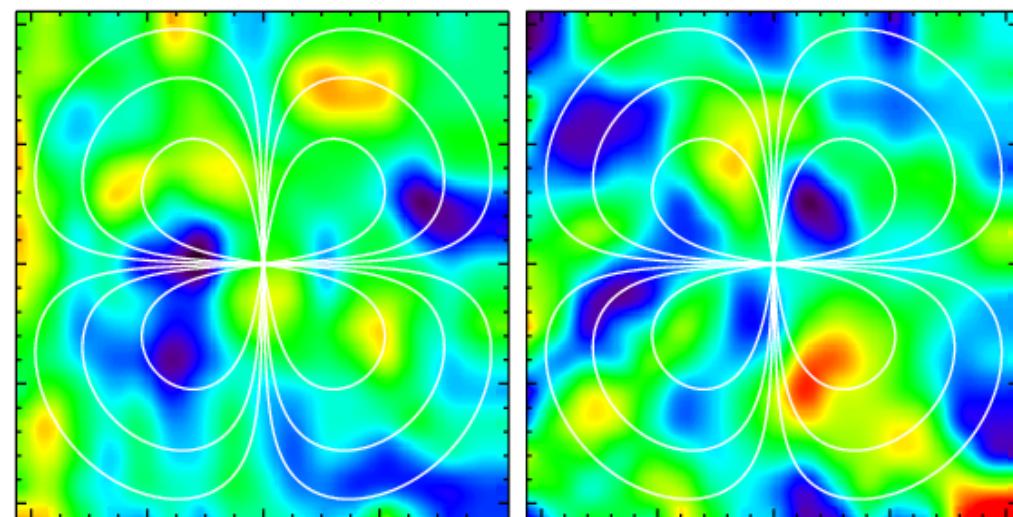
Wave Plate:
 Q/U mixing
plus
 Q/U modulation



Cross-Polar Beam Systematics

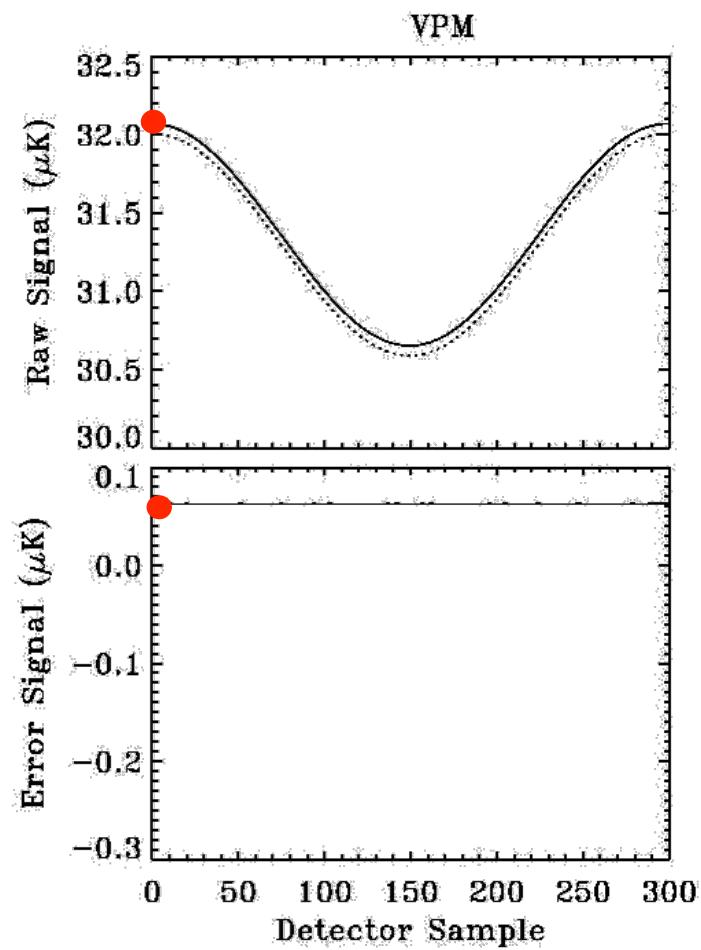


True
Sky

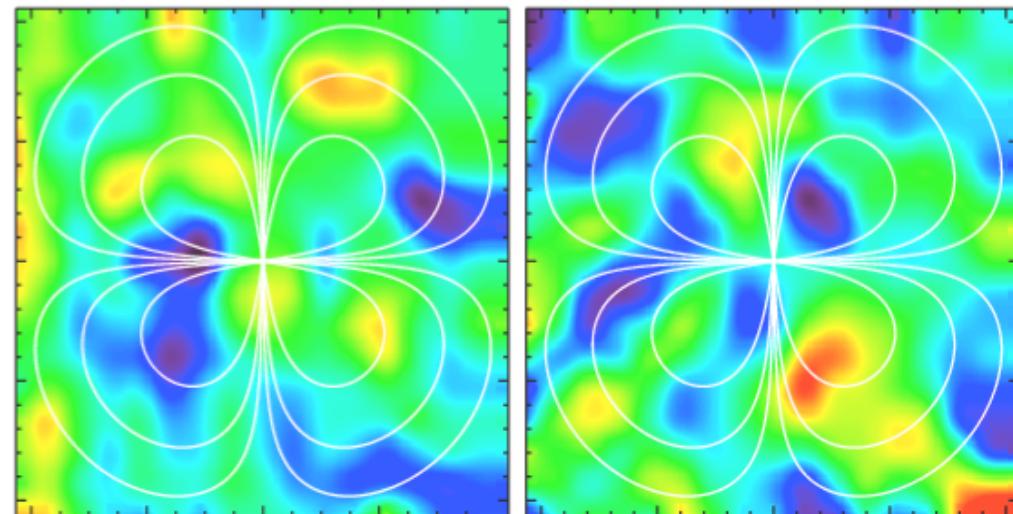
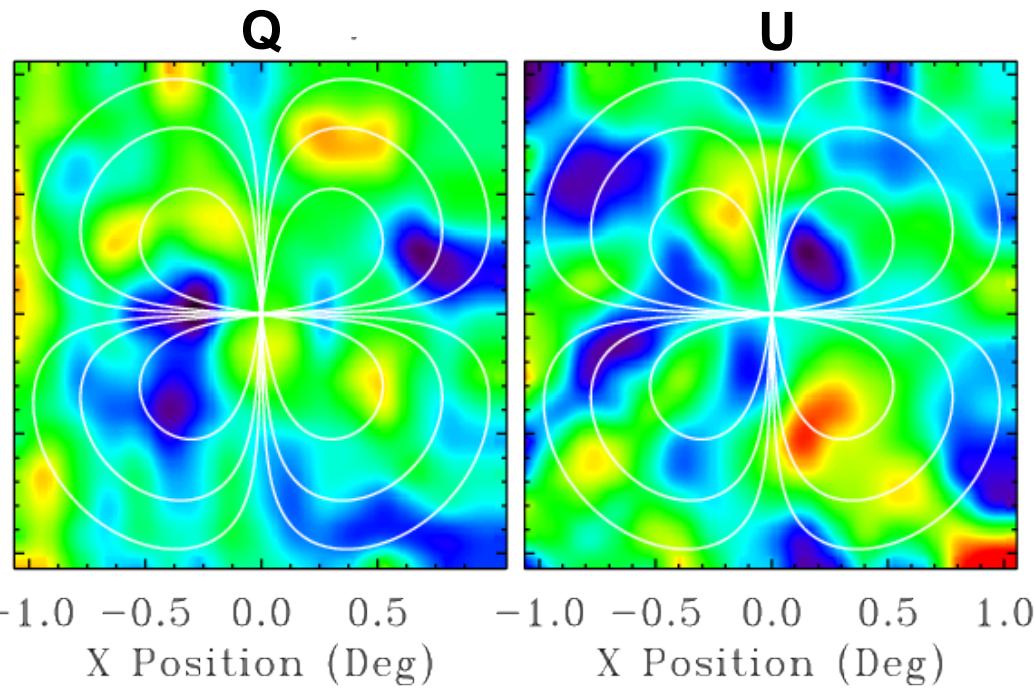


After
VPM
Modulation

VPM:
 Q/U mixing
but
 Q/V modulation



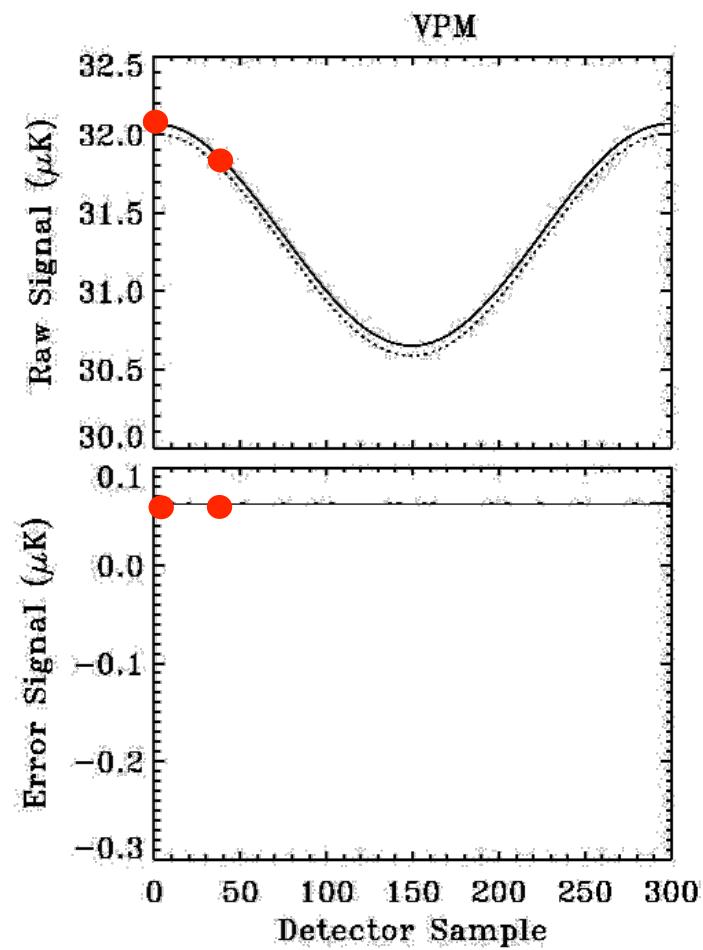
Cross-Polar Beam Systematics



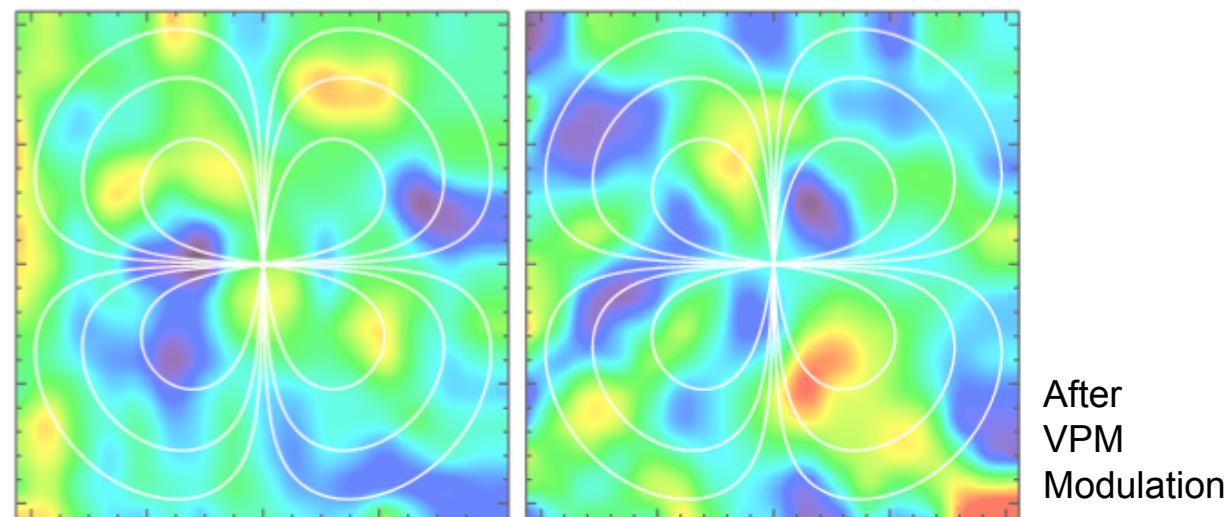
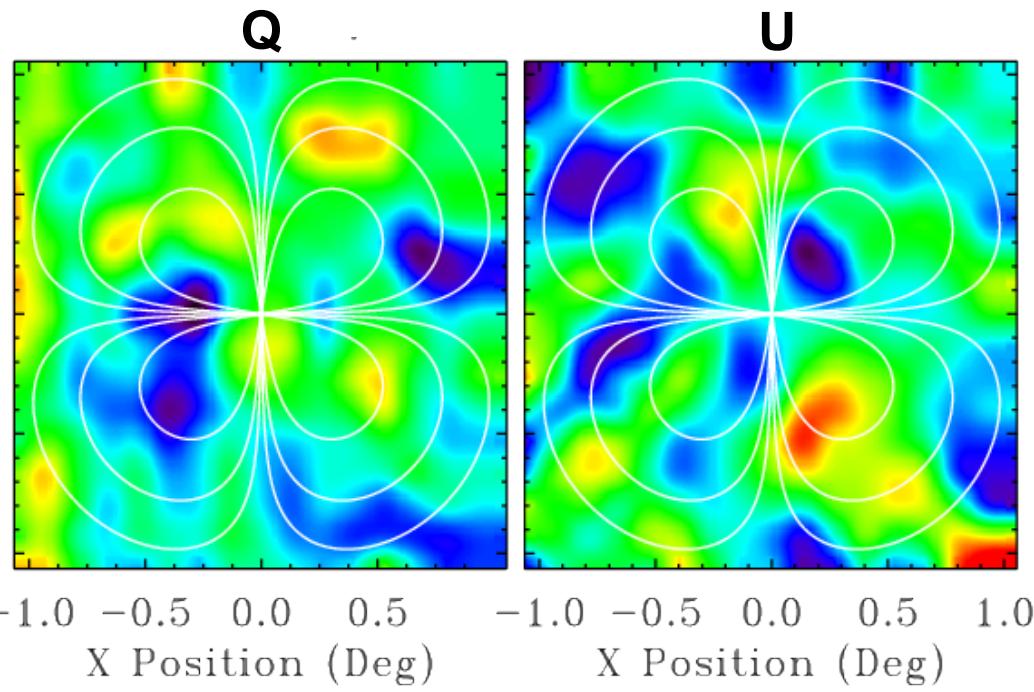
True
Sky

After
VPM
Modulation

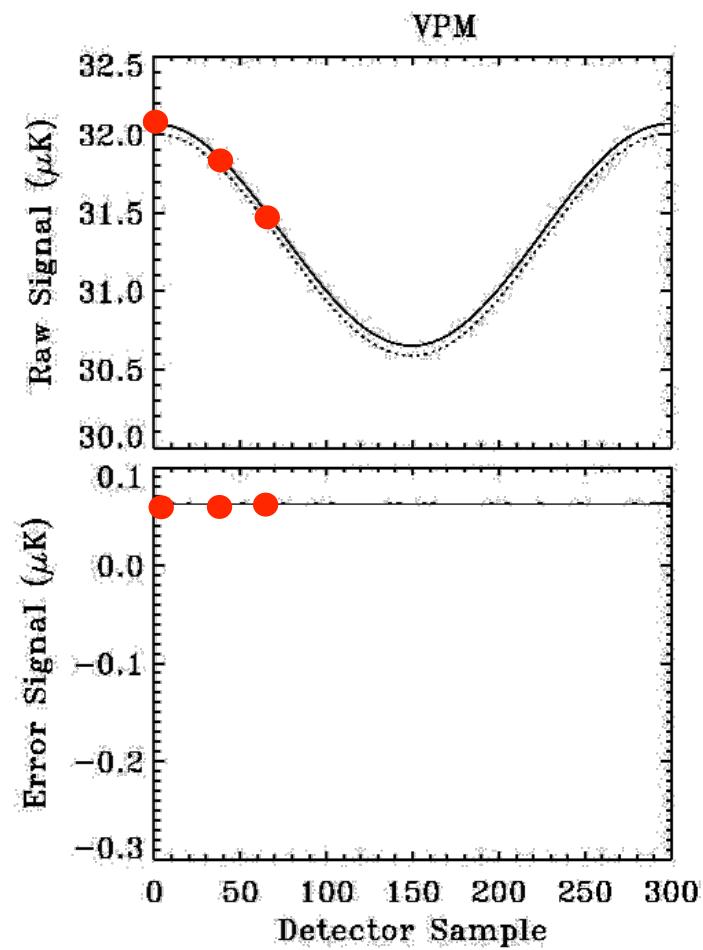
VPM:
Q/U mixing
but
Q/V modulation



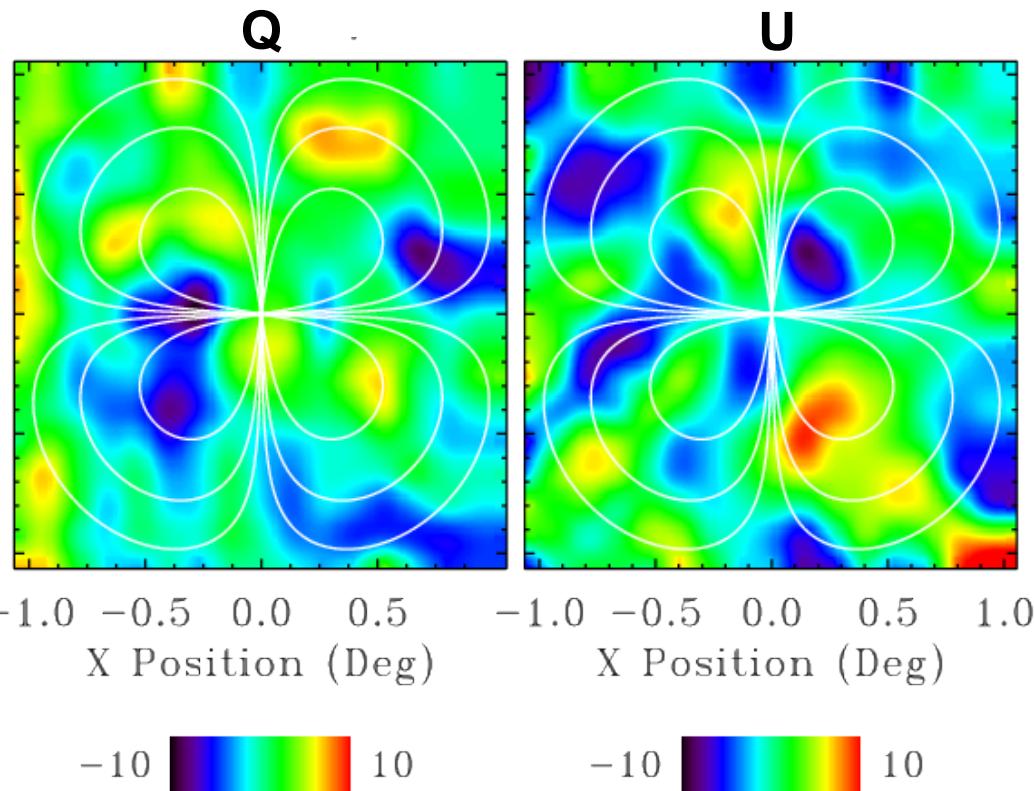
Cross-Polar Beam Systematics



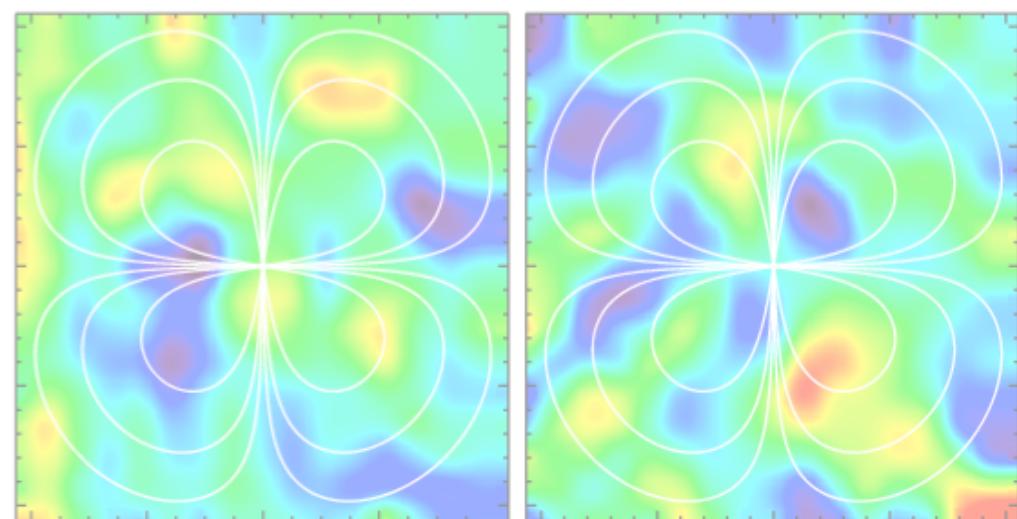
VPM:
Q/U mixing
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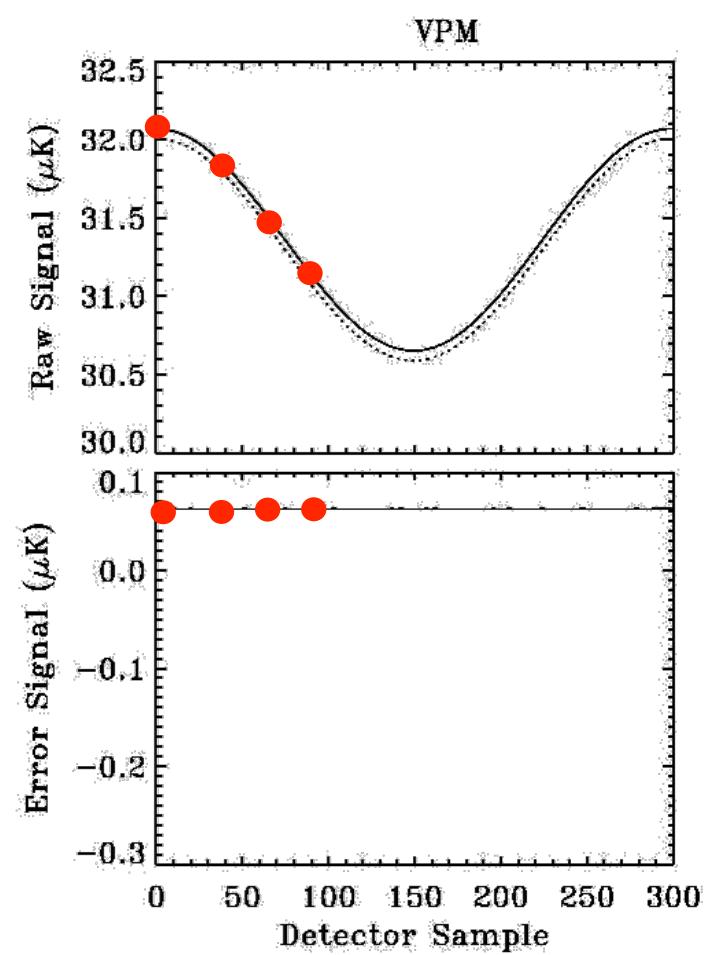
Cross-Polar Beam Systematics



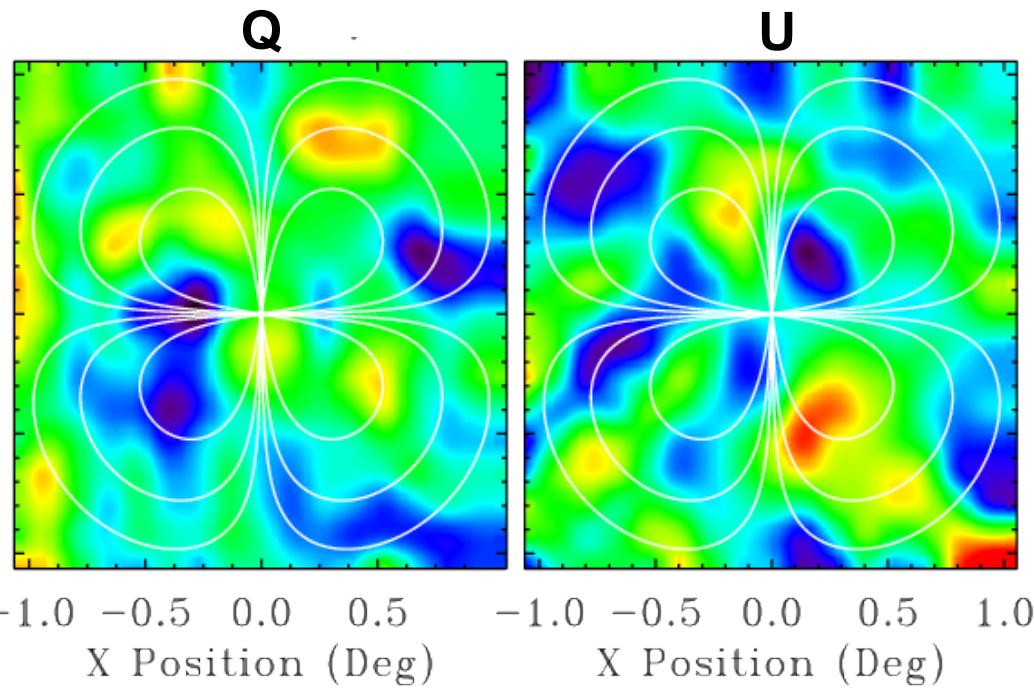
True
Sky



After
VPM
Modulation

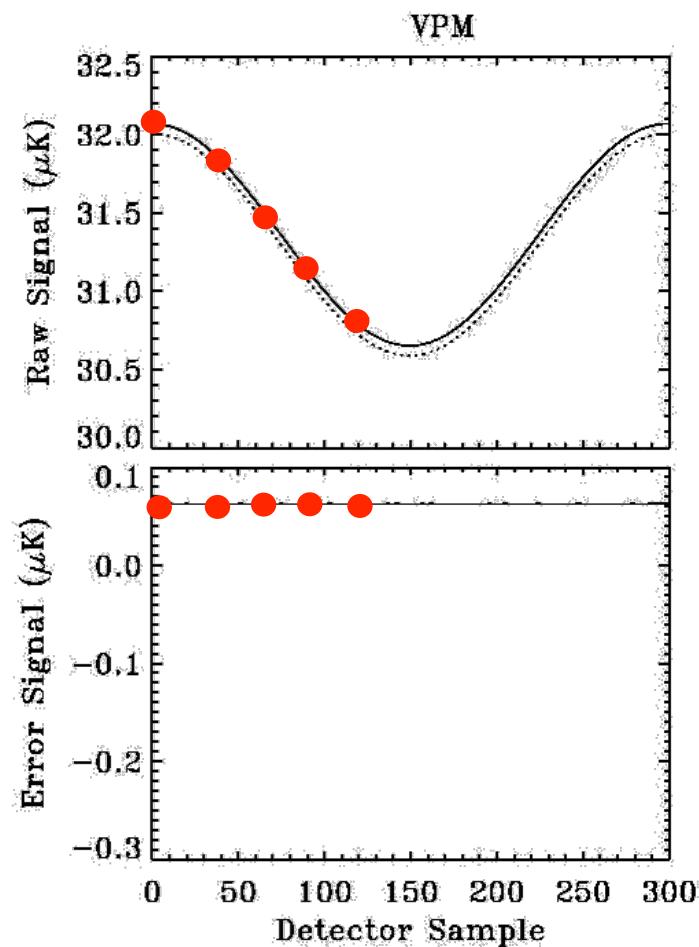


Cross-Polar Beam Systematics

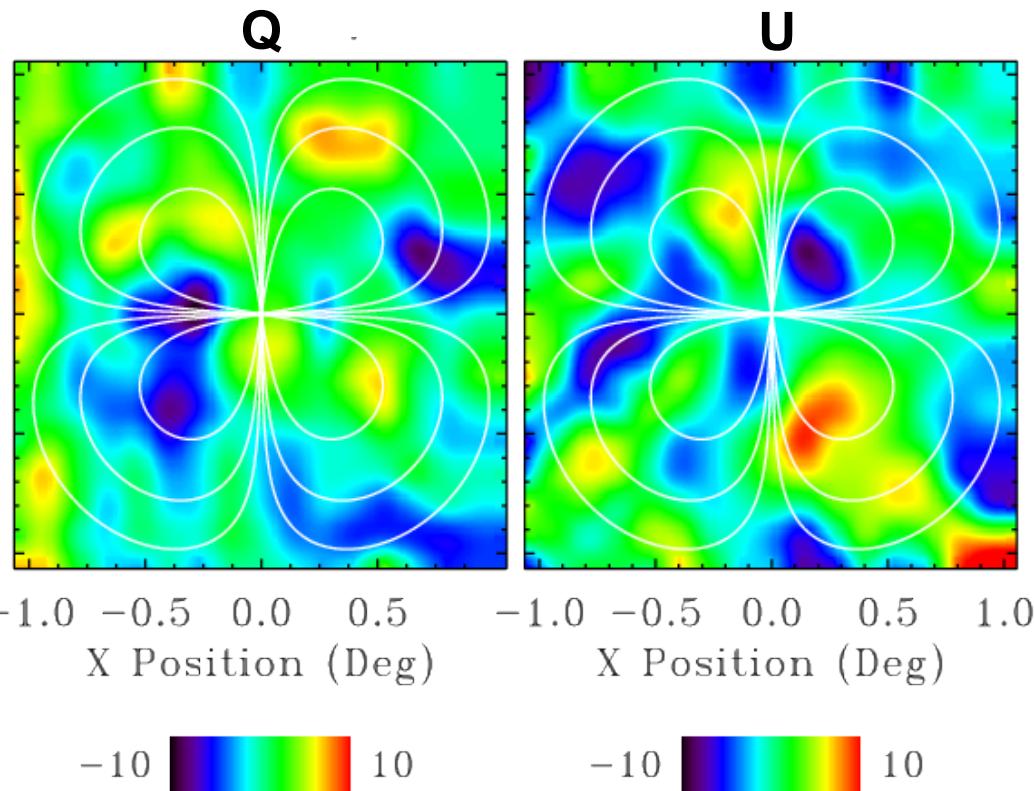


True
Sky

VPM:
Q/U mixing
but
Q/V modulation



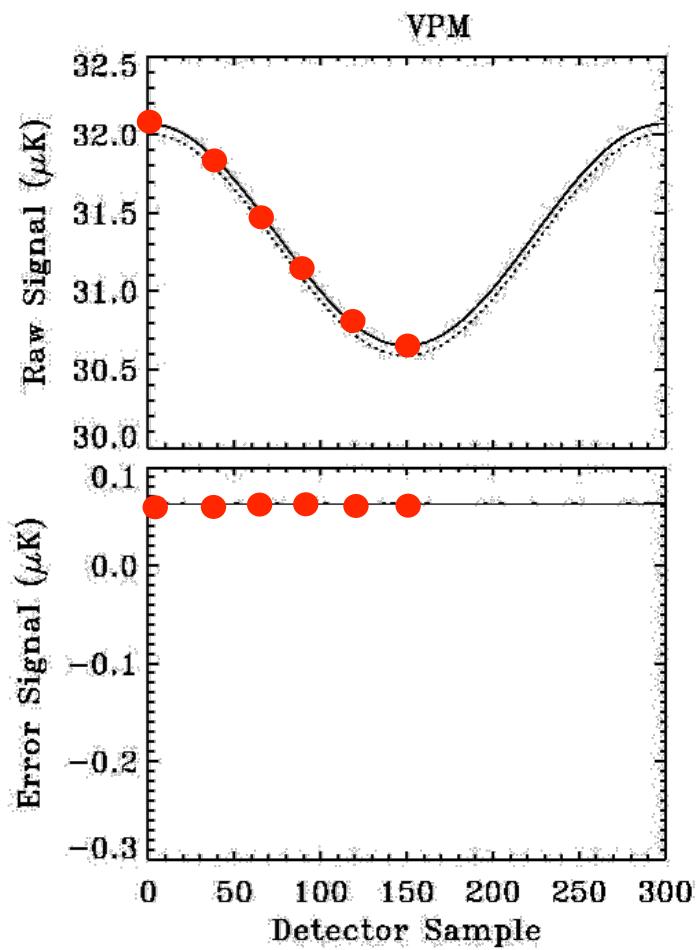
Cross-Polar Beam Systematics



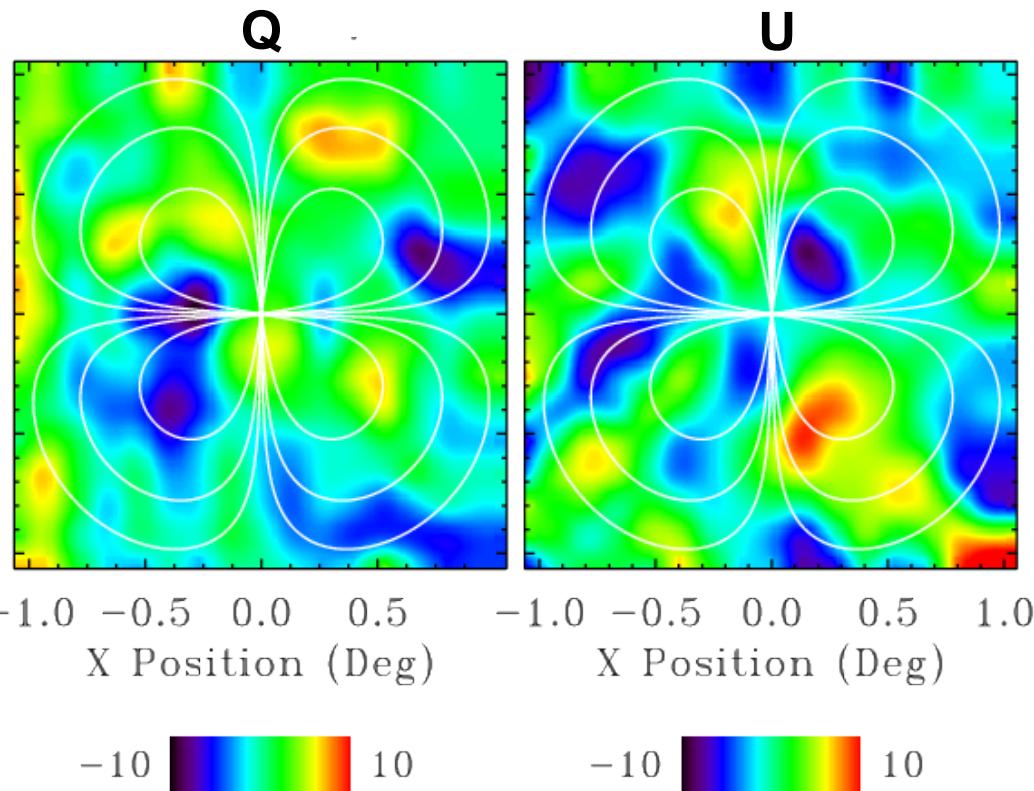
True
Sky

After
VPM
Modulation

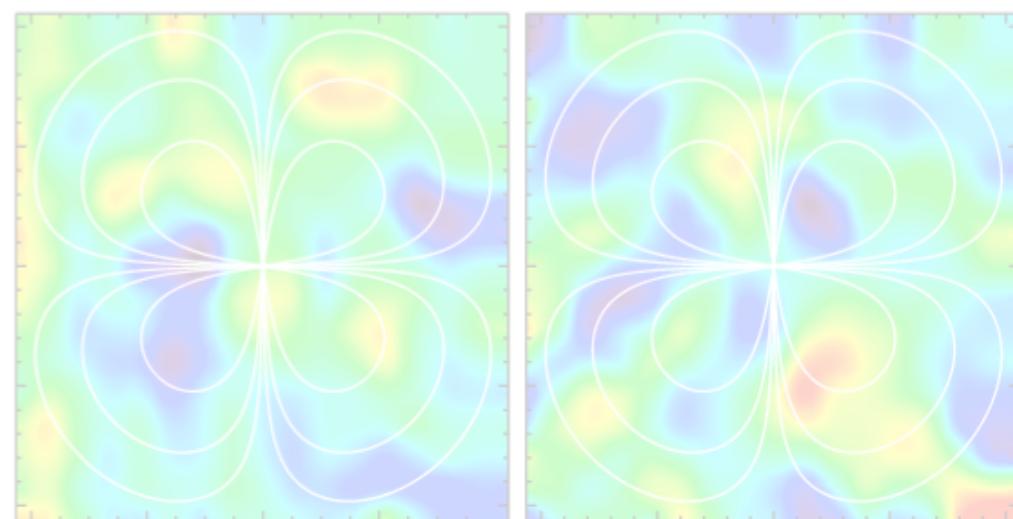
VPM:
Q/U mixing
but
Q/V modulation



Cross-Polar Beam Systematics

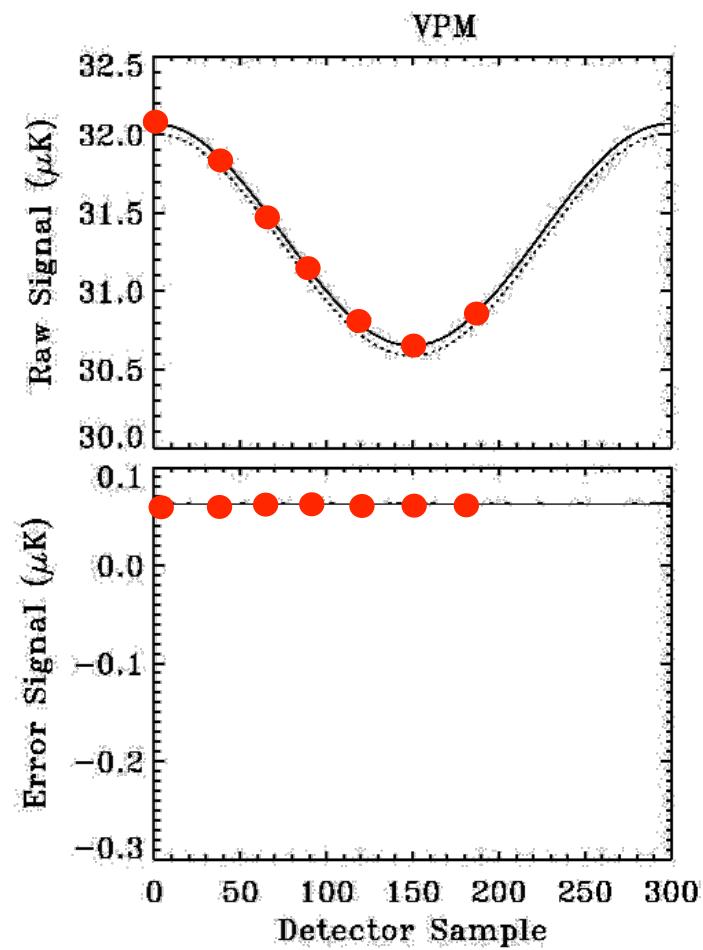


True
Sky

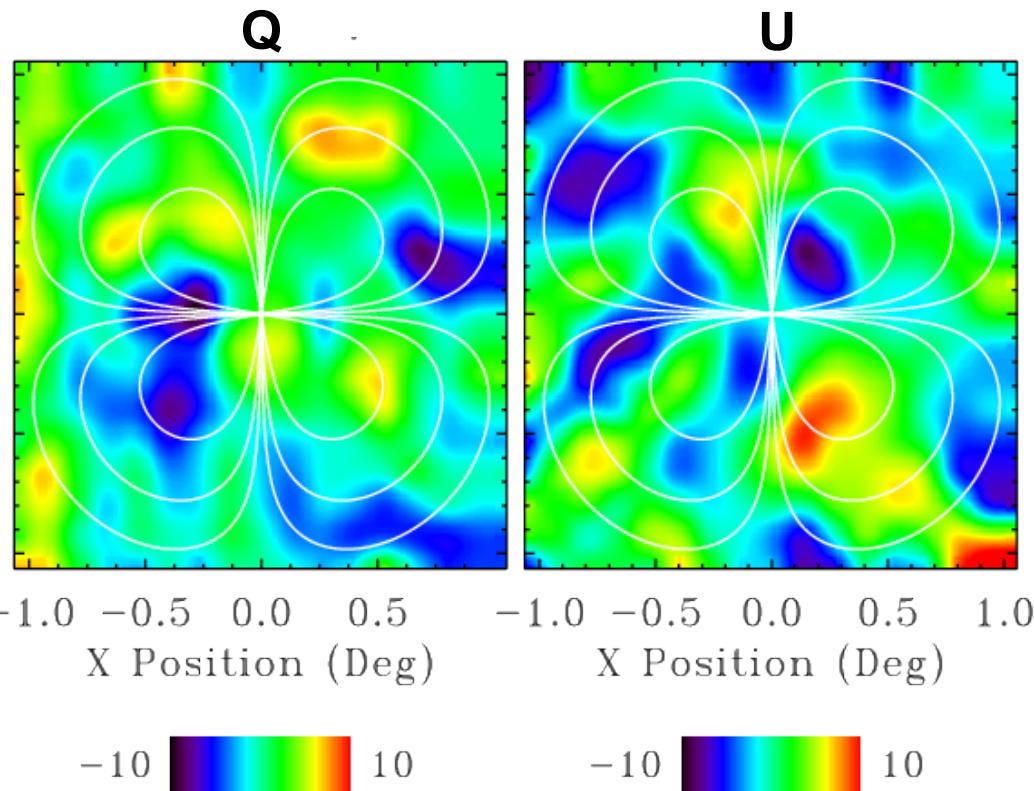


After
VPM
Modulation

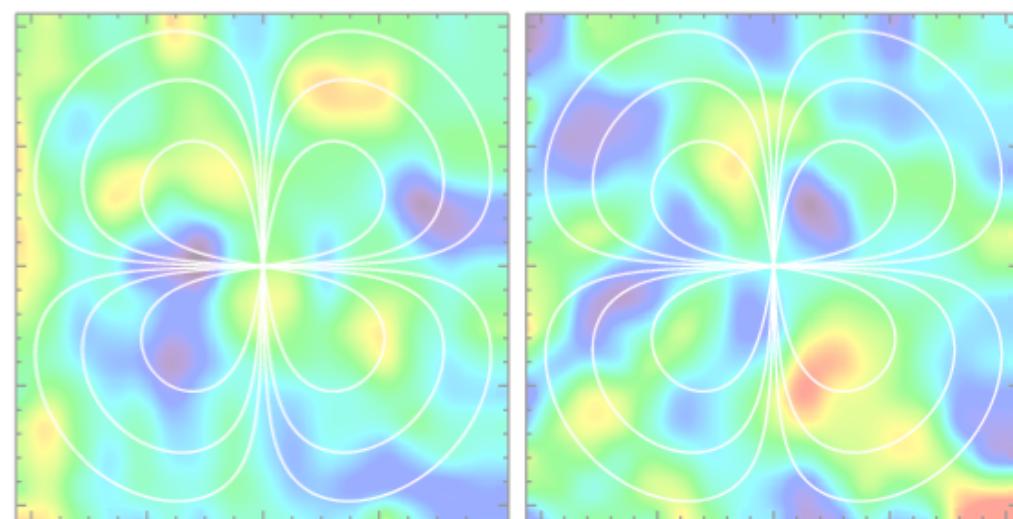
VPM:
Q/U mixing
but
Q/V modulation



Cross-Polar Beam Systematics

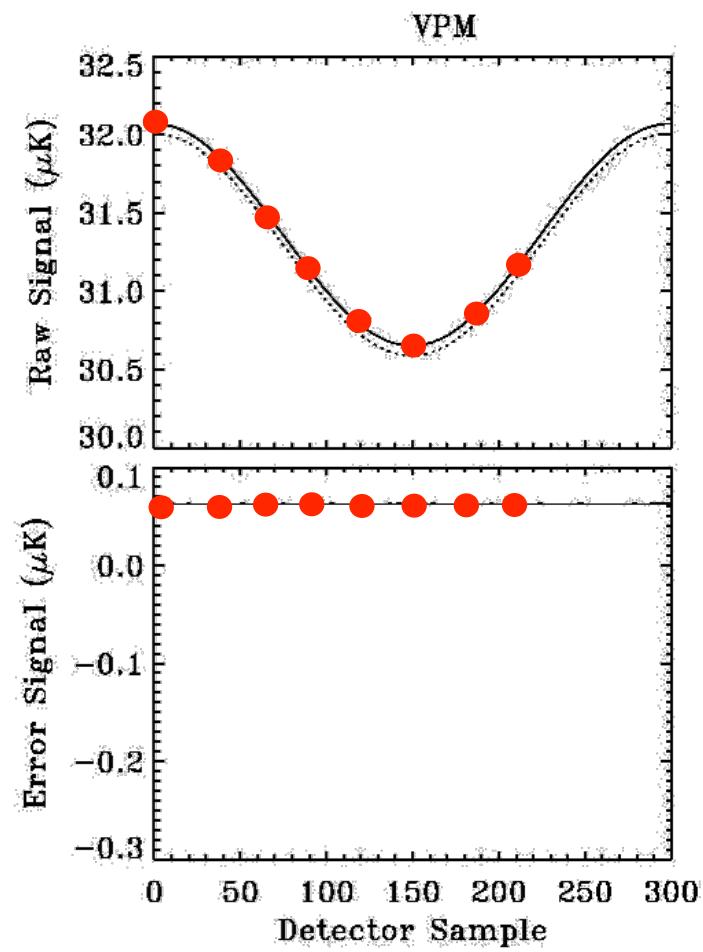


True
Sky

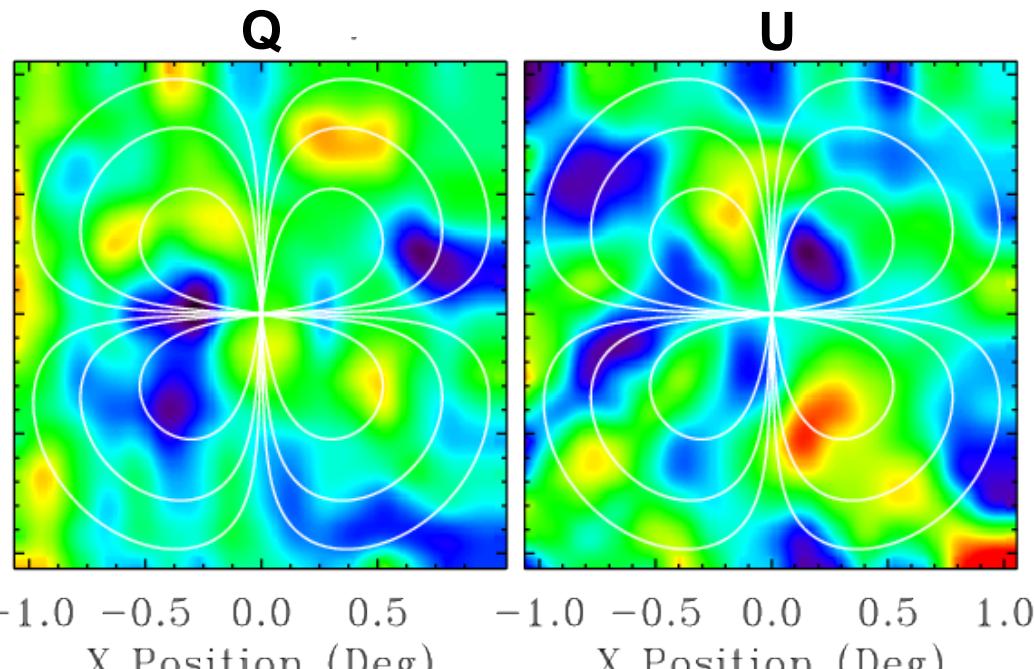


After
VPM
Modulation

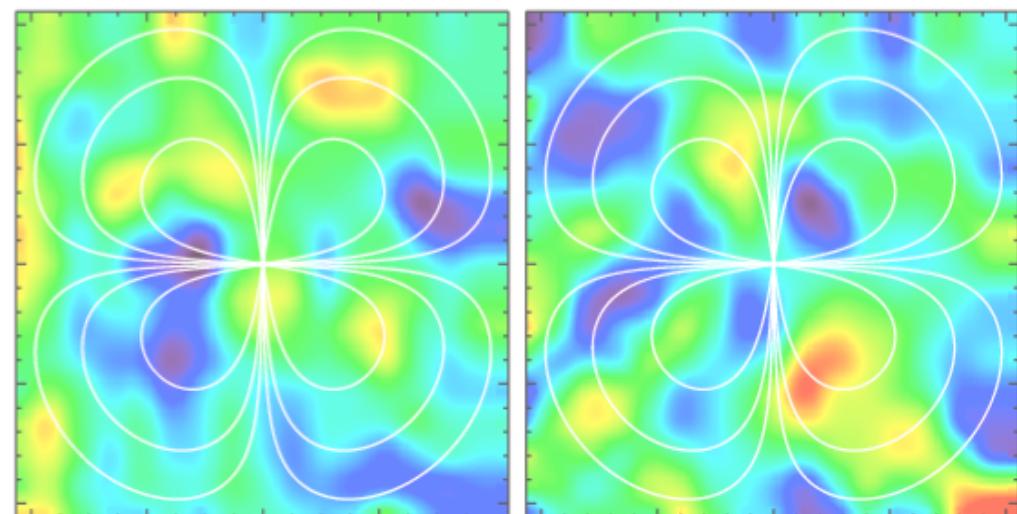
VPM:
Q/U mixing
but
Q/V modulation



Cross-Polar Beam Systematics

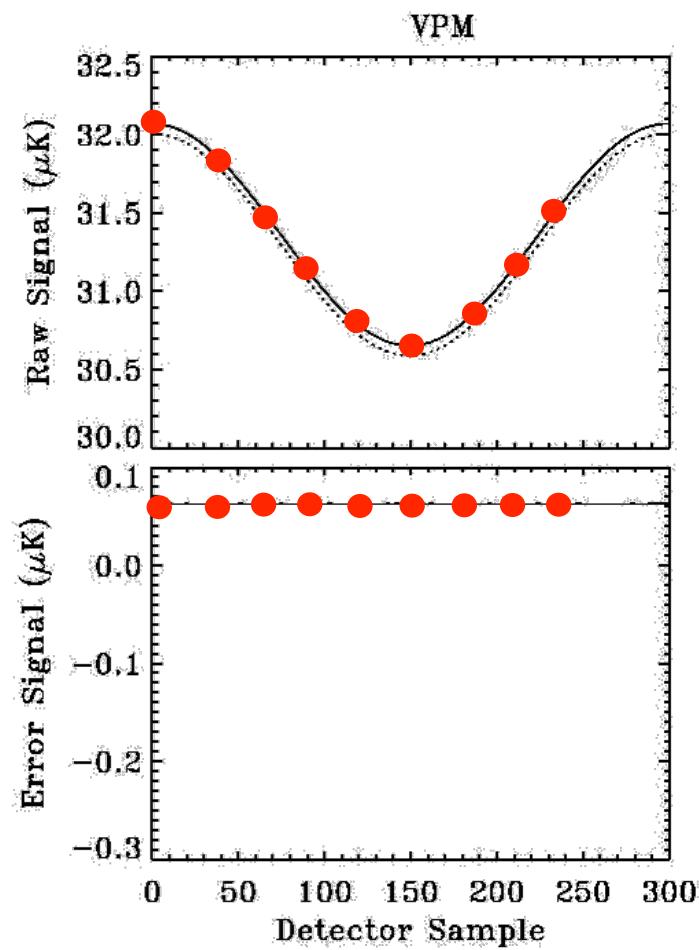


True
Sky

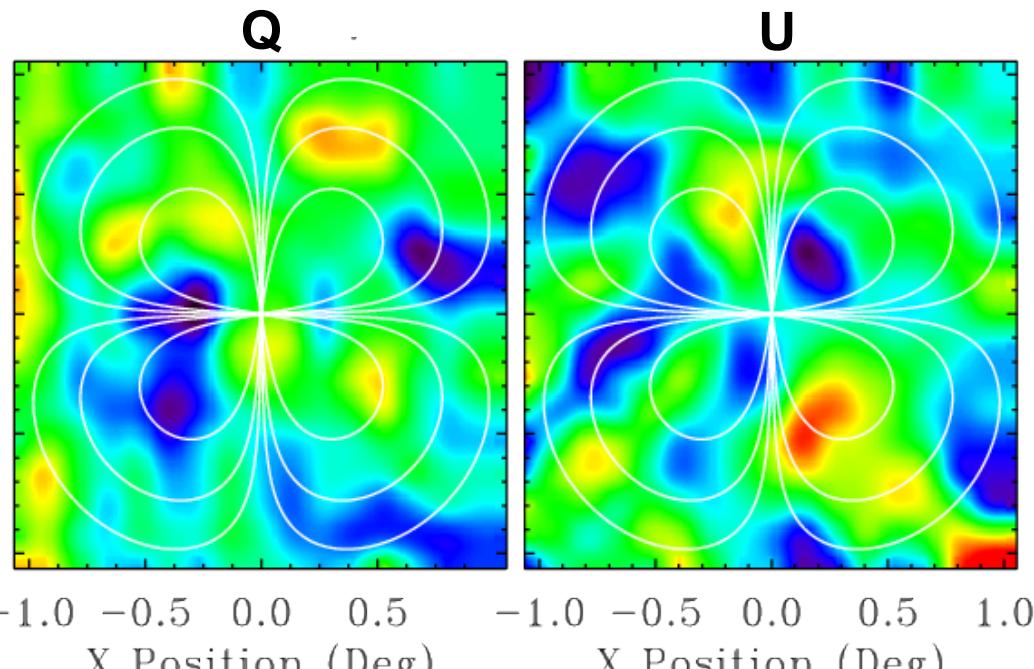


After
VPM
Modulation

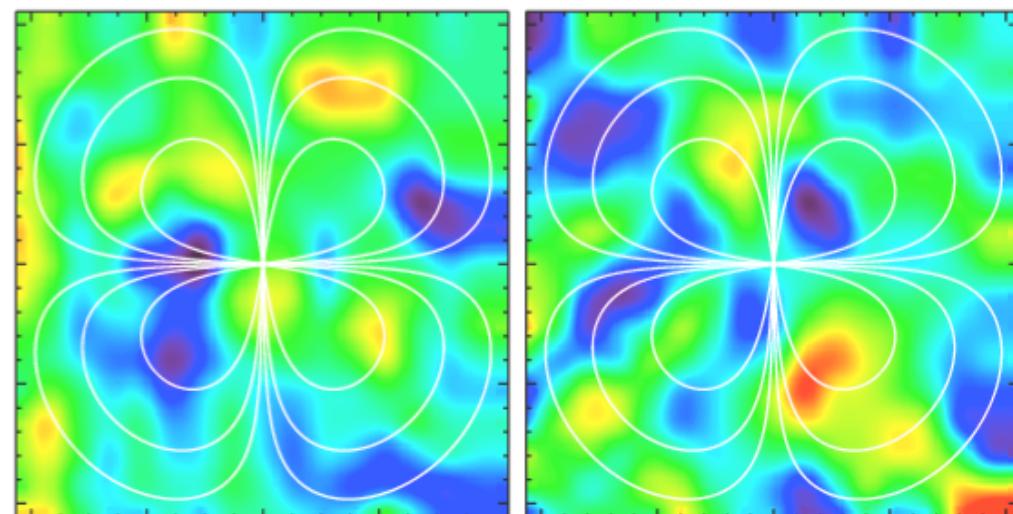
VPM:
 Q/U mixing
but
 Q/V modulation



Cross-Polar Beam Systematics

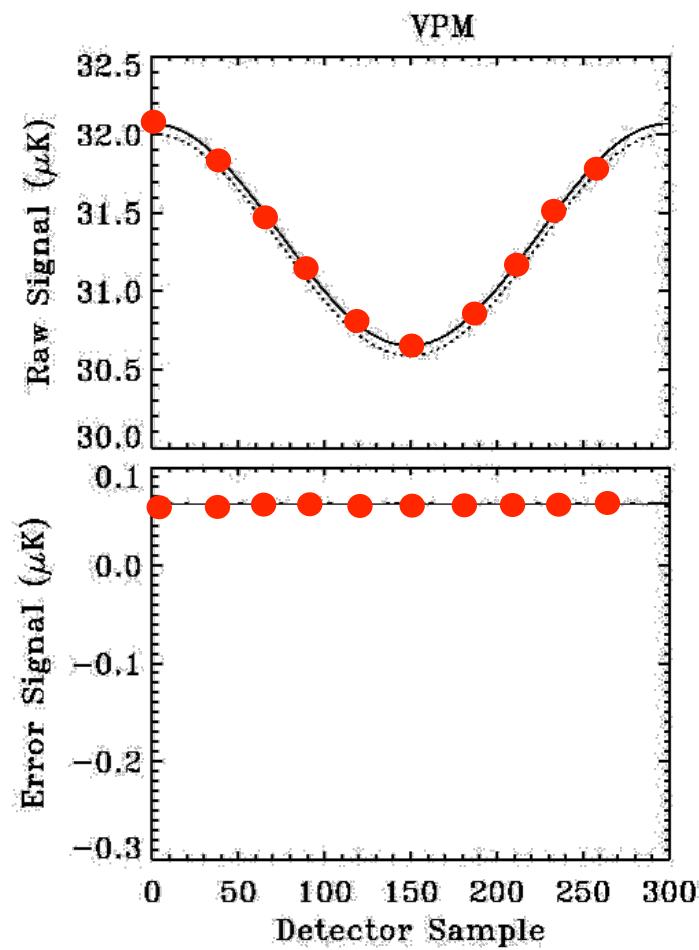


True
Sky

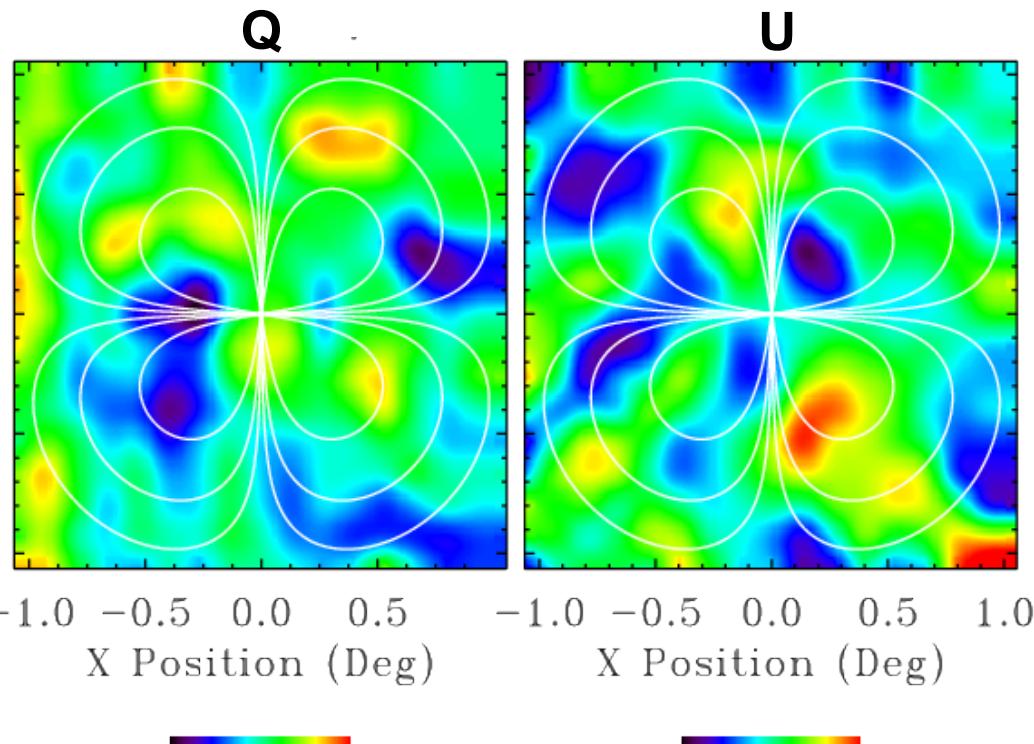


After
VPM
Modulation

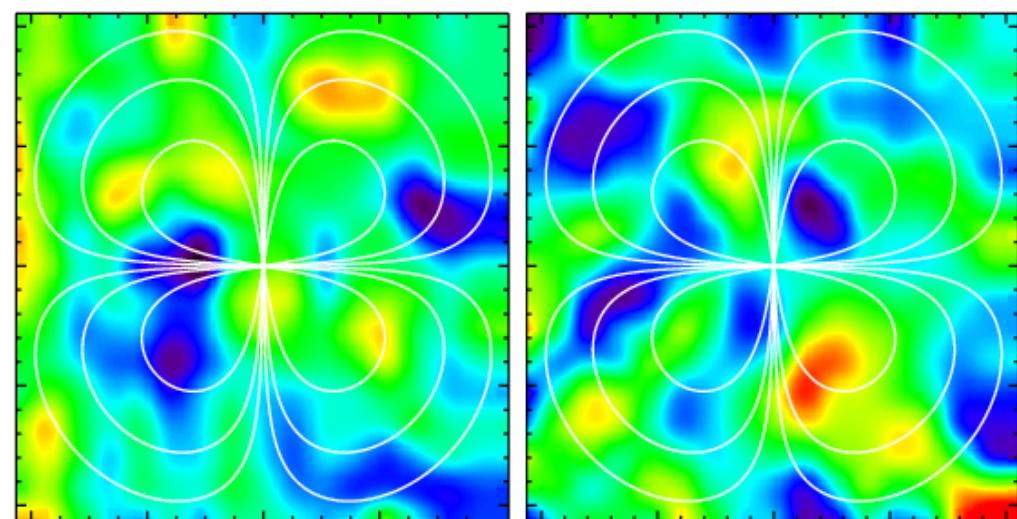
VPM:
 Q/U mixing
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 Q/V modulation



Cross-Polar Beam Systematics

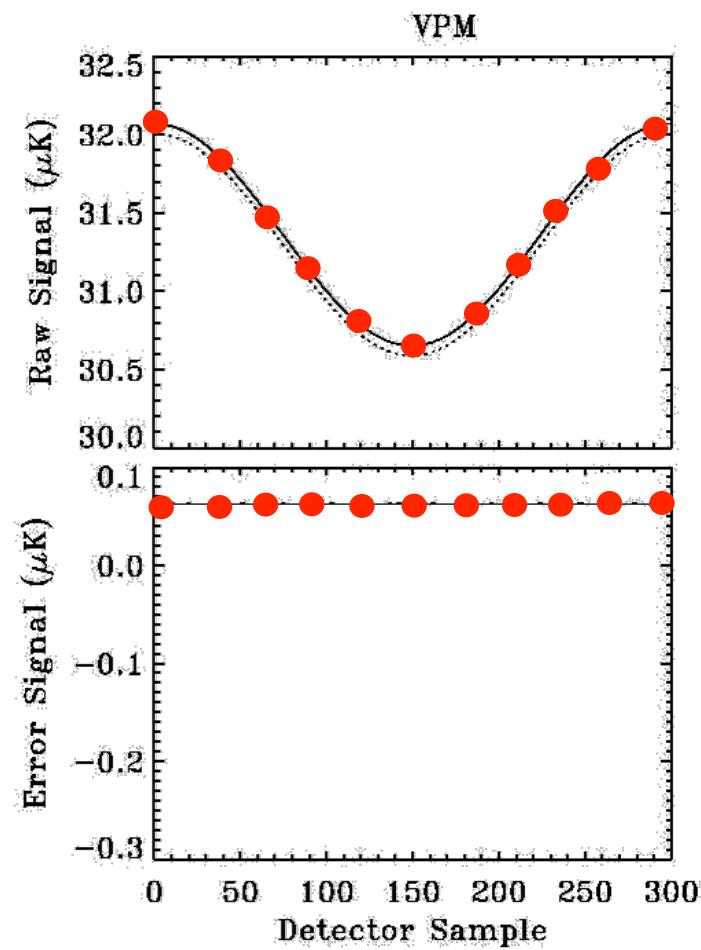


True
Sky



After
VPM
Modulation

VPM:
Q/U mixing
but
Q/V modulation



VPM Advantages



Minimizes a whole range of systematic errors

- $Q \leftrightarrow V$ modulation distinct from $Q \leftrightarrow U$ ($E \leftrightarrow B$) mixing
- Take advantage of $V=0$ for sky

Decouples polarization from scan strategy

- Diagonal pixel covariance matrix
- No degradation at large angular separations/low ℓ

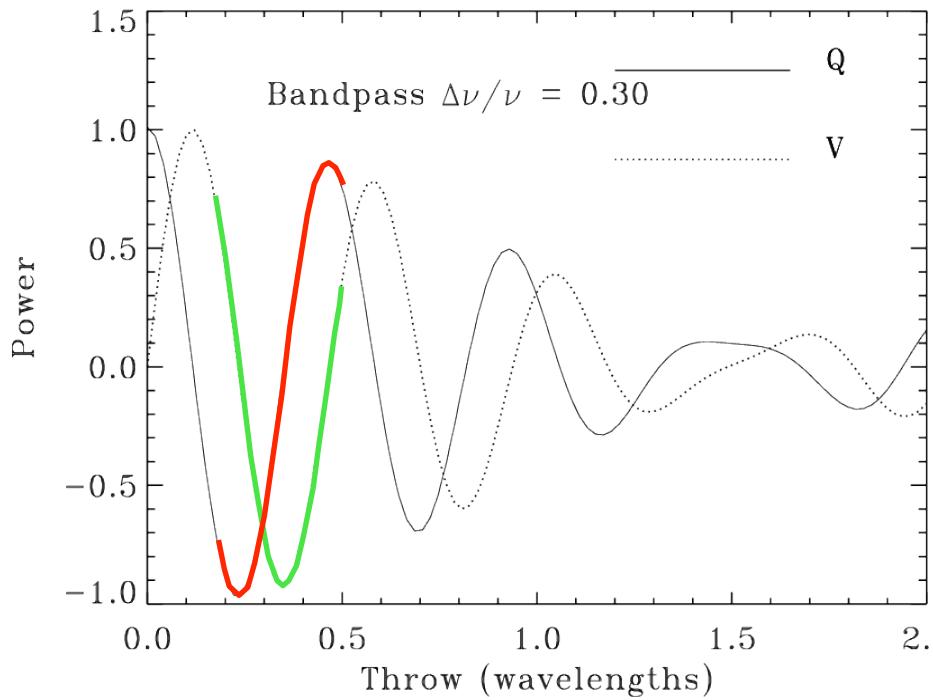
Simple cryogenic implementation

- Small linear translation instead of large angular rotation
- Simple cooling path to grating and mirror
- Vary mirror sweep to vary Q/V sampling
- Non-ideal effects are computable from first principles

Plus: Get full-sky map of Stokes V
Four orders-of-magnitude improvement!

Yow! Fun With Circular Polarization

VPM Stroke vs Efficiency



Full-sky maps in Q, U, and V

- Clean test for systematics
- Limit non-standard physics

Sine sweep from $-Q$ to $+Q$
70% Q
30% V

