

Fast global matching via energy pyramid

7/17/2014

B. Conejo

(bconejo@caltech.edu)

with S. Leprince, F. Ayoub & JP. Avouac (GPS, Caltech)

And P. Monasse & N. Komodakis (LIGM, Paris-Est)



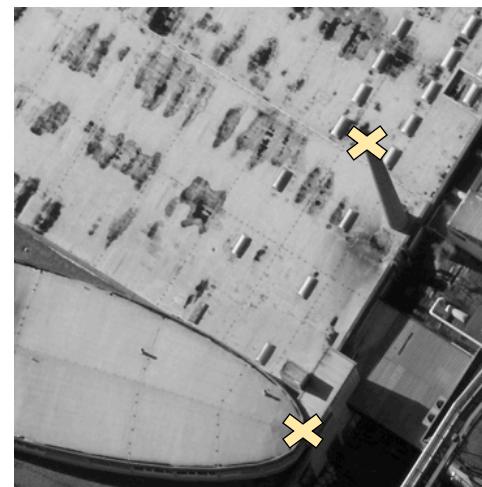
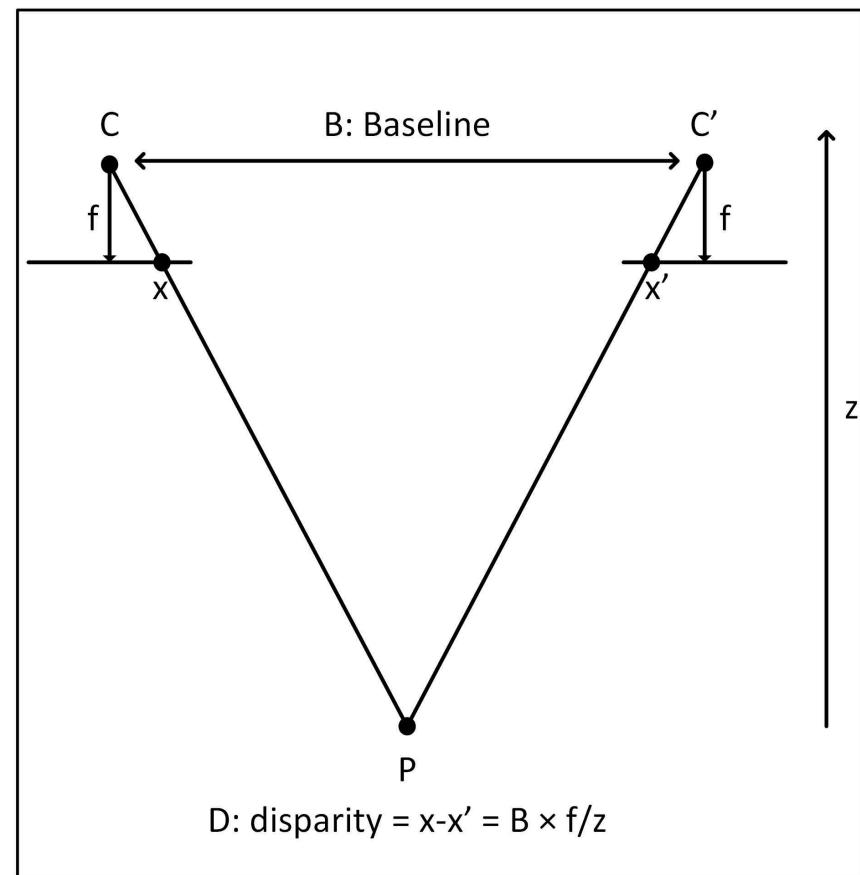
| Caltech
www.caltech.edu

Motivation:

Some matching problems:



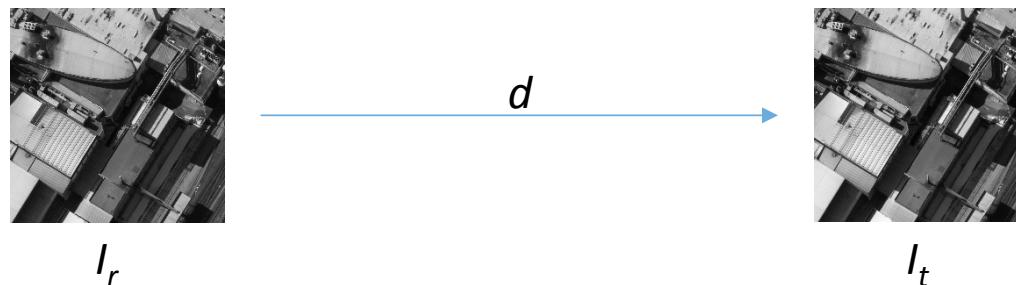
Classic stereo-imaging setup



Disparity is inversely proportional to depth!

Modeling: bayesian approach

Given a stereo-pair of images (I_r, I_t) how to retrieve the most probable disparity map d^* ?



In term of probability, we need to estimate the Maximum A Posteriori (MAP) of:

$$P(d|I_r, I_t) = P_M(d|I_r, I_t)P_R(d|I_r).$$

Diagram illustrating the components of the posterior probability:

- A red horizontal bar under the equation is divided into two segments: a shorter red segment on the left and a longer green segment on the right.
- A green arrow points from the end of the green segment to the text "Regularization: priors on disparity".
- A red arrow points from the end of the red segment to the text "Matching: encourages similarity".

Gibbs measure relates probability density function to energy:

$$P(X = x) = \frac{1}{Z} \exp(-E(x))$$

Diagram illustrating the Gibbs measure formula:

- A blue bracket under the term $\exp(-E(x))$ is labeled "Energy of configuration x ".
- A yellow bracket under the term Z is labeled "Normalizing constant".

Modeling: continuous Conditional Random Field (CRF)

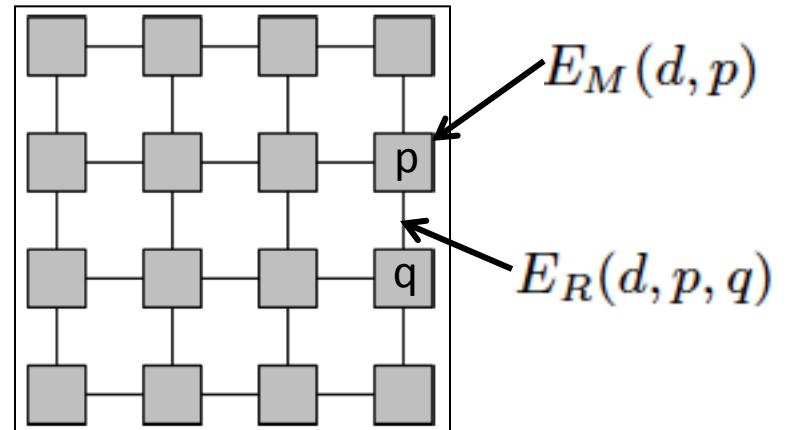
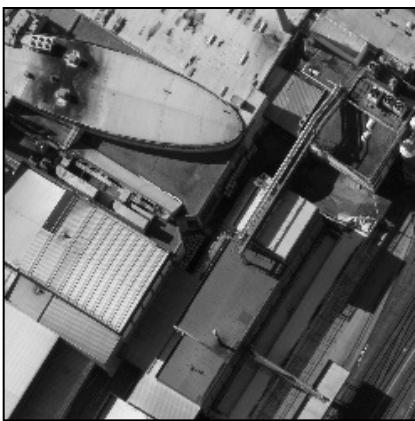


Image and its associated graph $G = (\mathcal{V}, \mathcal{E})$

From the Gibbs measure we relates probabilities to the energies (E_M, E_R, E):

$$E_M(d, p) = \rho(I_r, I_t \circ (id + d(p))). \longrightarrow \text{Similarity criteria (L}_1, \text{L}_2, \text{ZNCC, ...)}$$

$$E_R(d, p, q)) = w(p, q) \|d(p) - d(q)\|_1 \longrightarrow \begin{aligned} &\text{Enforces piecewise constant prior} \\ &\text{Modulates the importance of prior} \end{aligned}$$

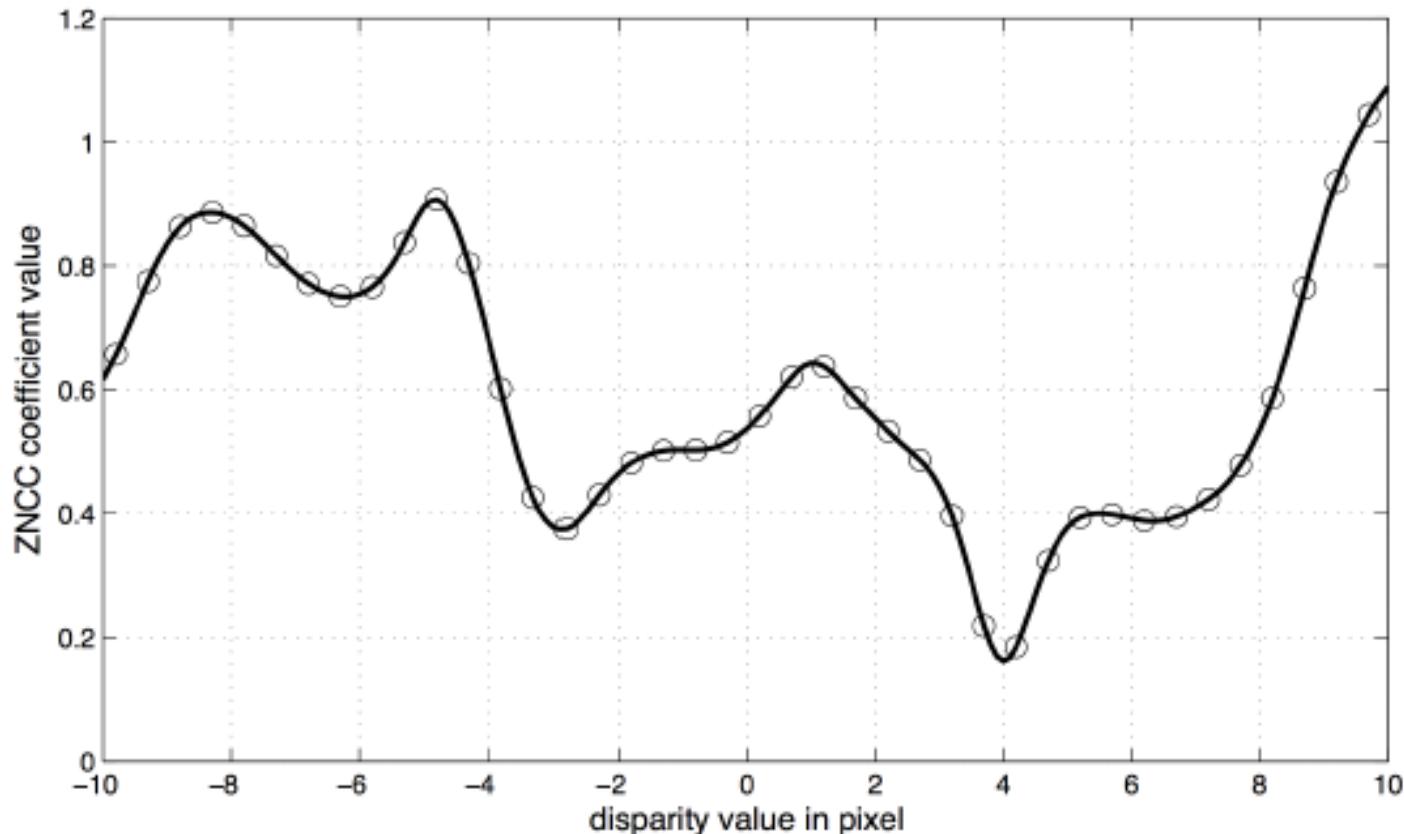
$$E(d) = \sum_{p \in \mathcal{V}} E_M(d, p) + \sum_{pq \in \mathcal{E}} E_R(d, p, q). \longrightarrow \text{First order Conditional Random Field (CRF)}$$

Modeling: non-convexity

We need to globally solve a continuous CRF over all possible disparity maps (D):

$$d^* = \min_{d \in D} E(d).$$

However, this is a non-convex problem: variational approaches will not work!



Non-convexity of a matching terms w.r.t. the disparity

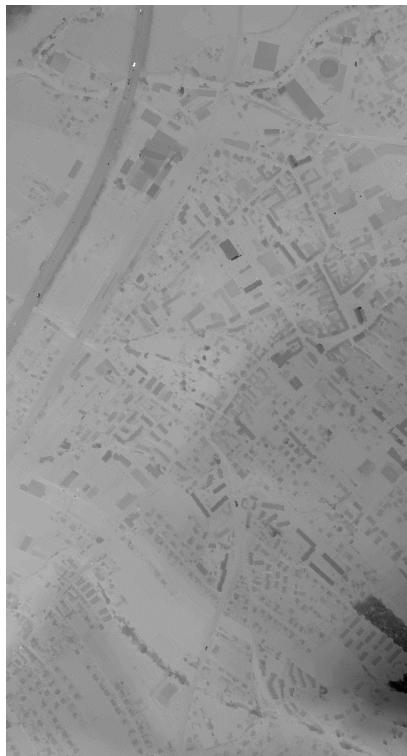
Multi-scale:

Solution: Restrict d to take value in a finite discrete set, i.e., the “search space”.

This leads to globally optimize a first order discrete CRF (still NP-Hard) :

- Message passing (quadratic w.r.t search space): Loopy BP, TRW-S, DD-MRF, ...
- Making move (linear w.r.t search space) : α -exp, β -swap, Fast-PD, ...

We work with large images (30,000 by 30,000) and we have large disparity range (-300,300). A direct approach is inefficient (even impossible) and unnecessary!



Locally the disparity range is “small”.

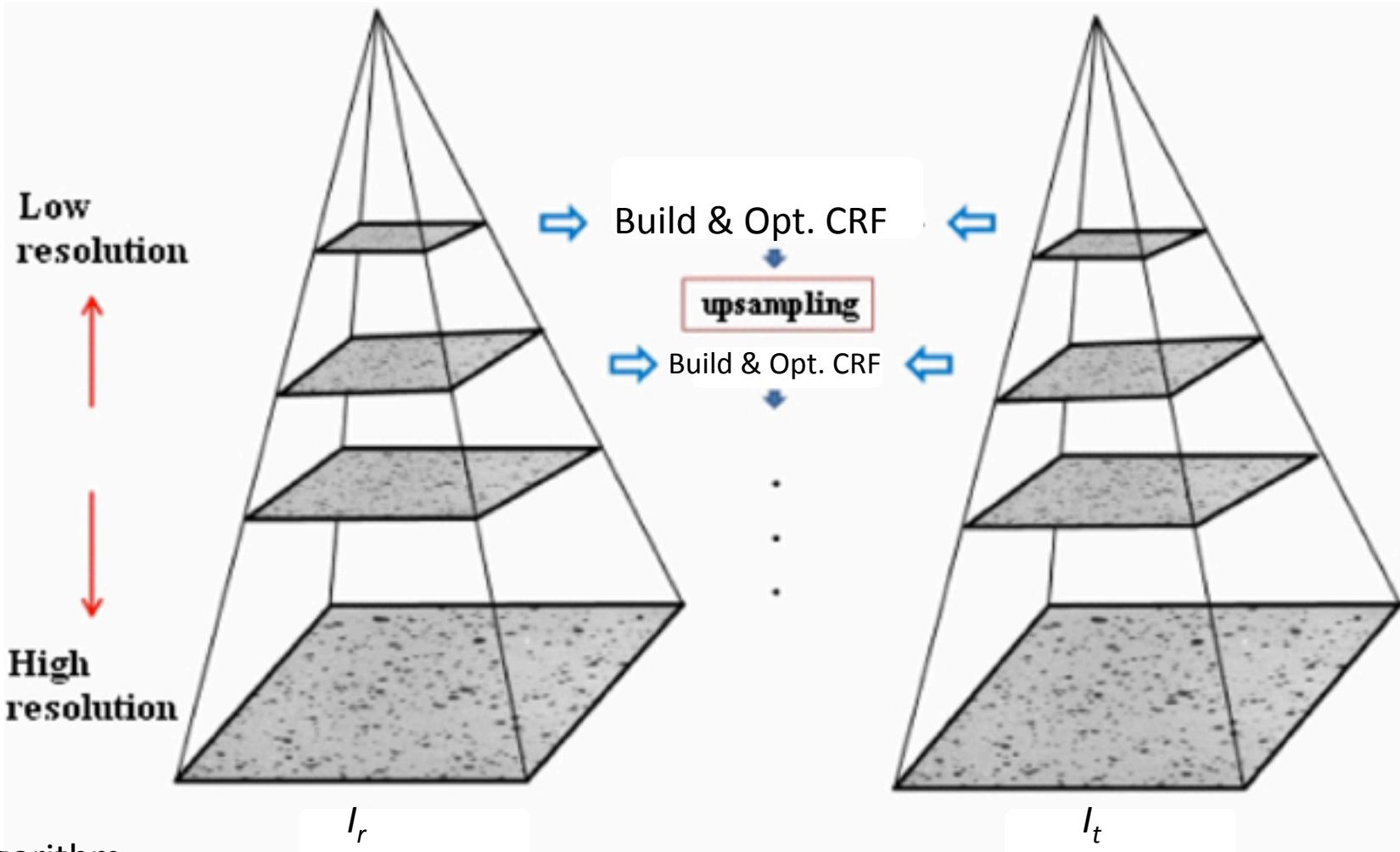
We can use a multi-scale approach:

- Coarsest scales: “large” disparities with low spatial frequencies (natural topography).
- Finest scales: “small” disparities with high spatial frequencies (man made objects).

Two multi-scale schemes exist:

- Image pyramid (classic).
- Energy pyramid (ours).

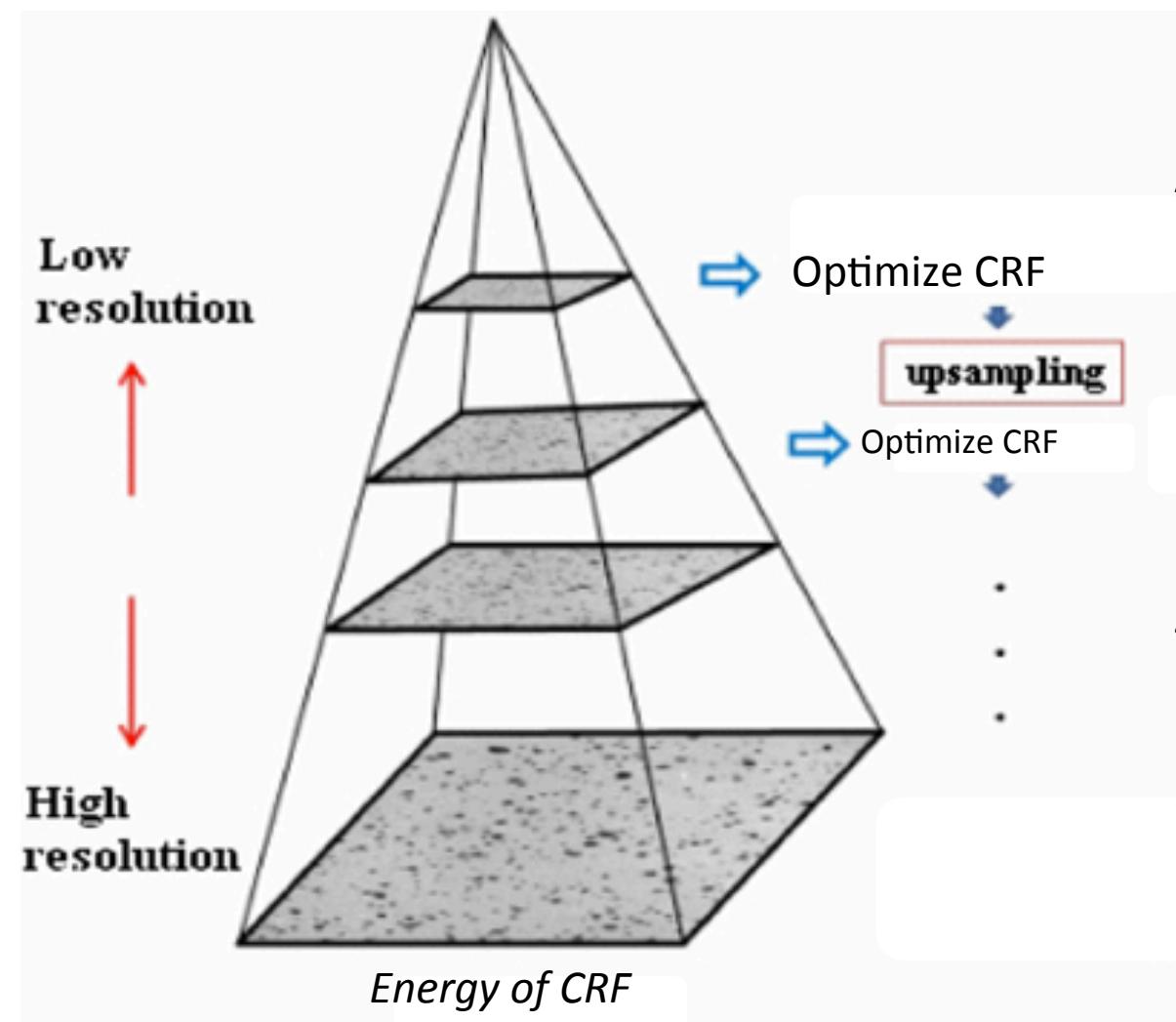
Multi-scale: Image Pyramid



Algorithm

- 1) Build pyramid of image for each image by iterative downsampling
- 2) Compute and optimize CRF at coarsest scale
- 3) Define new search space around current solution
- 4) Repeat (2-3) until finest scale

Multi-scale: Energy Pyramid

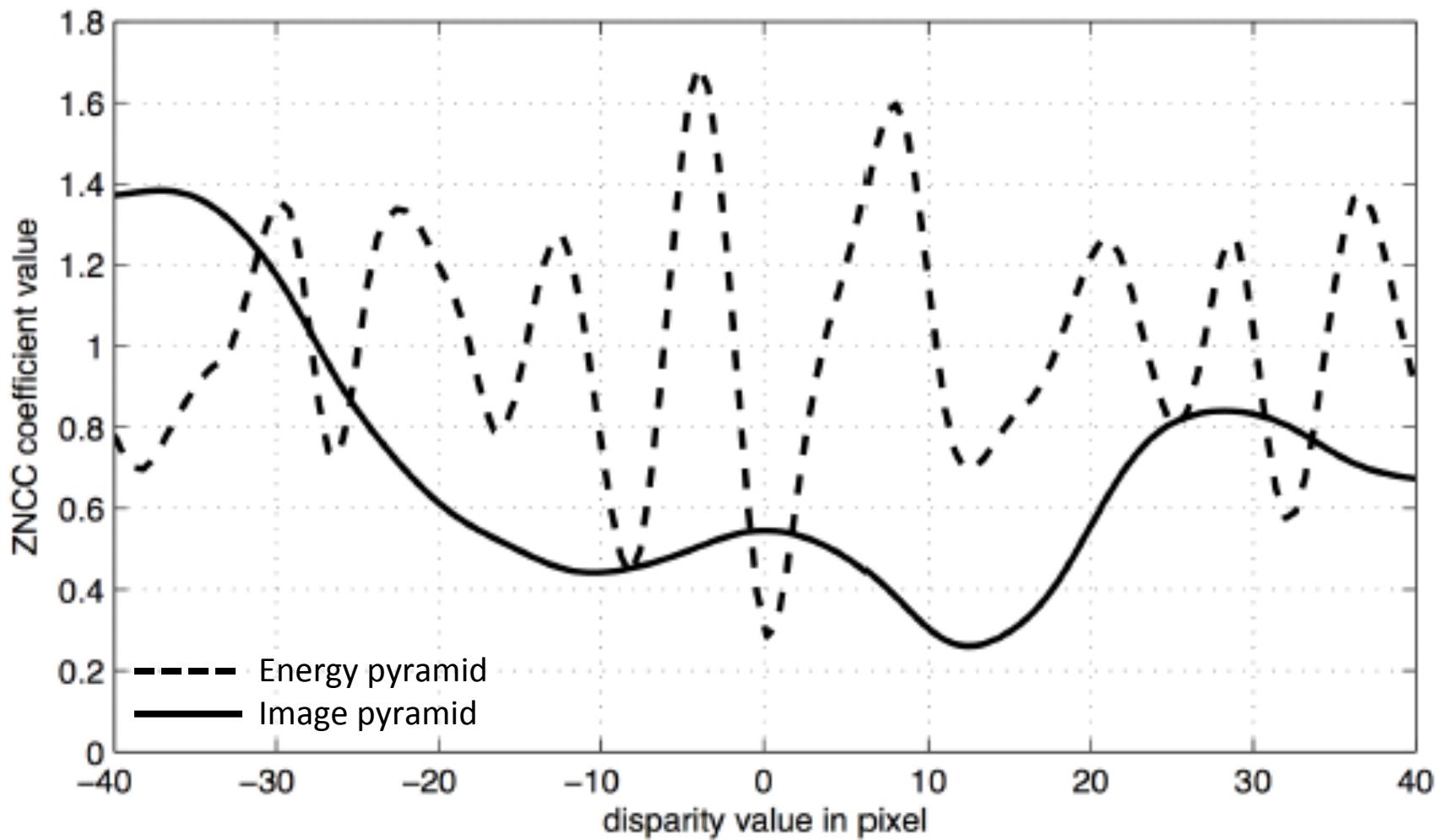


Algorithm:

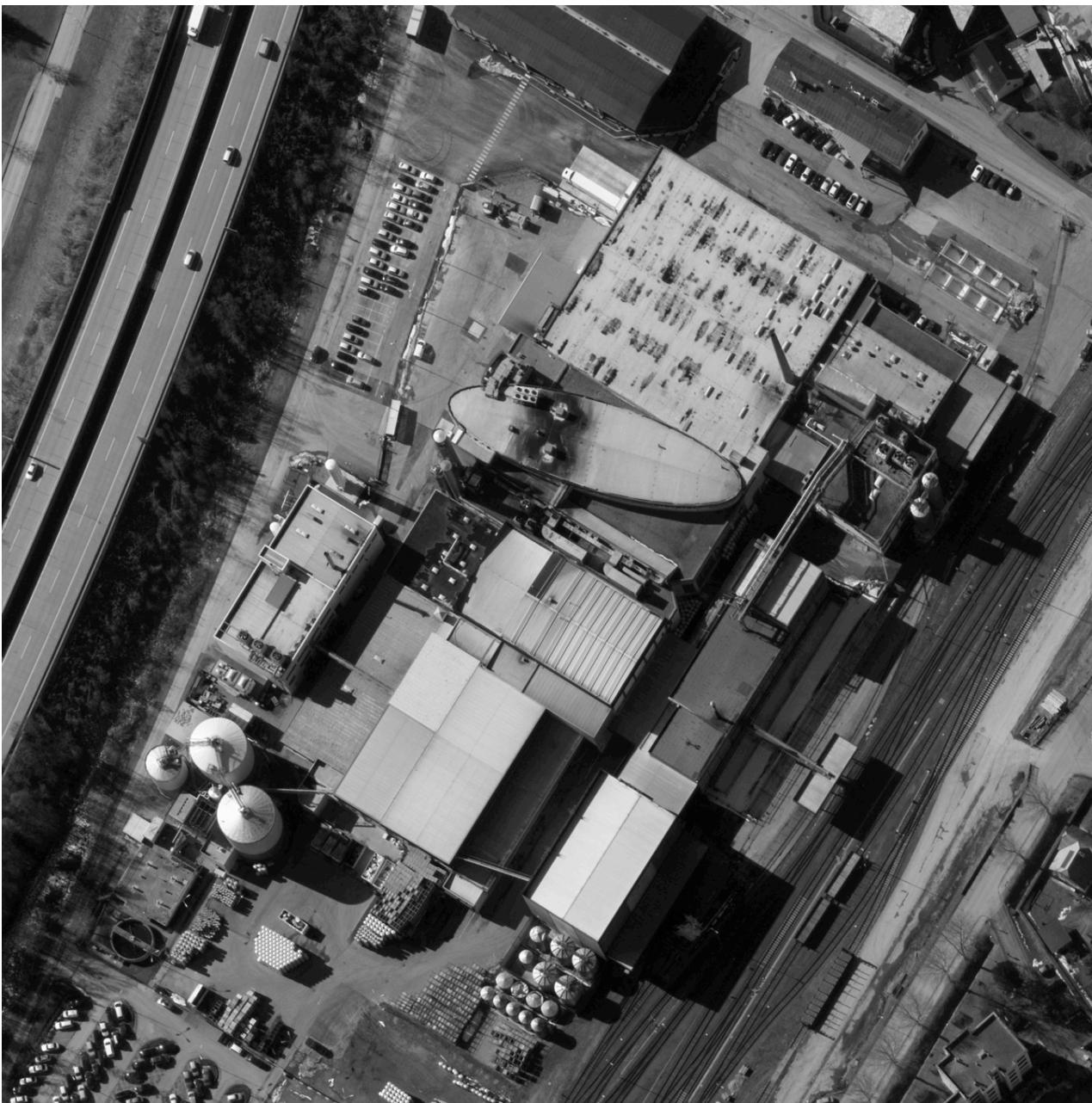
- 1) Compute CRF at finest scale
- 2) Build energy pyramid by iterative downsampling
- 3) Optimize CRF at coarsest scale
- 4) Define new search space around current solution
- 5) Repeat (3-4) until finest scale

Multi-scale: Image pyramid vs Energy pyramid

The image pyramid yields a smoothed representation of the energy and destroys local minimums:



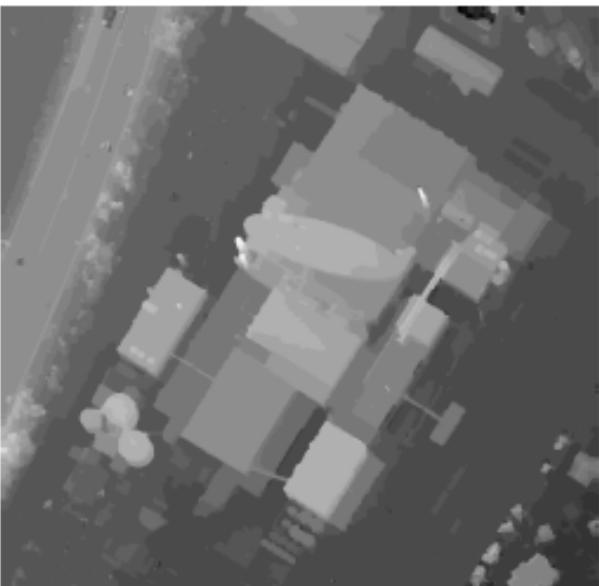
Stereo-imaging in urban context:



B.Conejo - Fast global Matching via Energy Pyramid

Energy Pyramid vs Image Pyramid

Scale 2

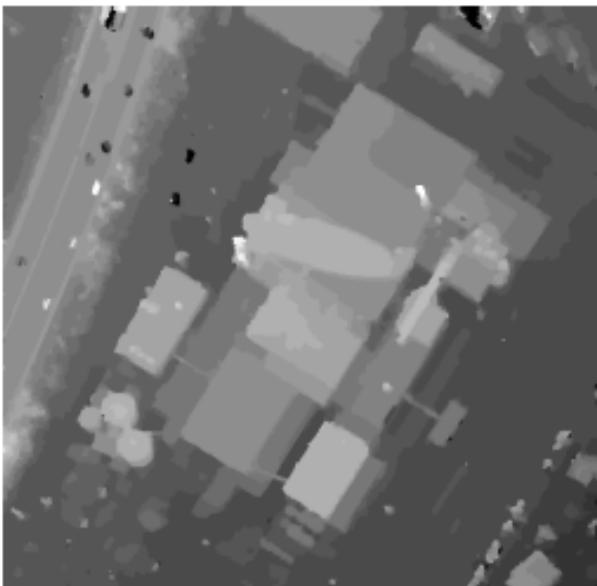


Scale 0



Energy Pyramid

Scale 2



Scale 0

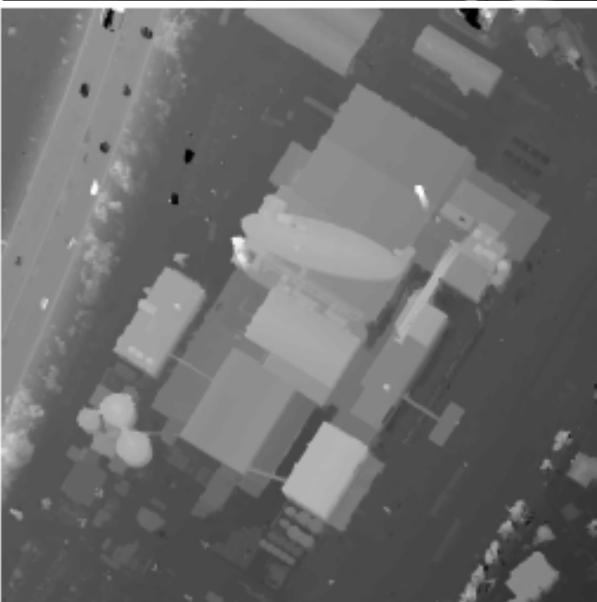
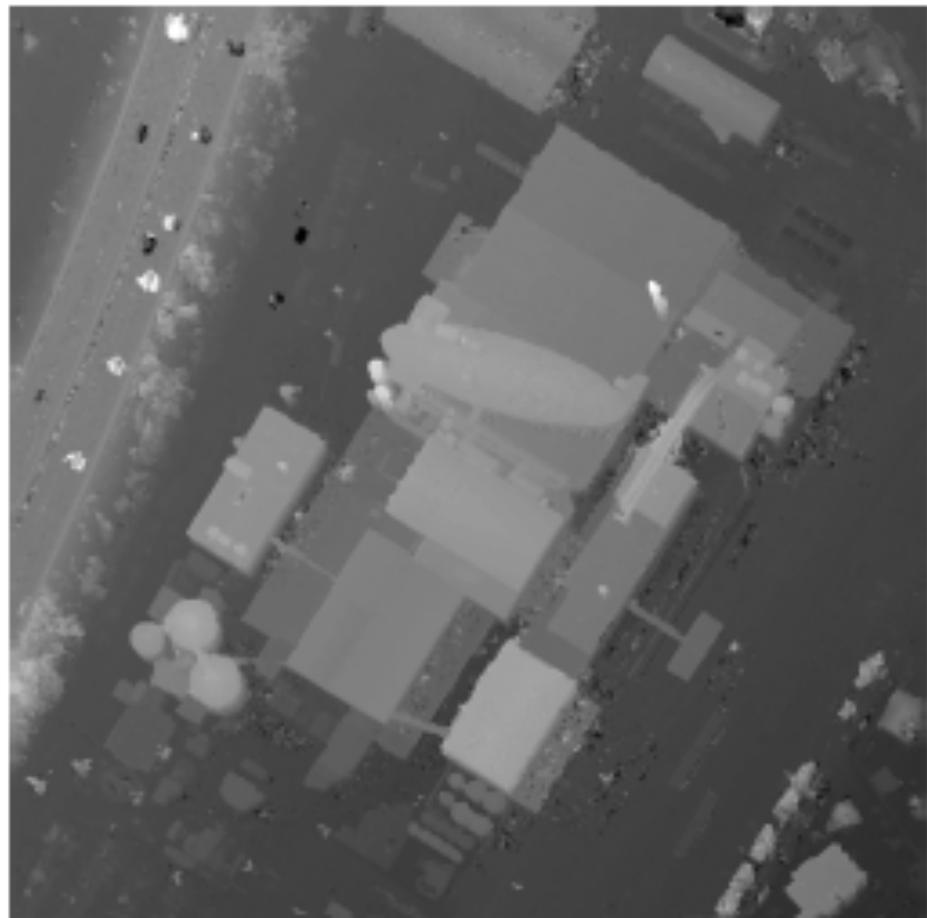
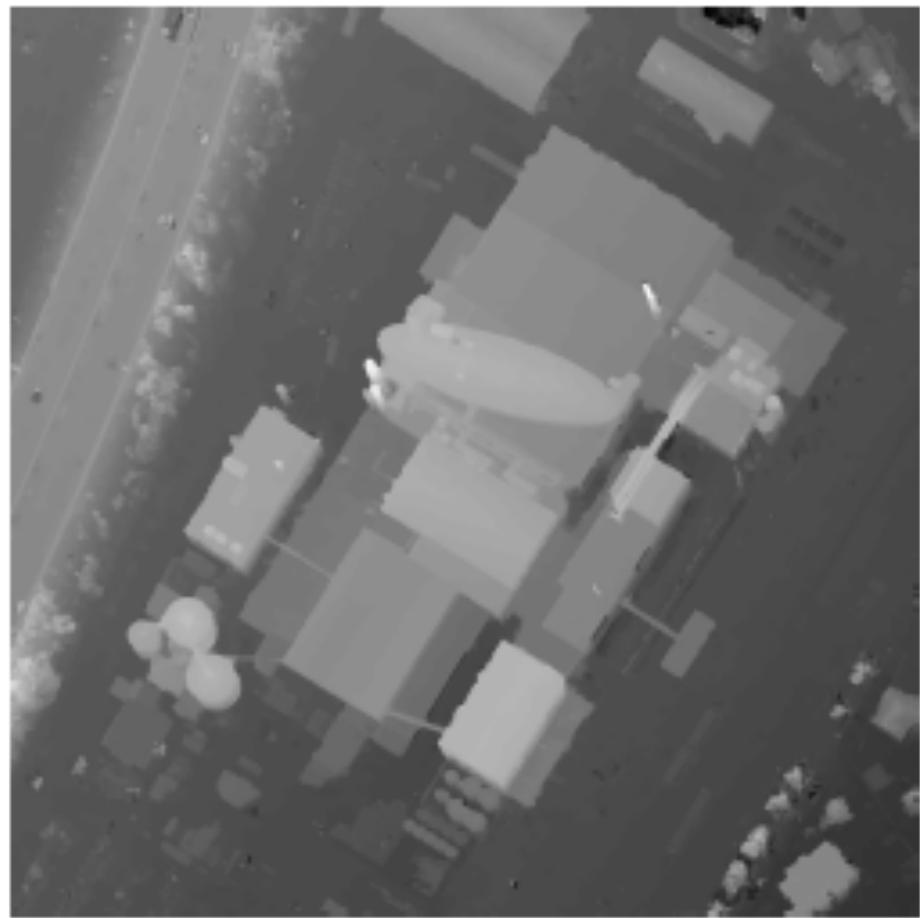


Image Pyramid

Micmac vs Energy Pyramid



Micmac



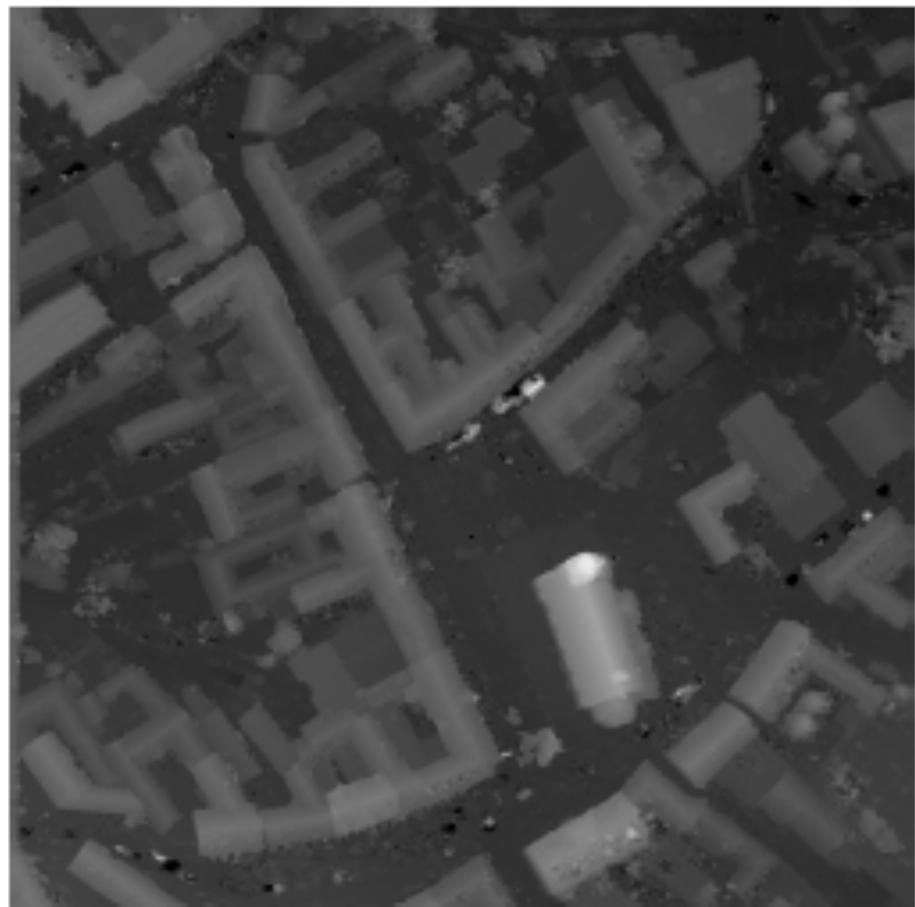
GM-EP
(Energy Pyramid)

Stereo-imaging in urban context:

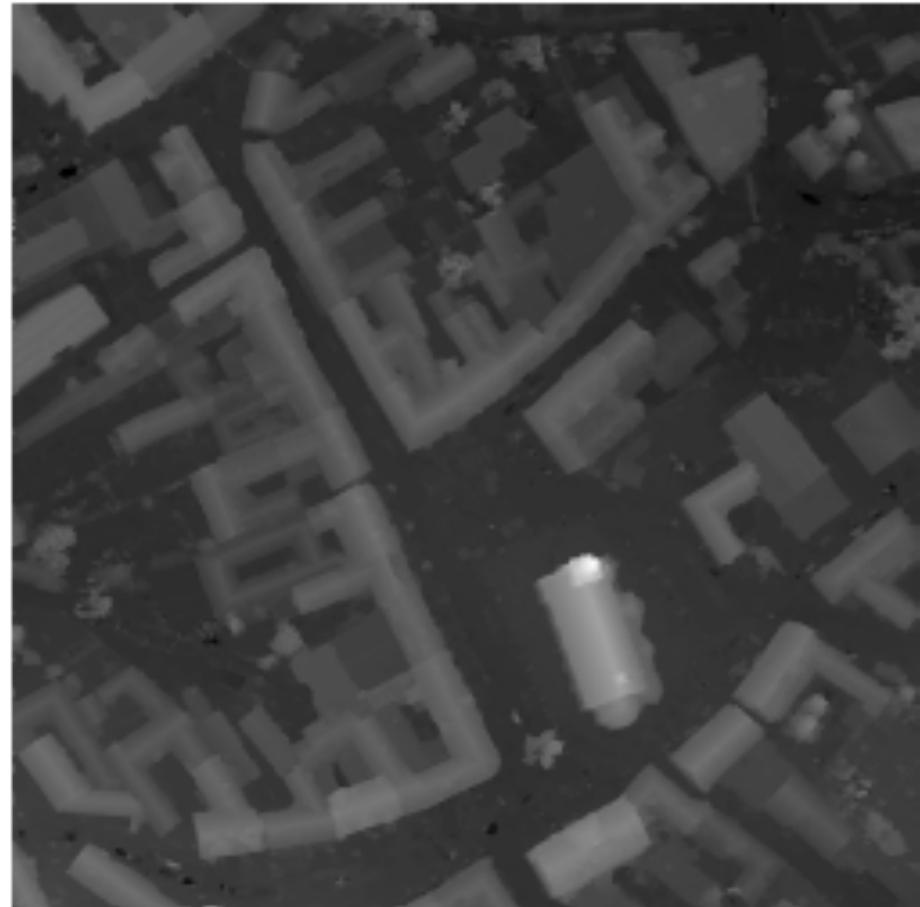


B.Conejo - Fast global Matching via Energy Pyramid

Micmac vs Energy Pyramid



Micmac



GM-EP
(Energy Pyramid)

Conclusion & Future work:

Key points:

- A versatile matching model efficiently optimized with state of the art discrete optimization technique.
- Energy pyramid yields a better representation of the energy.

Future work:

- Modeling:
 - Impact of images' noise,
 - Symmetry w.r.t. the images,
 - Occlusions ,
 - CRF parameters (unary terms, weights of CRF, distance function).
- Optimization
 - Auto definition of the search-space,
 - Multigrid instead of multiscale,
 - Parallelization for shared and distributed memory architectures.

GRACIAS **THANK**
ARIGATO **YOU**
SHUKURIA **BOLZİN MERCI**
JUSPAXAR

DANKSCHEEN
SPASSIBO
NUHUN
SNACHALHUYA
CHALTU
YAQHANYELAY
TASHAKKUR ATU
WABEEJA MAITEKA
YUSPAGARATAM
DHANYABAAD
ANHHA MERSI
HUI
MAAKE
ATTO
SANCO
MERASTAWHY
GAEJTHO
LAH
FAKAUE
KOMAPSUMNIDA
GRAZIE
MEHRBANI
PALDIES
EKFHM
SUKSAM
EKHMET
UNALCHEESH
SPASIBO
DENKAUJA
HENACHALHUYA
HATUR GUI
IKOBU
SIKOMO
MAKETAI
MINMONCHAR

