Universal laws and architectures

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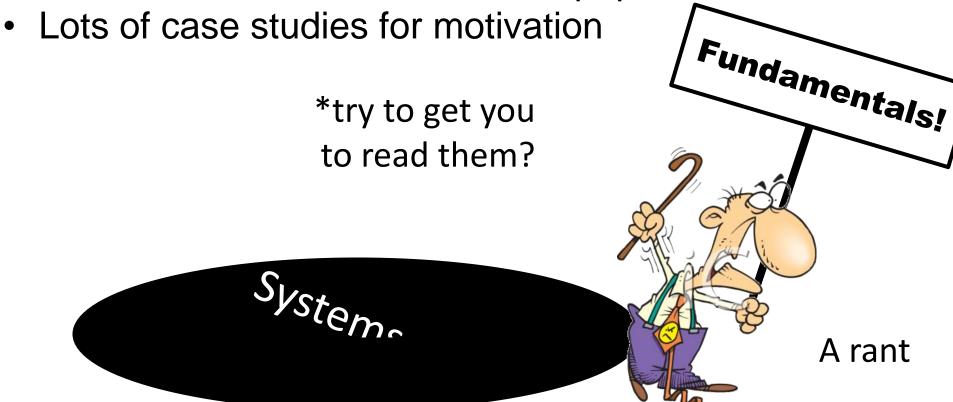
Turing on layering

The 'skin of an onion' analogy is also helpful. In considering the functions of the mind or the brain we find certain operations which we can explain in purely mechanical terms. This we say does not correspond to the real mind: it is a sort of skin which we must strip off if we are to find the real mind. But then in what remains we find a further skin to be stripped off, and so on. Proceeding in this way do we ever come to the 'real' mind, or do we eventually come to the skin which has nothing in it? In the latter case the whole mind is mechanical.

1950, Computing Machinery and Intelligence, Mind

"Universal laws and architectures?"

- Universal "conservation laws" (constraints)
- Universal architectures (constraints that deconstrain)
- Mention recent papers*
- Focus on broader context not in papers



This paper aims to bridge progress in **neuroscience** involving sophisticated quantitative analysis of behavior, including the use of **robust control**, with other relevant conceptual and theoretical frameworks from **systems engineering**, **systems biology**, **and mathematics**.

Architecture, constraints, and behavior

Very accessible

No math

John C. Doyle^{a,1} and Marie Csete^{b,1}

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Edited by Donald W. Pfaff, The Rockefeller University, New York, NY, and approved June 10, 2011 (received for review March 3, 2011)

This paper aims to bridge progress in neuroscience involving sophisticated quantitative analysis of behavior, including the use of robust control, with other relevant conceptual and theoretical frameworks from systems engineering, systems biology, and mathematics. Familiar and accessible case studies are used to illustrate concepts of robustness, organization, and architecture (modularity and protocols) that are central to understanding complex networks. These essential organizational features are hidden during normal function of a system but are fundamental for understanding the nature, design, and function of complex biologic and technologic systems.

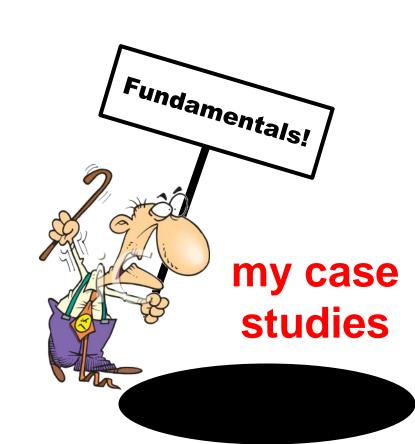
evolved for sensorimotor control and retain much of that evolved architecture, then the apparent distinctions between perceptual, cognitive, and motor processes may be another form of illusion (9), reinforcing the claim that robust control and adaptive feedback (7, 11) rather than more conventional serial signal processing might be more useful in interpreting neurophysiology data (9). This view also seems broadly consistent with the arguments from grounded cognition that modal simulations, bodily states, and situated action underlie not only motor control but cognition in general (12), including language (13). Furthermore, the myriad constraints involved in the evolution of circuit

Doyle, Csete, *Proc Nat Acad Sci USA*, JULY 25 2011

- Lots from cell biology
 - glycolytic oscillations for hard limits
 - bacterial layering for architecture
- Networking and "clean slate" architectures
 - wireless end systems
 - info or content centric application layer
 - integrate routing, control, scheduling, coding, caching
 - control of cyber-physical
 - PC, OS, VLSI, antennas, etc (IT components)
- Neuroscience
 - brains
 - neuroendocrine control
- Medical and exercise physiology

my case studies

- Cell biology
- Networking &"clean slate" architectures
- Neuroscience
- Medical physiology
- Smartgrid, cyber-phys
- Wildfire ecology
- Earthquakes
- Lots of aerospace
- Physics:
 - turbulence,
 - stat mech (QM?)
- "Toy":
 - Lego,
 - clothing,
 - buildings, ...
- Synesthesia

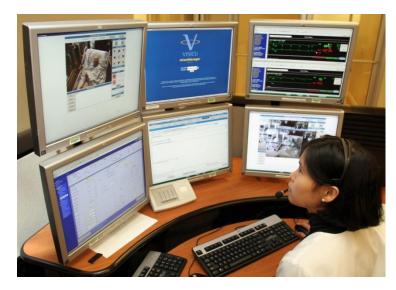


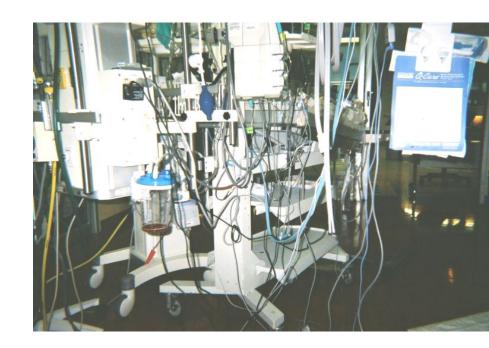


Existing design frameworks

- Sophisticated components
- Poor integration
- Limited theoretical framework

Fix?





Happy families are all alike; every unhappy family is unhappy in its own way.

Leo Tolstoy, Anna Karenina, Chapter 1, first line

- What could this mean? Given incredible diversity of people and environments?
- It has to be a statement about organization, and specifically architecture.
- Happy = empathy + cooperation + simple rules?
- · Constraints on components and architecture

accessible accountable accurate adaptable administrable affordable auditable autonomy available credible process capable compatible composable configurable correctness customizable debugable degradable determinable demonstrable dependable deployable discoverable distributable durable effective efficient evolvable extensible failure transparent fault-tolerant fidelity flexible inspectable installable Integrity interchangeable interoperable learnable maintainable

manageable mobile modifiable modular nomadic operable orthogonality portable precision predictable producible provable recoverable relevant reliable repeatable reproducible resilient responsive reusable robust

safety scalable seamless self-sustainable serviceable supportable securable simplicity stable standards compliant survivable sustainable tailorable testable timely traceáble ubiquitous understandable upgradable usable

Simplified, minimal requirements

accessible accountable accurate adaptable administrable affordable auditable autonomy available credible process capable compatible composable configurable correctness customizable debugable degradable determinable demonstrable

dependable deployable discoverable distributable durable effective efficient evolvable extensible failure transparent fault-tolerant fidelity flexible inspectable installable Integrity interchangeable interoperable learnable maintainable

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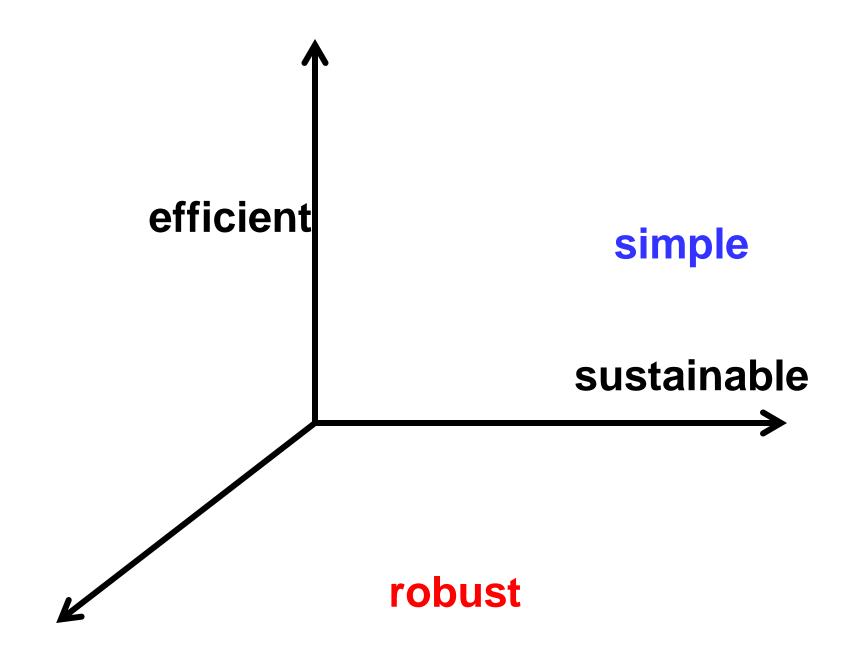
efficient

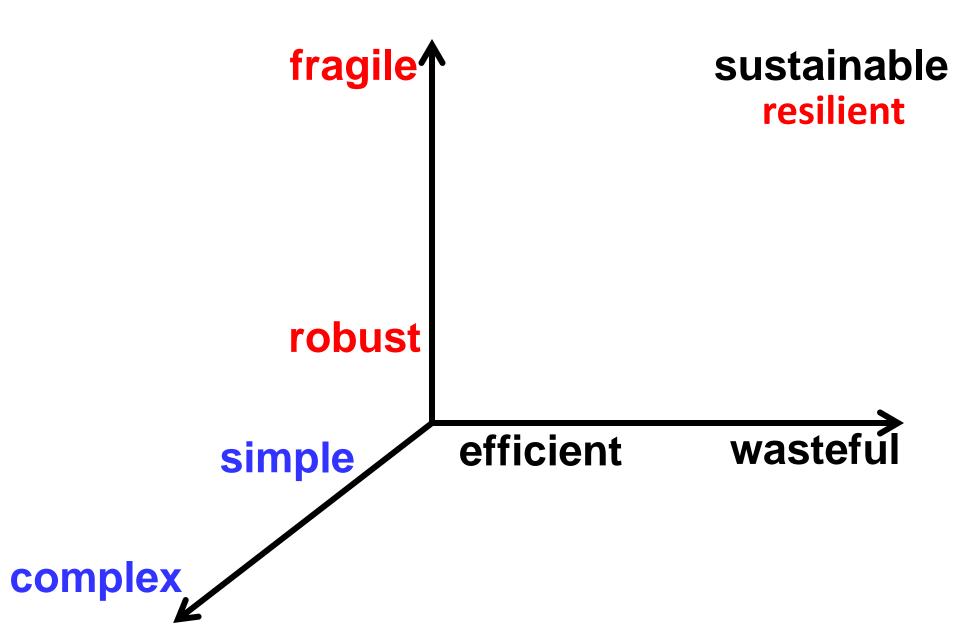
simple

sustainable

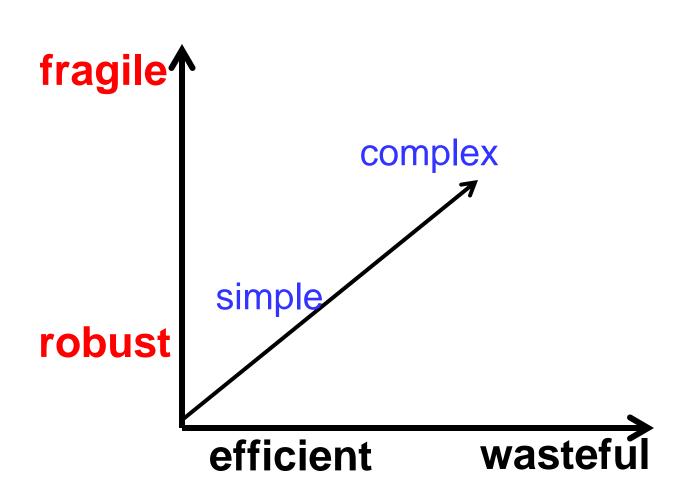
resilient

robust

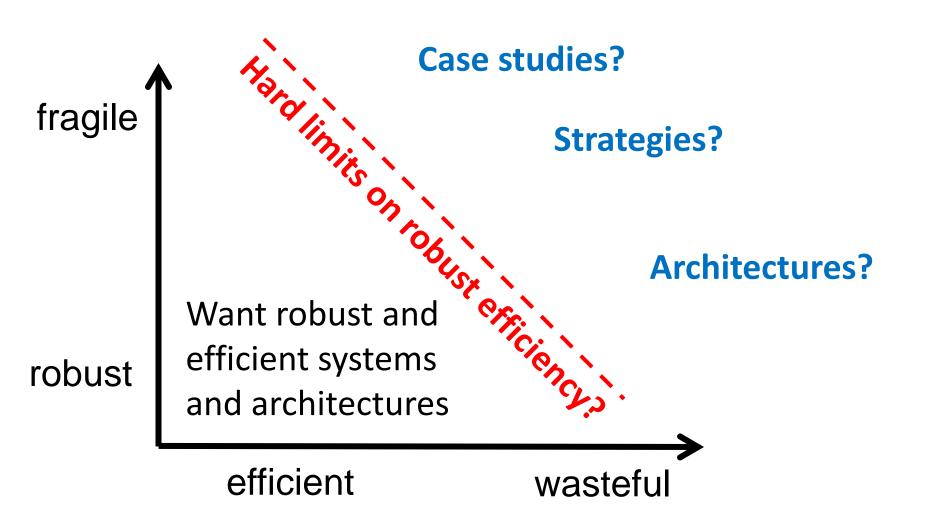




sustainable



Want to understand the space of systems/architectures



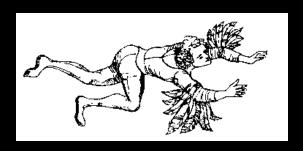
Resilient architectures are all alike; every brittle system is brittle in its own way.

Apologies to Tolstoy

- Resilience includes robustness, efficiency, sustainability, scalability, etc etc
- Effective architectures provide flexible tradeoffs across all these dimensions
- Subject to "laws" which are hard constraints on what is achievable
- Defer resolving terminology, focus on...
- Theorems and concrete case studies

Resilient architectures are all alike; every brittle system is brittle in its own way.

Good architecture =
"constrains that deconstrain"
(Gerhart and Kirschner)



The dangers of naïve biomemetics



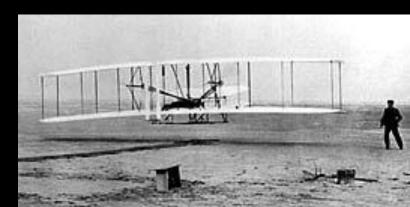


Feathers and flapping?



Or lift, drag, propulsion, and *control*?





Getting it (W)right, 1901

- "We know how to construct airplanes..." (lift and drag)
- "... also know how to build engines." (propulsion)
- "When... balance and steer[ing]... has been worked out, the age of flying will have arrived, for all other difficulties are of minor importance." (control)

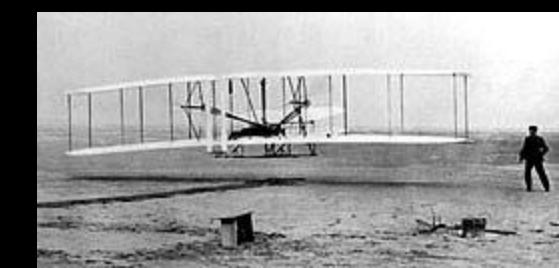


Universals?



Lift, drag, propulsion, and *control*?





Universals?

- Complexity ← control, robust/fragile tradeoffs
- Fragility ← Hijacking, side effects, unintended...
- Of mechanisms evolved for robustness
- Math: robust/fragile constraints ("conservation laws")

Both Accident or necessity?



Fire in the Earth System

I'm interested in fire...

David M. J. S. Bowman, 1* Jennifer K. Balch, 2,3,4* Paulo Artaxo, William J. Bond,6 Jean M. Carlson, Mark A. Cochrane, Carla M. D'Antonio, Ruth S. DeFries, 10 John C. Doyle, 11 Sandy P. Harrison, 12 Fay H. Johnston, 13 Jon E. Keeley, 14,15 Meg A. Krawchuk, 16 Christian A. Kull, 17 J. Brad Marston, 18 Max A. Moritz, 16 I. Colin Prentice, 19 Christopher I. Roos, 20 Andrew C. Scott,²¹ Thomas W. Swetnam,²² Guido R. van der Werf,²³ Stephen J. Pyne²⁴

Fire is a worldwide phenomenon that appears in the geological record soon after the appearance of terrestrial plants. Fire influences global ecosystem patterns and processes, including vegetation distribution and structure, the carbon cycle, and climate. Although humans and fire have always coexisted, our capacity to manage fire remains imperfect and may become more difficult in the future as climate change alters fire regimes. This risk is difficult to assess, however, because fires are still poorly represented in global models. Here, we discuss some of the most important issues involved in developing a better understanding of the role of fire in the Earth system.

Very accessible No math



Wildfires, complexity, and highly optimized tolerance

Max A. Moritz*, Marco E. Morais[†], Lora A. Summerell[‡], J. M. Carlson^{§¶}, and John Doyle[∥]

*Department of Environmental Science, Policy, and Management, University of California, Berkeley, CA 94720; Departments of †Geography and §Physics, University of California, Santa Barbara, CA 93106; †Department of Earth Sciences, California Polytechnic State University, San Luis Obispo, CA 93407; and Department of Control and Dynamical Systems, California Institute of Technology, Pasadena, CA 91125

Communicated by James S. Langer, University of California, Santa Barbara, CA, October 19, 2005 (received for review July 26, 2004)

Recent, large fires in the western United States have rekindled debates about fire management and the role of natural fire regimes in the resilience of terrestrial ecosystems. This real-world experience parallels debates involving abstract models of forest fires, a central metaphor in complex systems theory. Both real and modeled fire-prone landscapes exhibit roughly power law statistics in fire size versus frequency. Here, we examine historical fire catalogs and a detailed fire simulation model; both are in agreement with a highly optimized tolerance model. Highly optimized tolerance suggests robustness tradeoffs underlie resilience in different fire-prone ecosystems. Understanding these mechanisms may provide new insights into the structure of ecological systems and be key in evaluating fire management strategies and sensitivities to climate change.

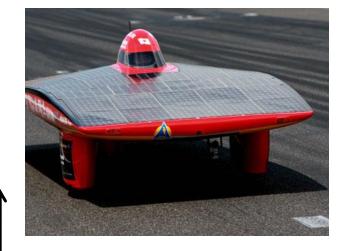
Highly optimized tolerance (HOT) is a conceptual framework for examining organization and structure in complex system (18). Theoretically, HOT builds on models and mathemati from physics and engineering, and identifies robustness tradeoff as a principle underlying mechanism for complexity and power law statistics. HOT has been discussed in the context of a variety of technological and natural systems, including wildfires (18, 22). A quantitative prediction for the distribution of fire sizes have come from an extremely simple analytical HOT model, referred to as the PLR (probability-loss-resource) model (22). As precursor to results presented later in this article, Fig. 2 demonstrates the PLR prediction and truncated power law statistical (23) for several fire history catalogs. This plot represents the radata as rank or cumulative frequency of fires *P(I)* greater that

Accessible ecology
UG math

17912–17917 PNAS December **13, 2005** vol. 102 no. 50

Wildfire ecosystem as ideal example

- Cycles on years to decades timescale
- Regime shifts: grass vs shrub vs tree
- Fire= keystone "specie"
 - Metabolism: consumes vegetation
 - Doesn't (co-)evolve
 - Simplifies co-evolution spirals and metabolisms
- 4 ecosystems globally with convergent evo
 - So Cal, Australia, S Africa, E Mediterranean
 - Similar vegetation mix
 - Invasive species



Current Technology?

fragile

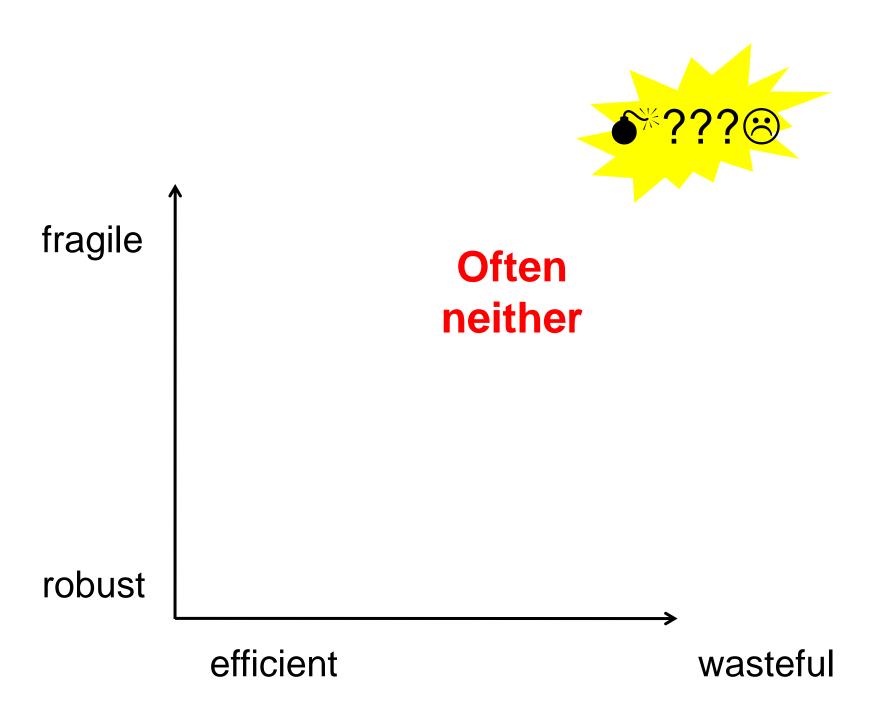
At best we get one

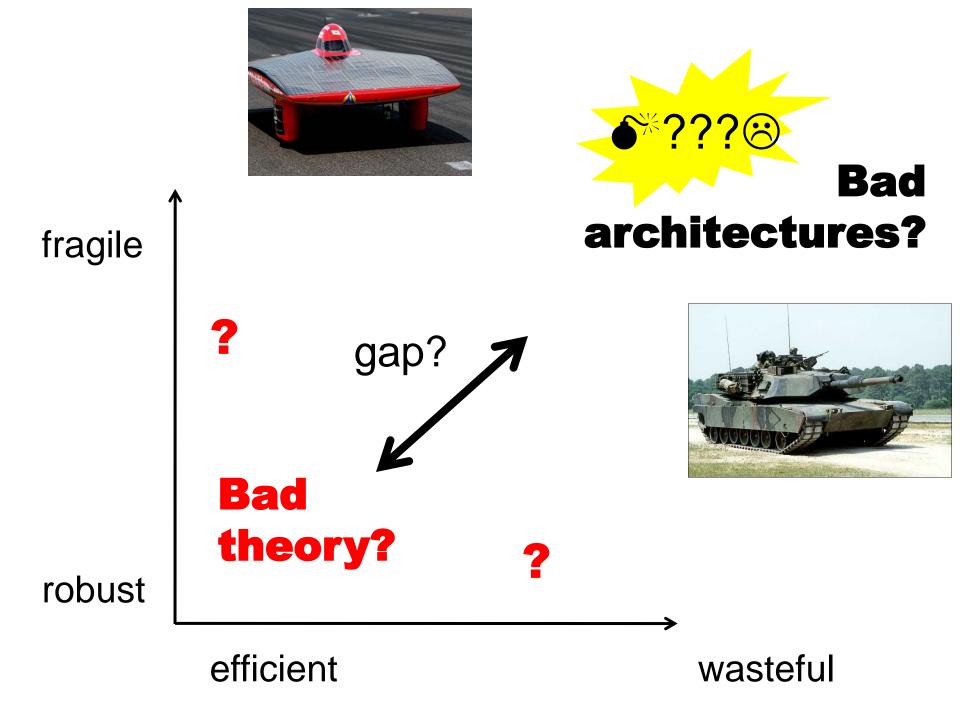


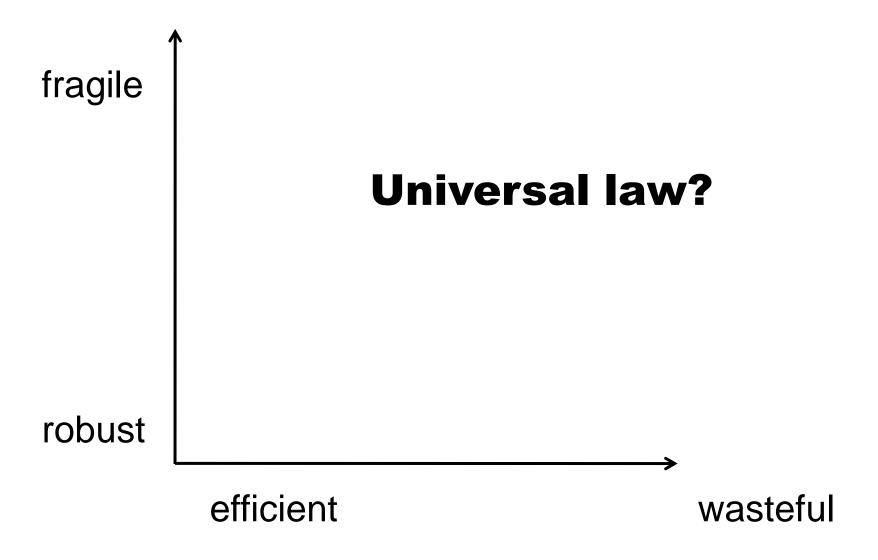
robust

efficient

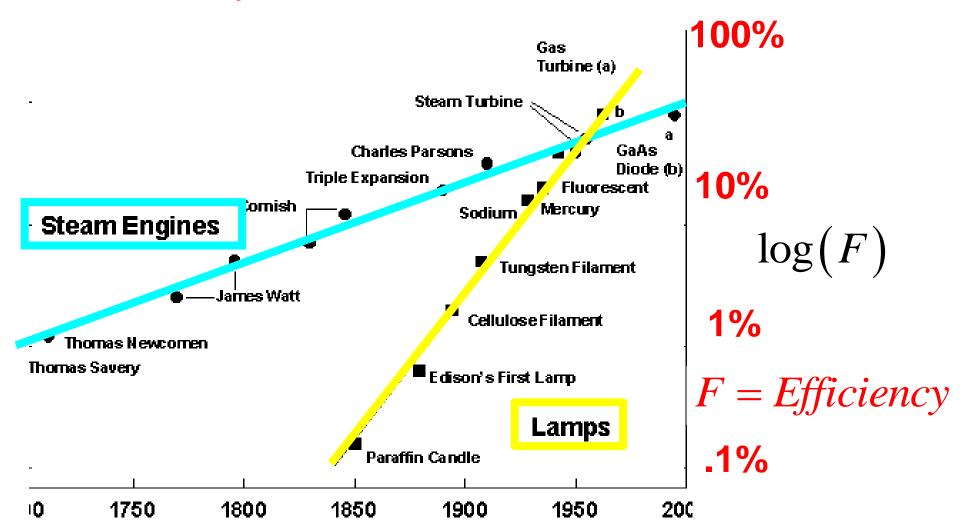
wasteful

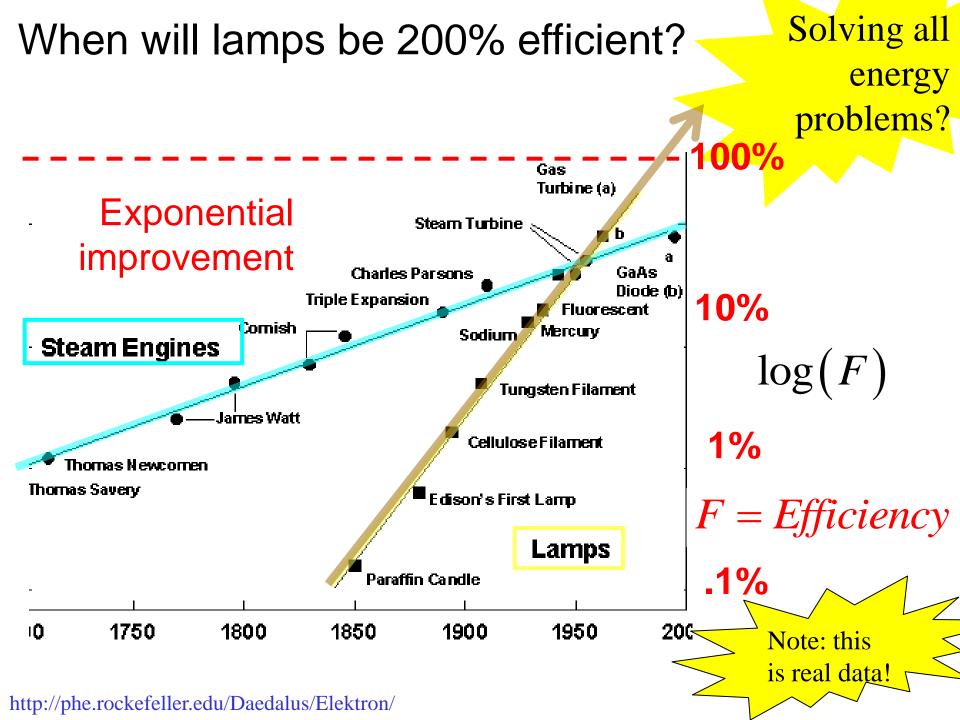




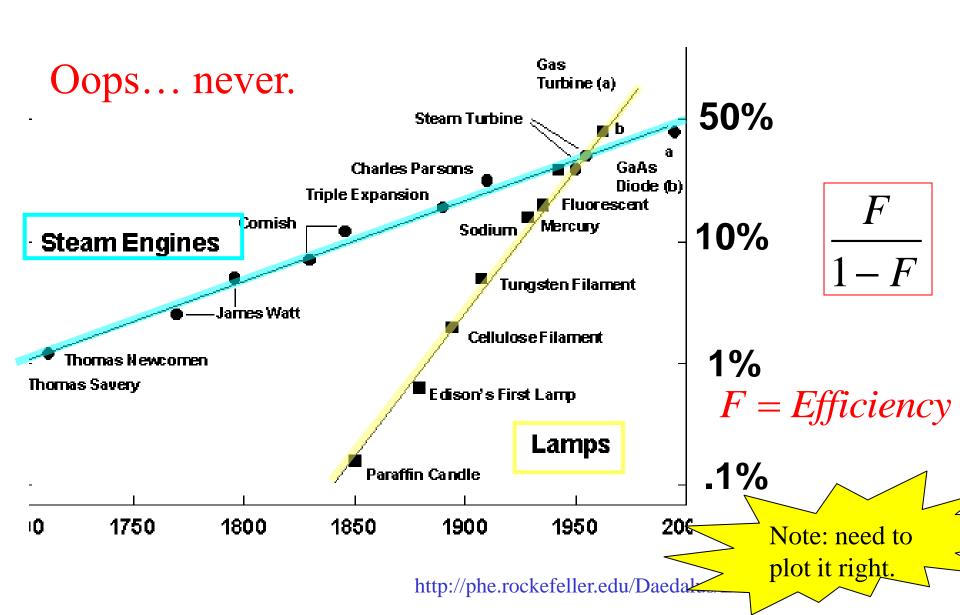


Exponential improvement in efficiency *F*

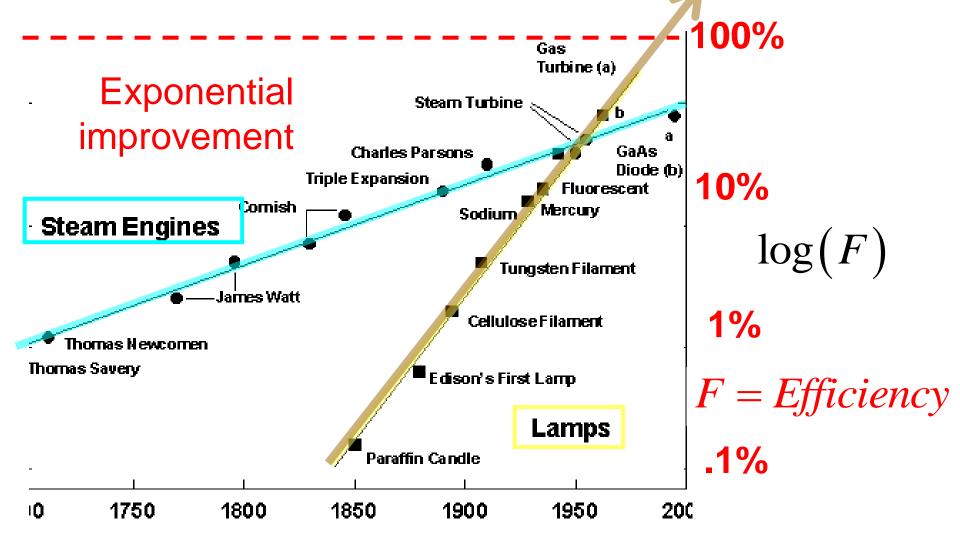




When will lamps be 200% efficient?







Universal law

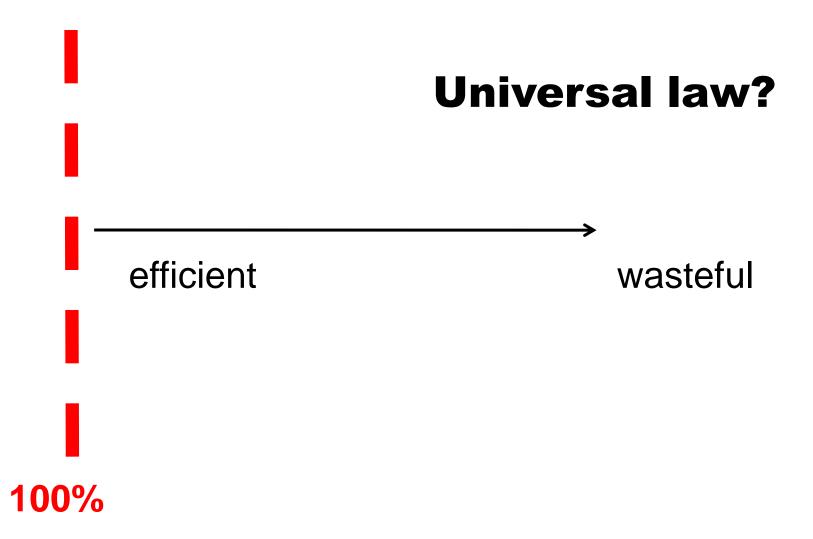
100%

10%

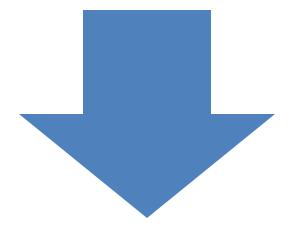
1%

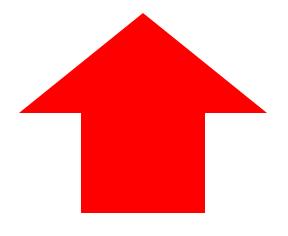
F = Efficiency

.1%



fragile





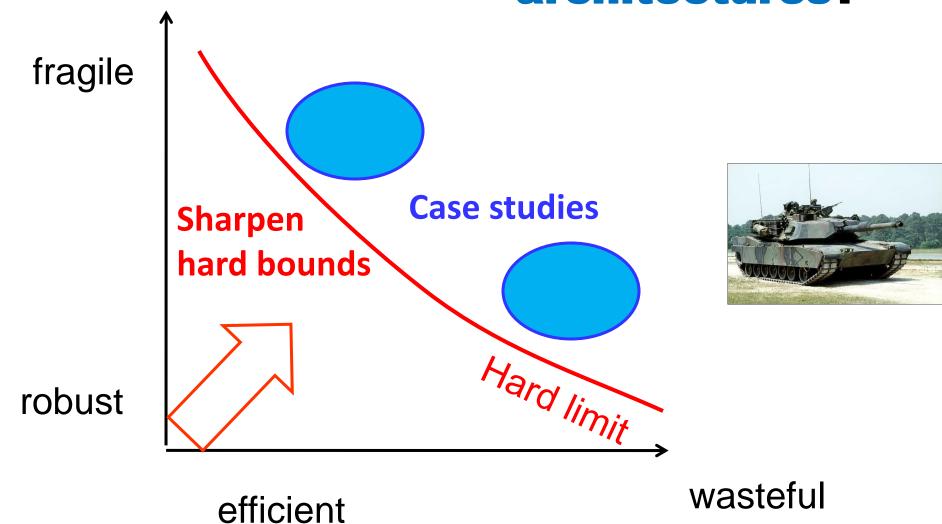
robust

Some features robust to some perturbations

Other features or other perturbations



laws and architectures?



Control, OR

Kalman

Comms

Bode

Pontryagin

Shannon

Nash

Theory?

Von

Deep, but fragmented, incoherent, incomplete

Neumann

Carnot

Turing

Godel

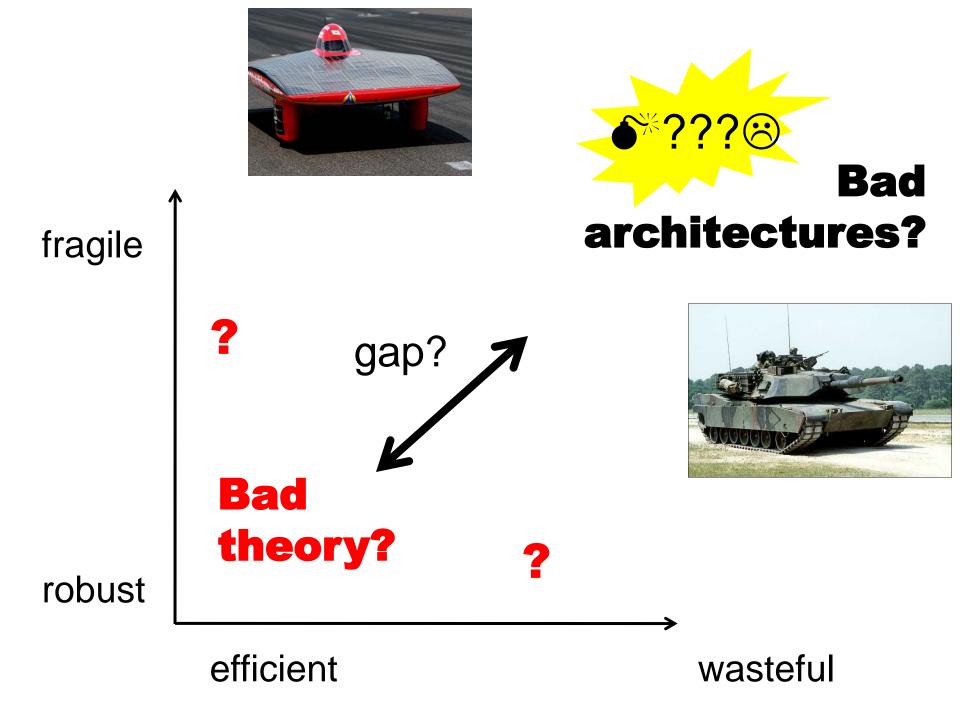
Boltzmann

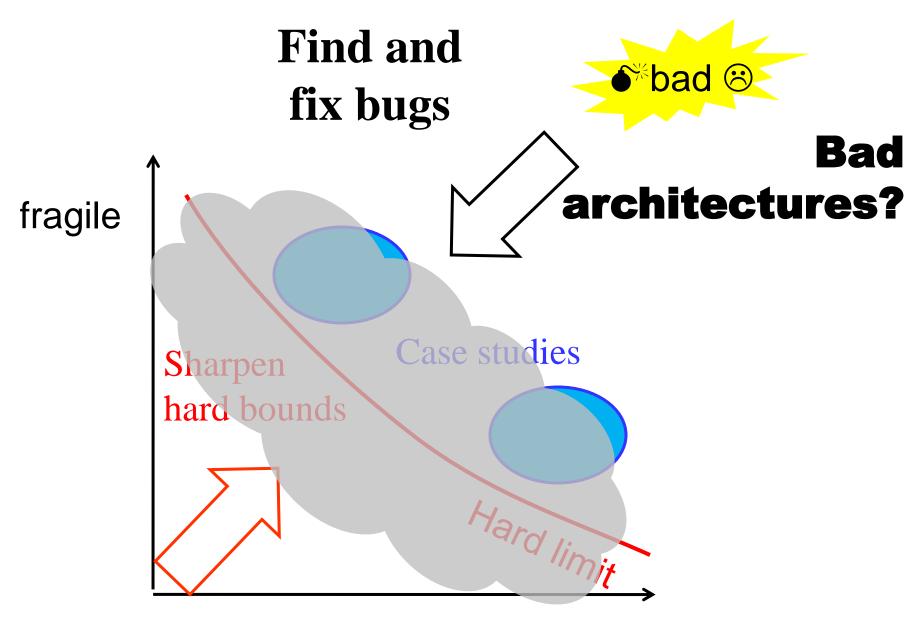
Heisenberg

Compute

Einstein

Physics





wasteful

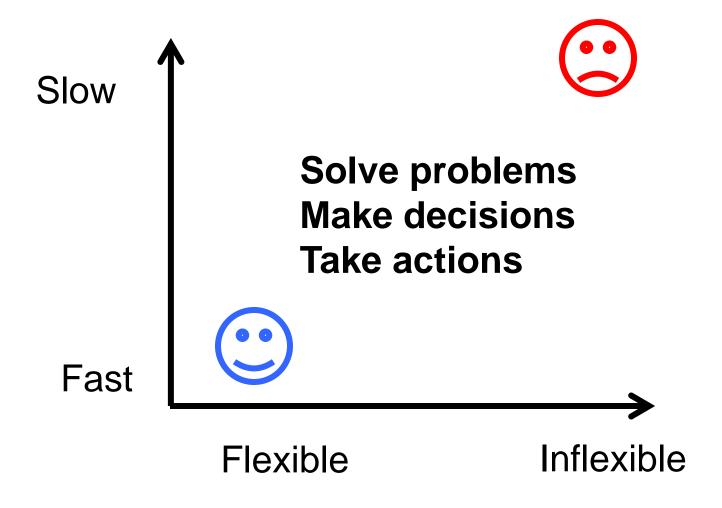
Turing (1912-1954)

- Turing 100th birthday in 2012
- Turing
 - machine (math, CS)
 - test (AI, neuroscience)
 - pattern (biology)
- Arguably greatest*
 - all time math/engineering combination
 - WW2 hero
 - "invented" software

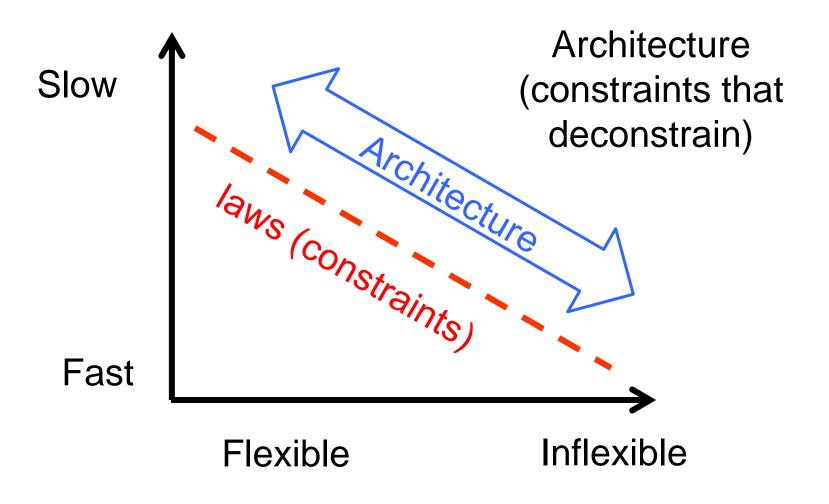
Key papers/results

- Theory (1936): Turing machine (TM), computability, (un)decidability, universal machine (UTM)
- Practical design (early 1940s): code-breaking, including the design of code-breaking machines
- Practical design (late 1940s): general purpose digital computers and software, layered architecture
- Theory (1950): Turing test for machine intelligence
- Theory (1952): Reaction diffusion model of morphogenesis, plus practical use of digital computers to simulate biochemical reactions

Fast and flexible



Laws and architectures



Compute Comms Godel Shannon **Turing** Each theory ≈ one dimension slow? Tradeoffs across dimensions Assume architectures a priori fragile? Progress is encouraging, but... Stovepipes are an obstacle... inflexible? Carnot **Boltzmann** Bode Heisenberg **Physics** Control

Einstein

Turing

Delay is most important

Bode

Control, OR

Communicate

Shannon

Delay is least important

Carnot

Boltzmann

Heisenberg

Physics

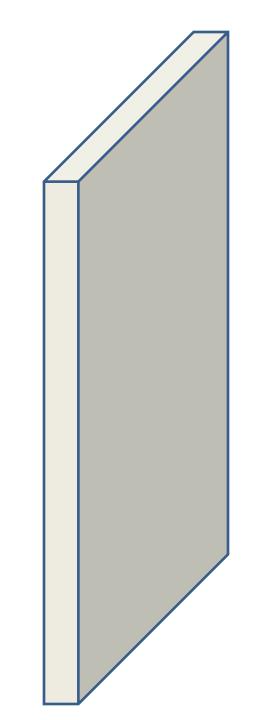
Einstein

Turing

Delay is most important

Bode

Control, OR

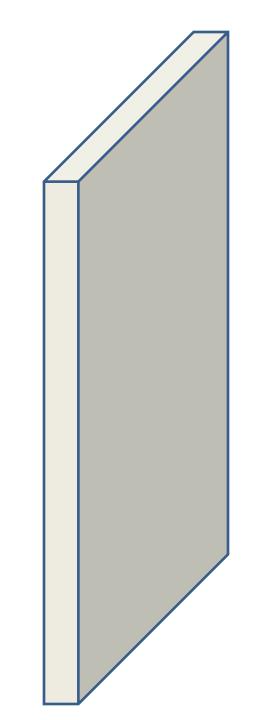


Turing

Delay is most important

Bode

Control, OR



Turing as "new" starting point?

Software
Hardware
Digital
Analog

Compute

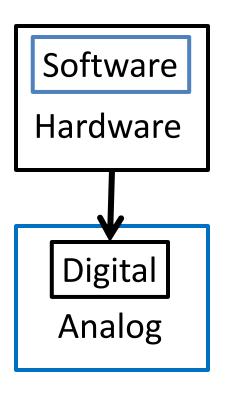
Turing

Delay is most important

Bode

Control, OR

Turing as "new" starting point?



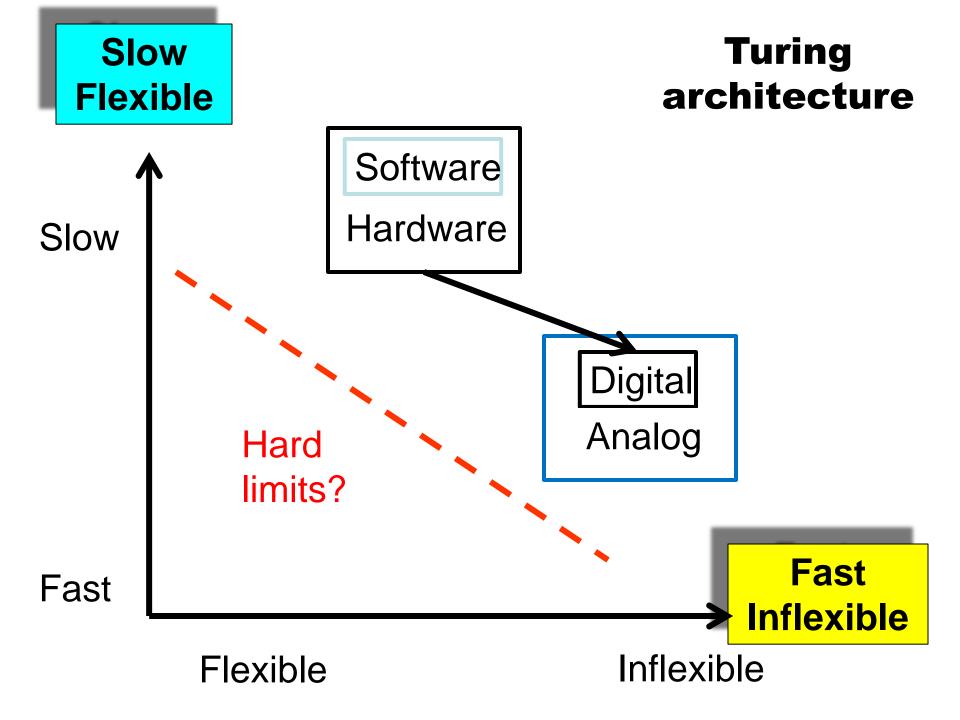
Essentials:

- 0. Model
- 1. Universal laws
- 2. Universal architecture
- 3. Practical implementation

Turing's 3 step research:

- 0. Virtual (TM) machines
- hard limits, (un)decidability using standard model (TM)
- 2. Universal architecture achieving hard limits (UTM)
- 3. Practical implementation in digital electronics (biology?)

Who/what



Flexible

General purpose Large uncertainties Diverse problems

Solve problems Make decisions Take actions

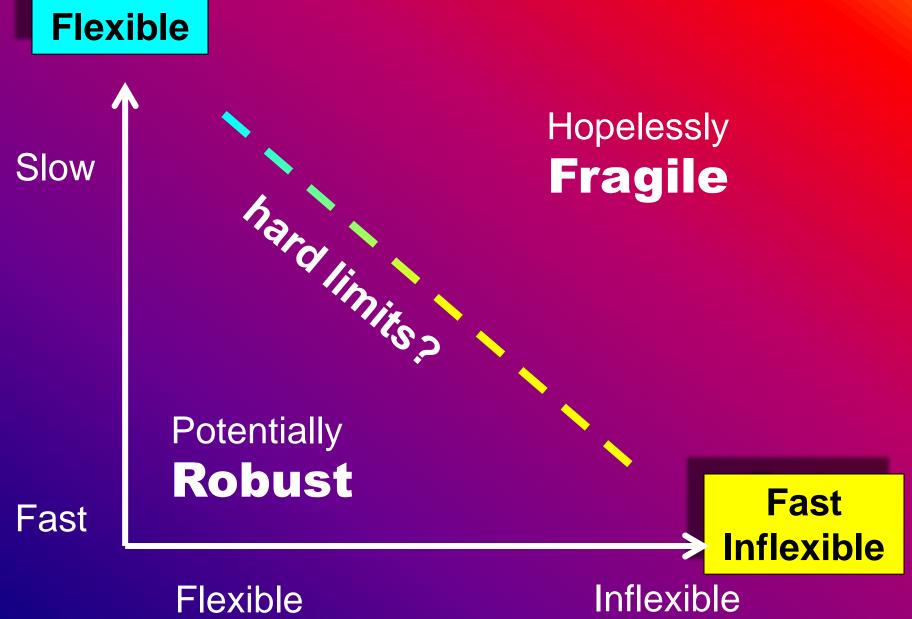
Low latency/delay

Fast

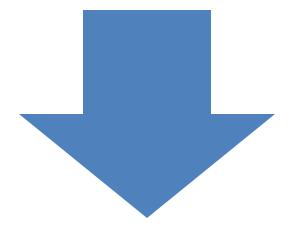
Fast

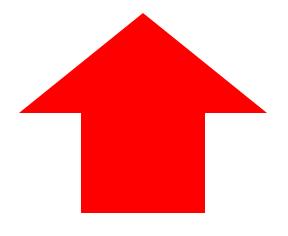
Flexible





fragile

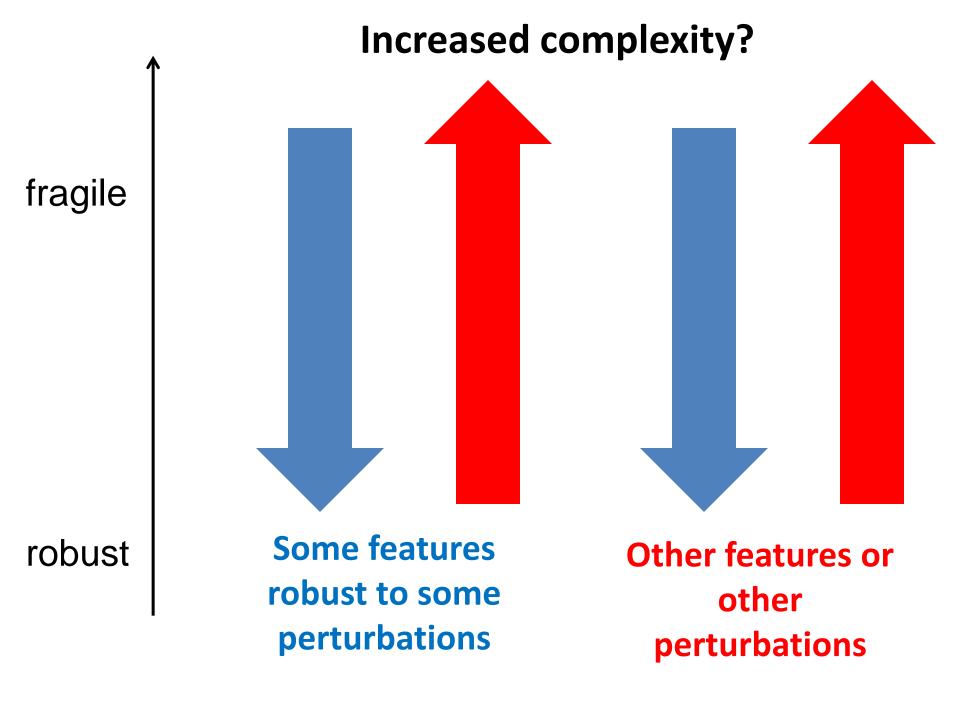




robust

Some features robust to some perturbations

Other features or other perturbations



Robust

Modular

Simple

Plastic

Evolvable

Fragile Dietribu

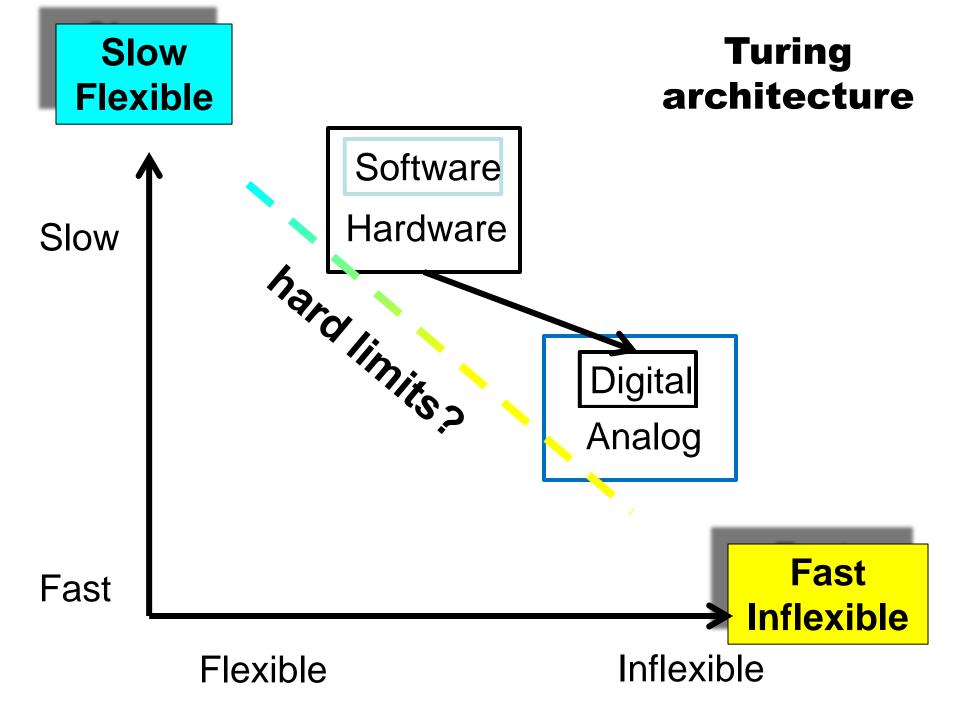
Distributed

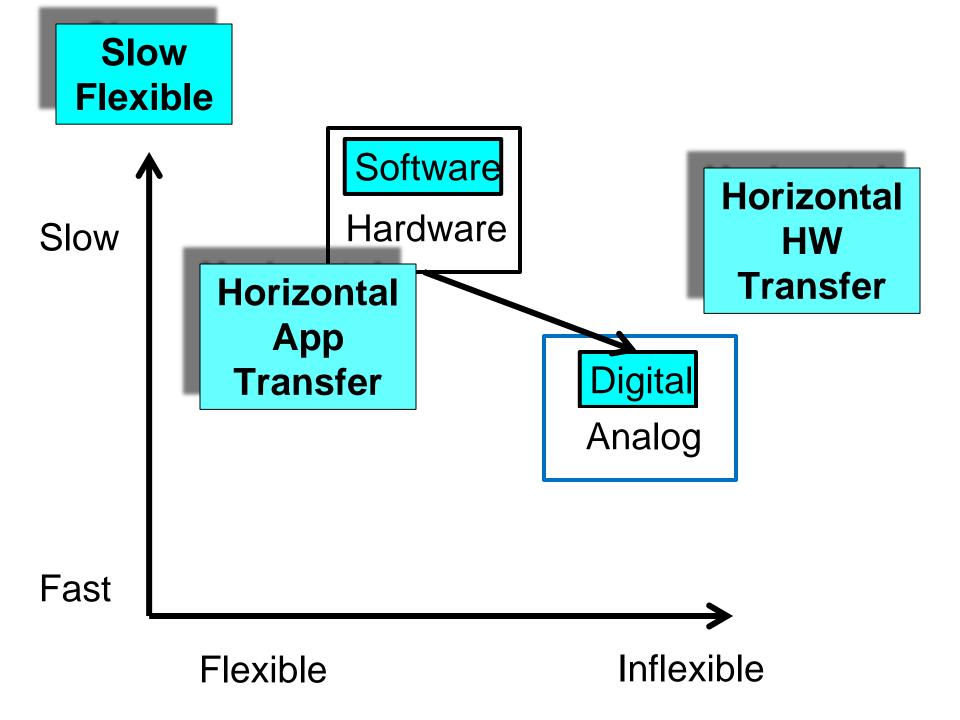
Complex

Frozen

Frozen

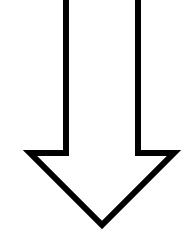




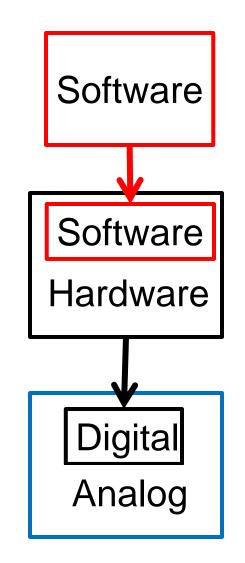


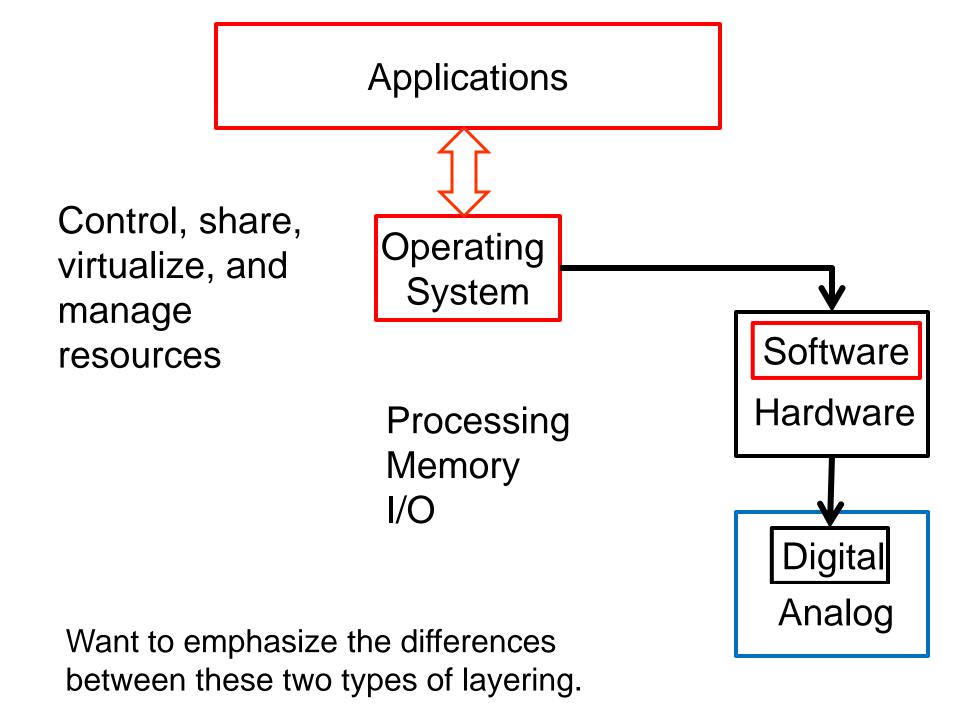
Slow execution Flexible reprogramming

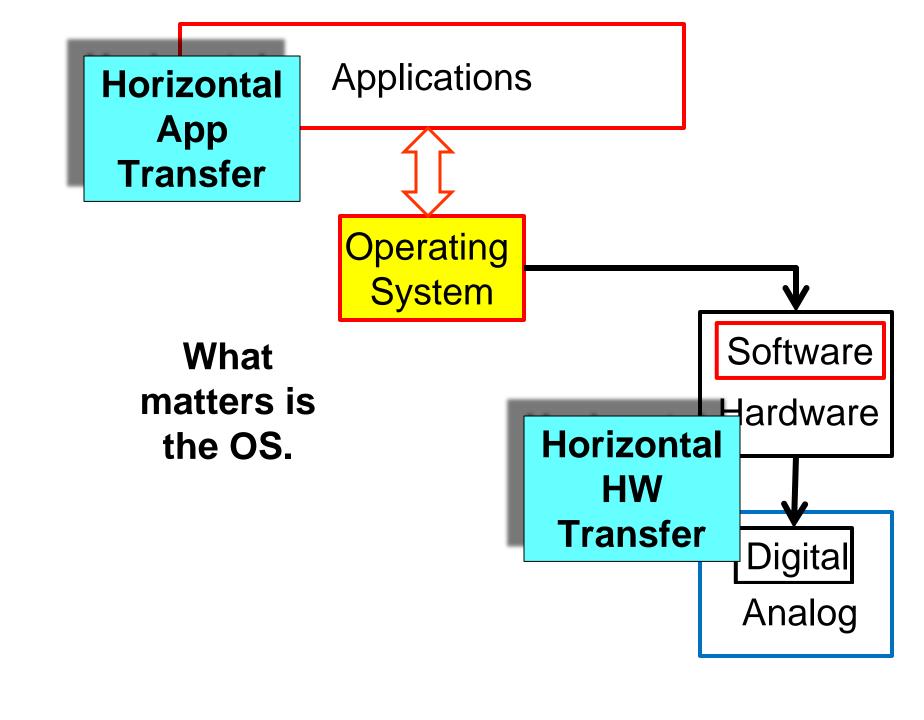
Faster execution Less flexible

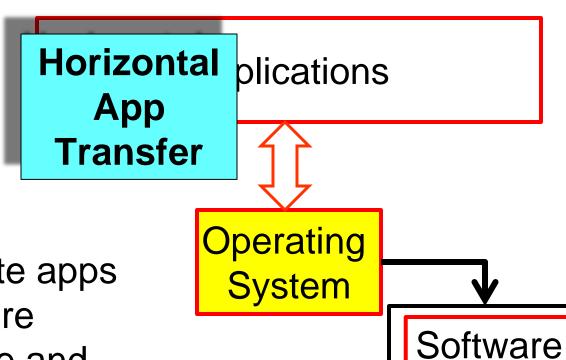


Modern technology gives lots of intermediate alternatives.









Hardware

Analog

tal

Horizontal

HW

Transfer

- Some people write apps and build hardware
- But most software and hardware is acquired by "horizontal" transfer from others
- Similarly, most new ideas (humans) and new genes (bacteria) are acquired horizontally

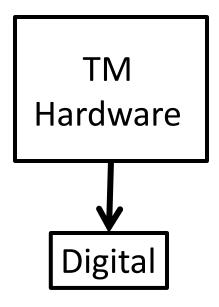
Turing

Why

Necessity

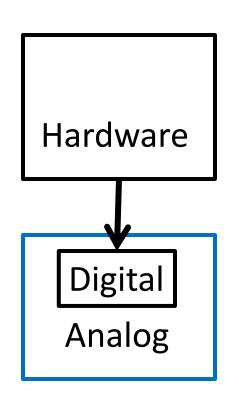
Essentials:

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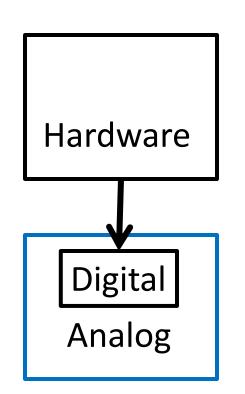
Turing's 3 step research:

- 0. Virtual (TM) machines
- hard limits, (un)decidability using standard model (TM)
- 2. Universal architecture achieving hard limits (UTM)
- 3. Practical implementation in digital electronics (biology?)



- ...being digital should be of greater interest than that of being electronic. That it is electronic is certainly important because these machines owe their high speed to this... But this is virtually all that there is to be said on that subject.
- That the machine is digital however has more subtle significance. ... One can therefore work to any desired degree of accuracy.

1947 Lecture to LMS

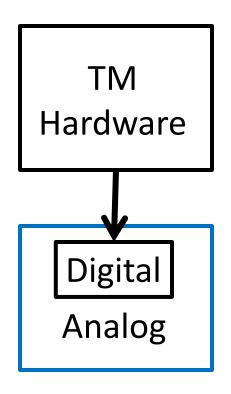


- ... digital ... of greater interest than that of being electronic ...
- ...any desired degree of accuracy...
- This accuracy is not obtained by more careful machining of parts, control of temperature variations, and such means, but by a slight increase in the amount of equipment in the machine.

1947 Lecture to LMS

Summarizing Turing:

- Digital more important than electronic...
- Robustness: accuracy and repeatability.
- Achieved more by internal hidden complexity than precise components or environments.



Turing Machine (TM)

- Digital
- Symbolic
- Logical
- Repeatable

avalanche The butterfly effect

• ... quite small errors in the initial conditions can have an overwhelming effect at a later time. The displacement of a single electron by a billionth of a centimetre at one moment might make the difference between a man being killed by an avalanche a year later, or escaping.

1950, Computing Machinery and Intelligence, *Mind*

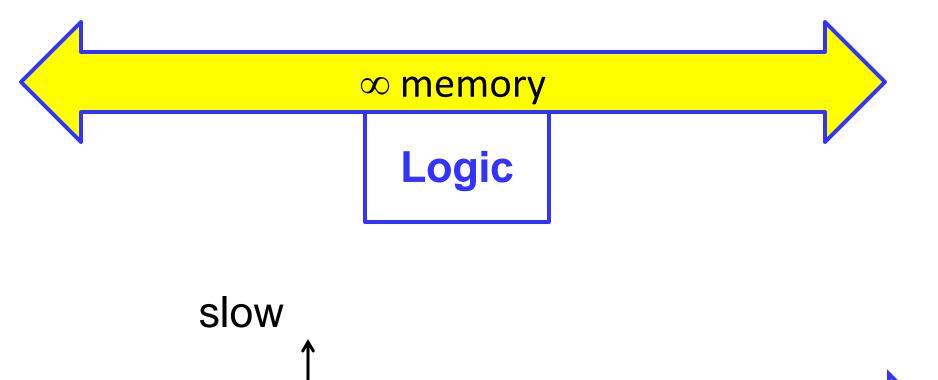
- ... quite small errors in the initial conditions can have an overwhelming effect at a later time....
- It is an essential property of the mechanical systems which we have called 'discrete state machines' that this phenomenon does not occur.
- Even when we consider the actual physical machines instead of the idealised machines, reasonably accurate knowledge of the state at one moment yields reasonably accurate knowledge any number of steps later.

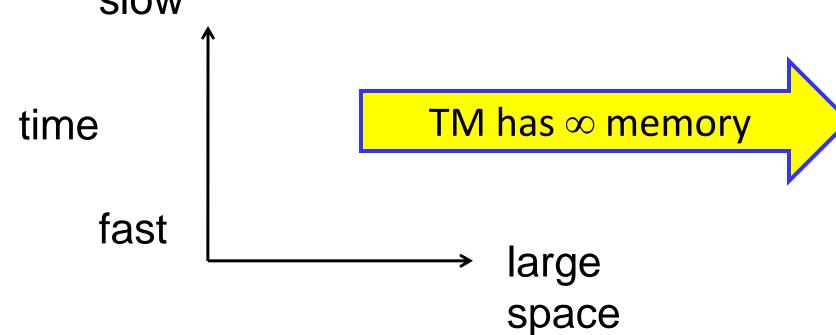
1950, Computing Machinery and Intelligence, Mind

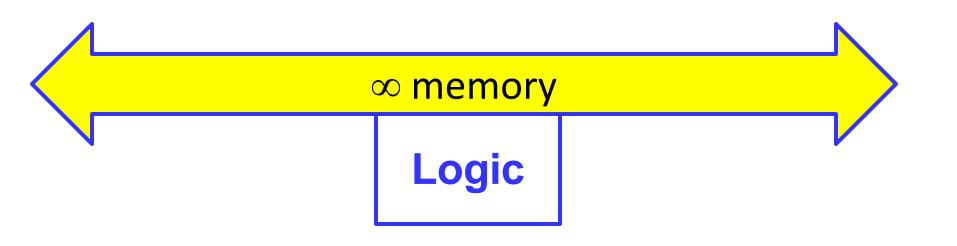
Logic

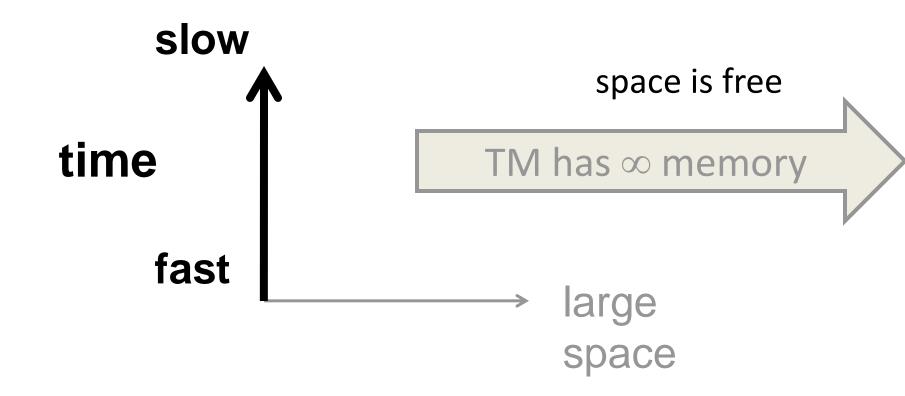
TM Hardware Turing's 3 step research:

- 0. Virtual (TM) machines
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<mark>∞ memory</mark>

Logic

time?

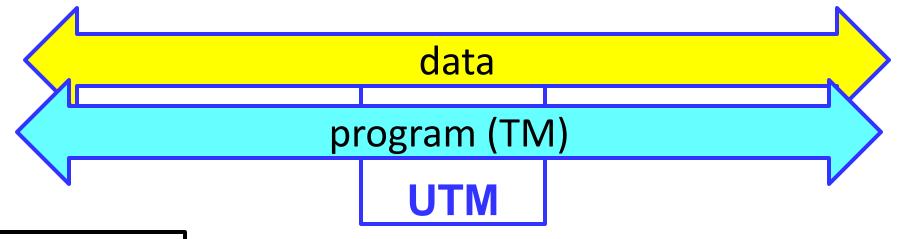
Decidable problem = ∃ algorithm that solves it

Most naively posed problems are undecidable.

program (TM) UTM

Turing's 3 step research:

- 0. Virtual (TM) machines
- 1. hard limits, (un)decidability using standard model (TM)
- 2. Universal architecture achieving hard limits (UTM)
- 3. Practical implementation in digital electronics (biology?)



Software Hardware

2. Universal architecture achieving hard limits (UTM)

- Software: A Turing machine (TM) can be data for another Turing machine
- A Universal Turing Machine can run any TM
- A UTM is a virtual machine.
- There are lots of UTMs, differ only (but greatly) in speed and programmability (space assumed free)

TM program HALT UTM

The halting problem

- Given a TM (i.e. a computer program)
- Does it halt (or run forever)?
- Or do more or less anything in particular.
- Undecidable! There does not exist a special TM that can tell if any other TM halts.
- i.e. the program HALT does not exist. 🕾

Thm: TM H=HALT does not exist.

That is, there does not exist a program like this:

$$H(TM,input) \triangleq \begin{cases} 1 \text{ if } TM(input) \text{ halts} \\ 0 \text{ otherwise} \end{cases}$$

Proof is by contradiction. Sorry, don't know any alternative. And Turing is a god.

$$H(TM, input) \triangleq \begin{cases} 1 \text{ if } TM(input) \text{ halts} \\ 0 \text{ otherwise} \end{cases}$$

Thm: No such H exists.

Proof: Suppose it does. Then define 2 more programs:

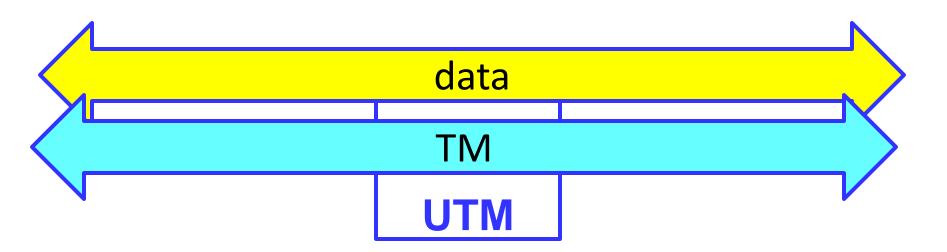
$$H'(TM,input) \triangleq \begin{cases} 1 \text{ if } H(TM,input) = 0 \\ \text{loop forever otherwise} \end{cases}$$

$$H*(TM) \triangleq H'(TM,TM)$$

$$Run \ H*(H*) = H'(H*,H*)$$

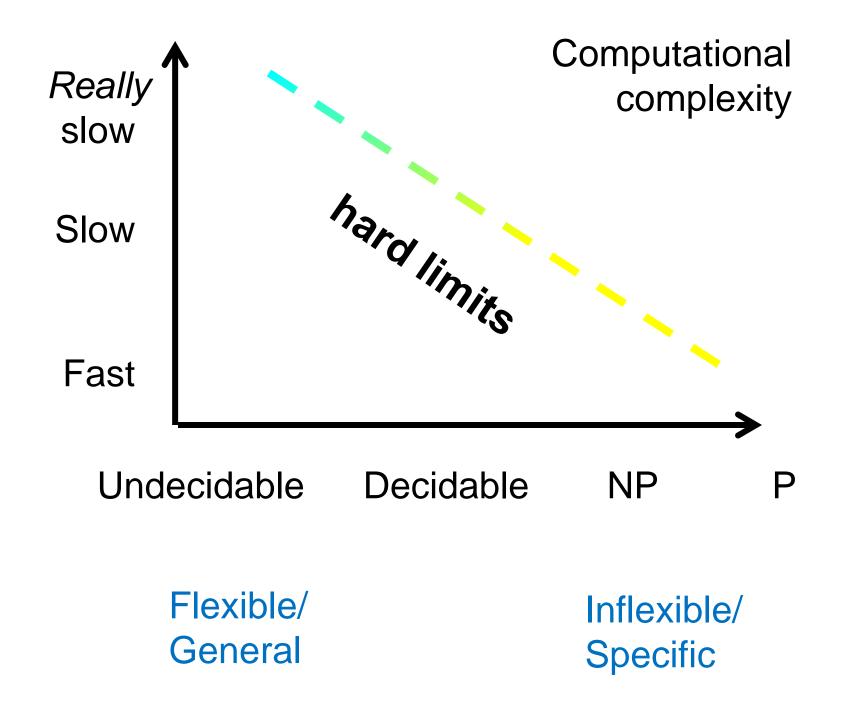
$$= \begin{cases} \text{halt if } H*(H*) \text{ loops forever} \\ \text{loop forever otherwise} \end{cases}$$

Contradiction!



Implications

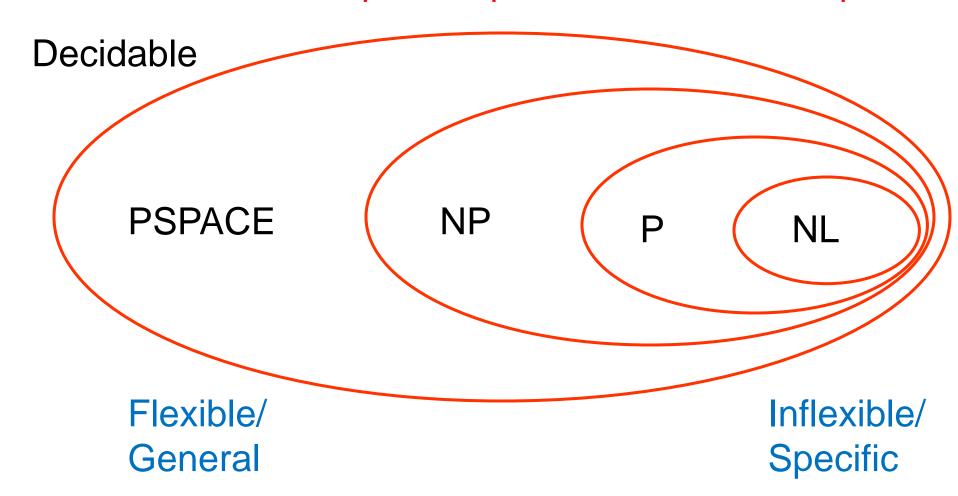
- Large, thin, nonconvex everywhere...
- TMs and UTMs are perfectly repeatable
- But perfectly unpredictable
- Undecidable: Will a TM halt? Is a TM a UTM? Does a TM do X (for almost any X)?
- Easy to make UTMs, but hard to recognize them.
- Is anything decidable? Yes, questions NOT about TMs.



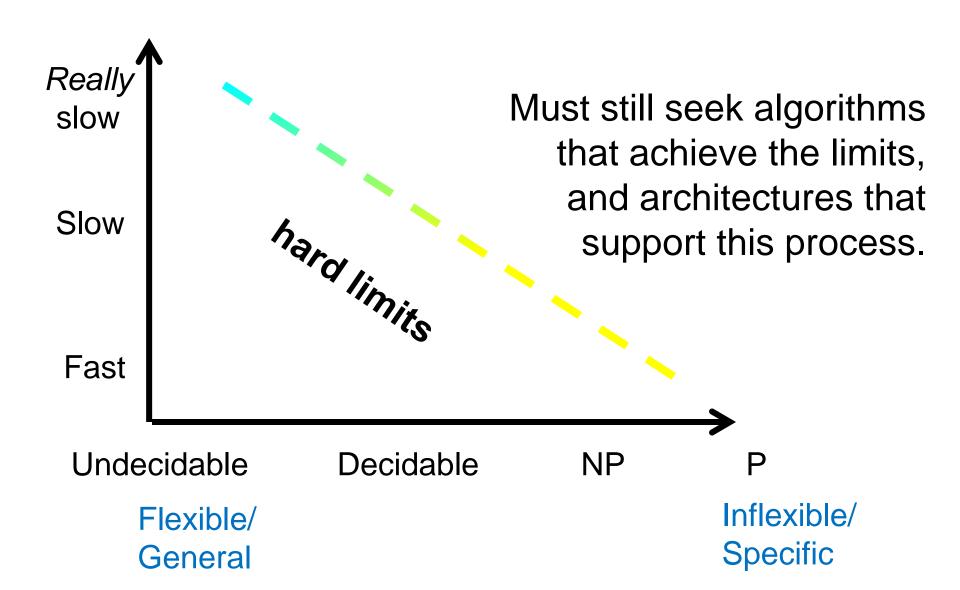
PSPACE⊂NP⊂P⊂NL PSPACE ≠ NL

Computational complexity

Space is powerful and/or cheap.



These are hard limits on the *intrinsic* computational complexity of *problems*.



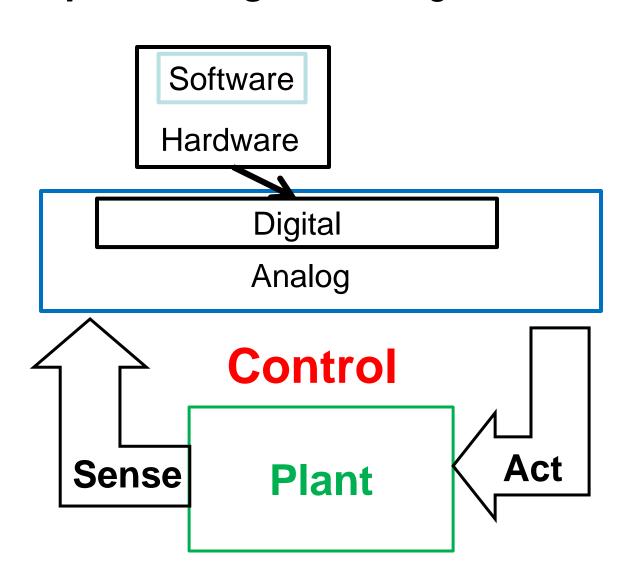
Compute

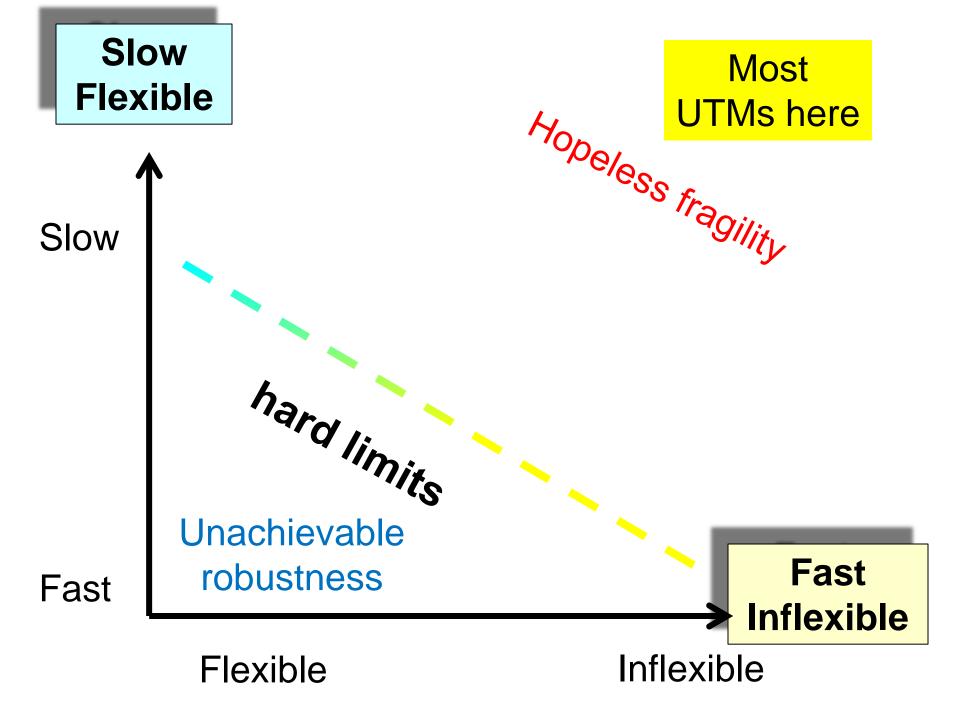
Computational complexity of

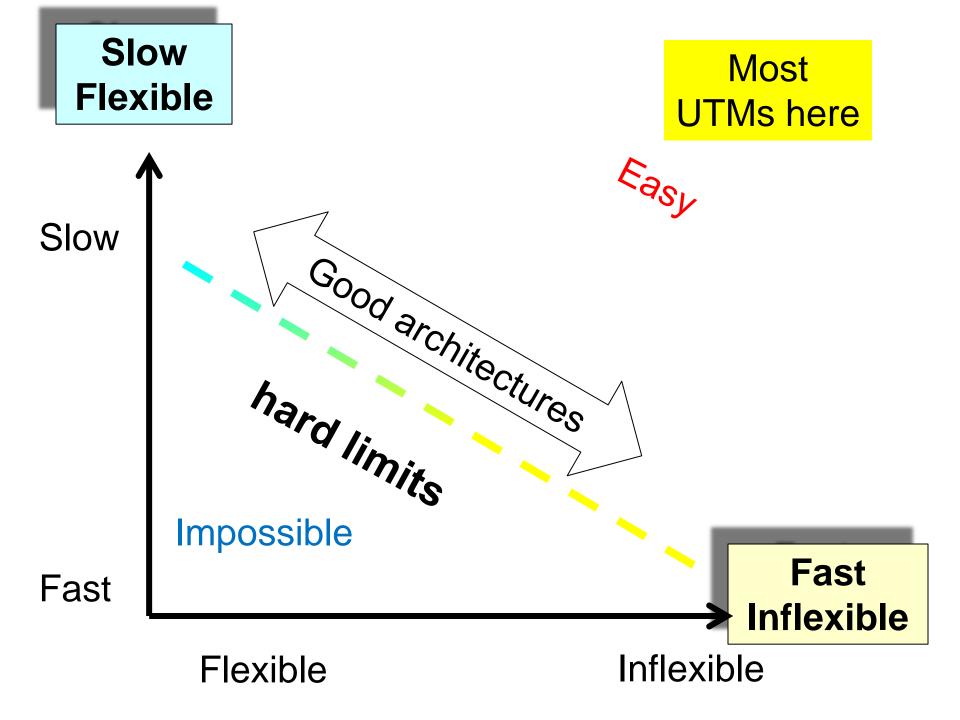
- Designing control algorithms
- Implementing control algorithms

Delay is even more important in control

Control







Issues for engineering

- Turing remarkably relevant for 76 years
- UTMs are ≈ implementable
 - Differ only (but greatly) in speed and programmability
 - Time/speed/delay is most critical resource
 - Space (memory) almost free for most purposes
- Read/write random access memory hierarchies
- Further gradations of decidable (P/NP/coNP)

Most crucial:

- UTMs differ vastly in speed, usability, and programmability
- You can fix bugs but it is hard to automate finding/avoiding them

Issues for engineering

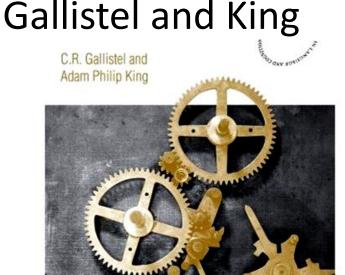
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- Read/write random access memory hierarchies
- Further gradations of decidable (P/NP/coNP)

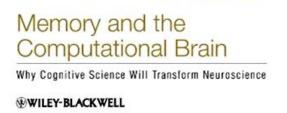
Most crucial:

- UTMs differ *vastly* in speed, usability, and programmability
- You can fix bugs but it is hard to automate finding/avoiding them

Conjectures, biology

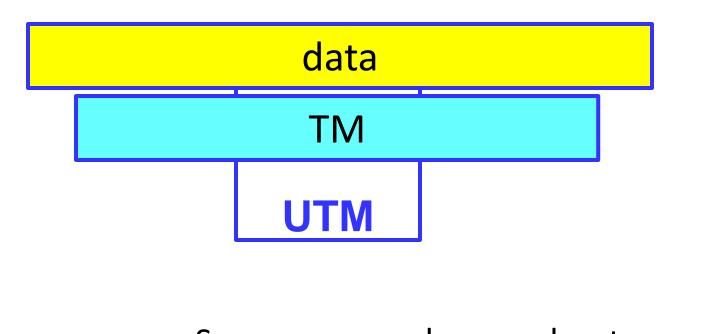
- Memory potential ≈ ∞
- Examples
 - Insects
 - Scrub jays
 - Autistic Savants

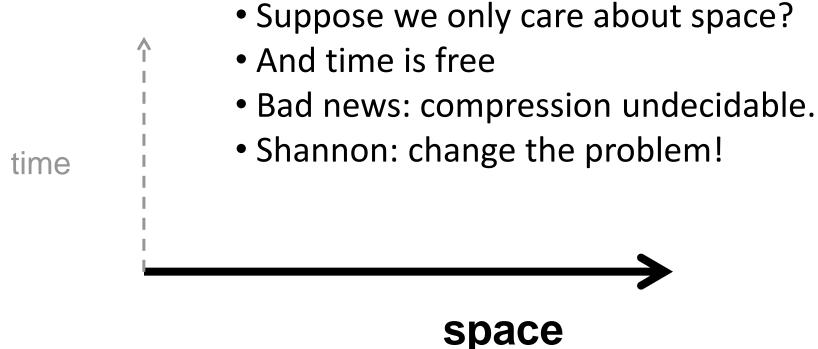




- But why so rare and/or accidental?
- Large memory, computation of limited value?
- Selection favors fast robust action?
- Brains are distributed (not studied by Gallistel)

Compute Communicate Turing Shannon Delay i **Delay** is most least importa important Carnot Bode **Boltzmann** Control, Heisenberg **Physics** Einstein





Communications

Shannon's brilliant insight

Shannon

- Forget time
- Forget files, use *infinite random ensembles*

Good news

- Laws and architecture!
- Info theory most popular and accessible topic in systems engineering
- Fantastic for some engineering problems

Communications

Shannon's brilliant insight

Shannon

- Forget time
- Forget files, use infinite random ensembles

Bad news

Laws and architecture very brittle

- Less than zero impact on internet architecture
- Almost useless for biology (But see Lestas et al, 2010)
- Misled, distracted generations of biologists (and neuroscientists)

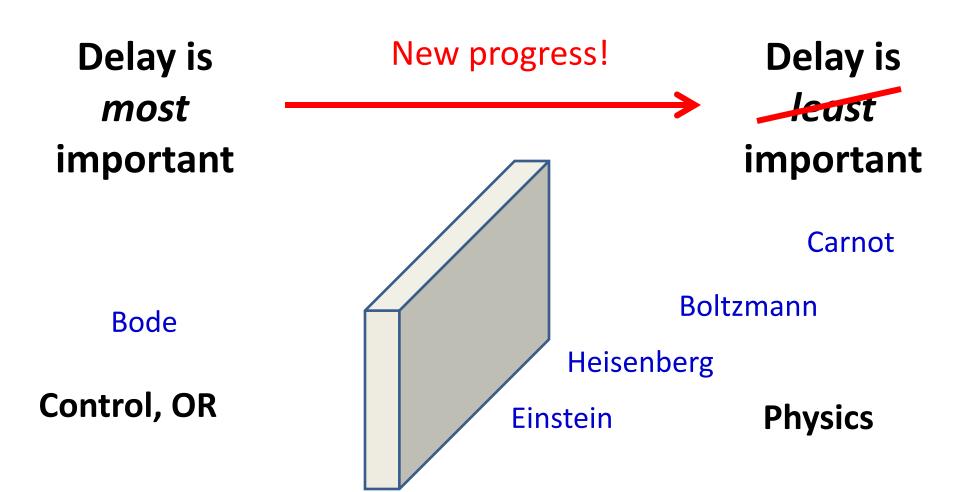
Compute

Communicate

Turing

Lowering the barrier

Shannon



System

"Emergent":
"Nontrivial"
consequences
of other
constraints

Architecture = Constraints

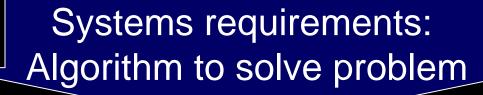
data

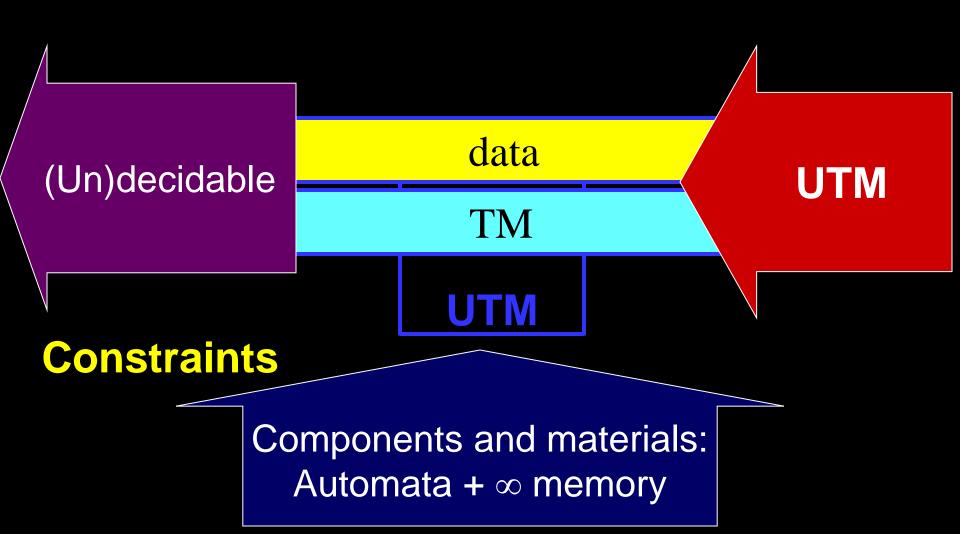
TM

UTN

Protocols

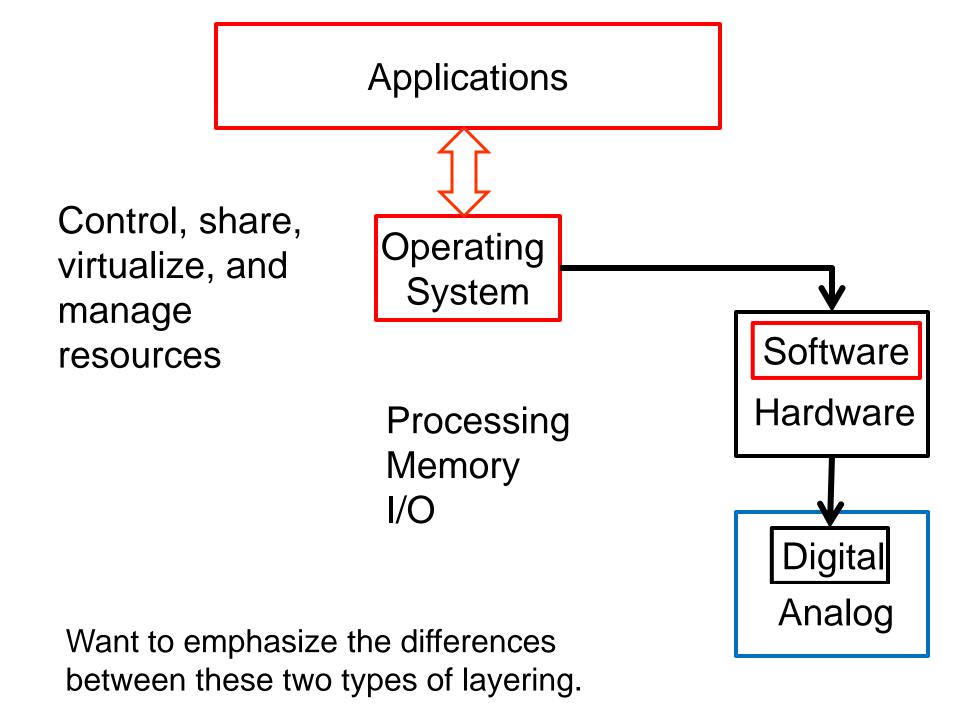
Components



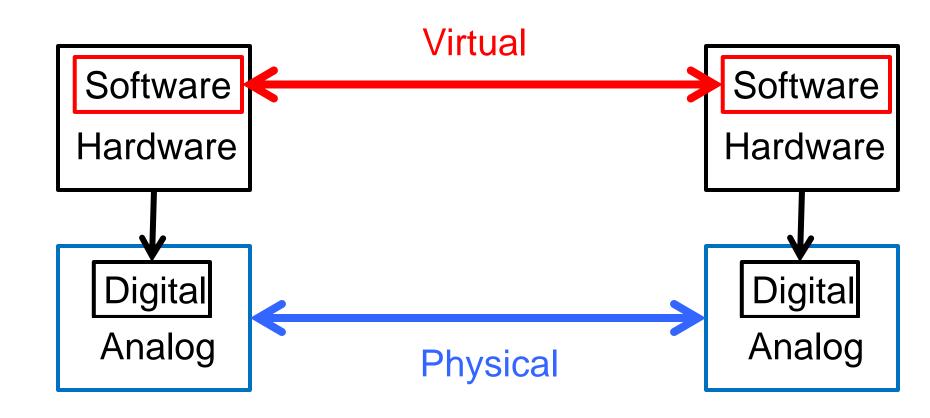


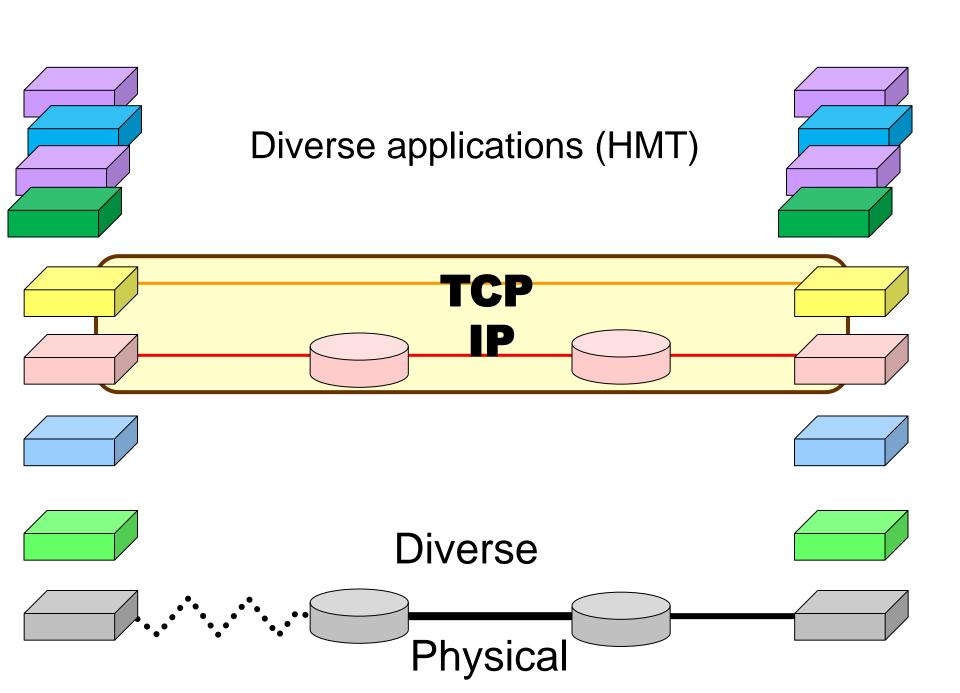
Universal architectures

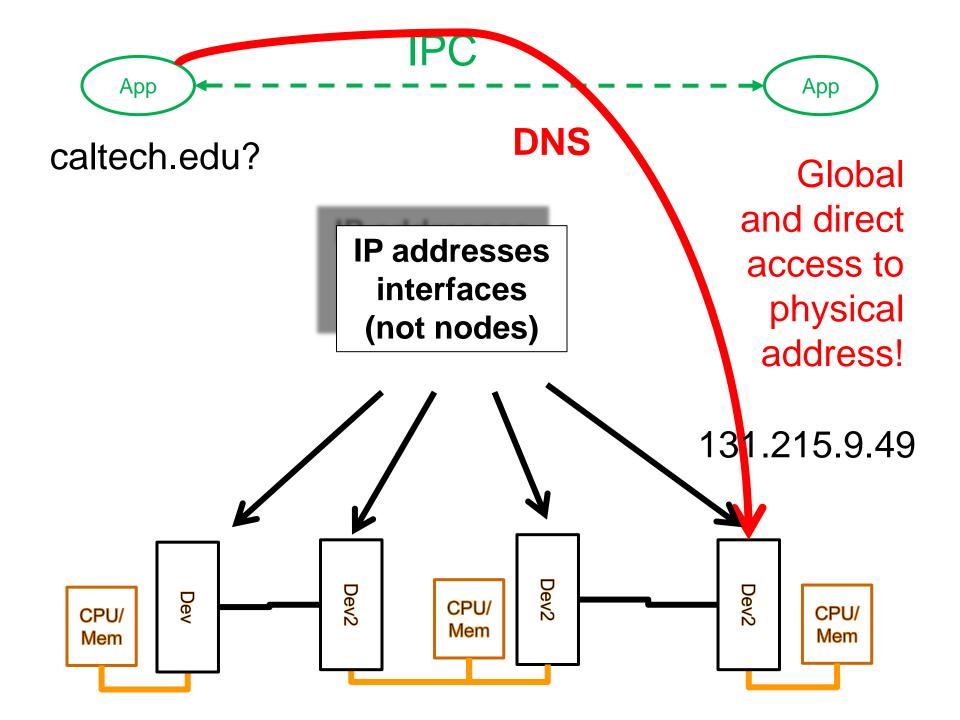
What can go wrong?

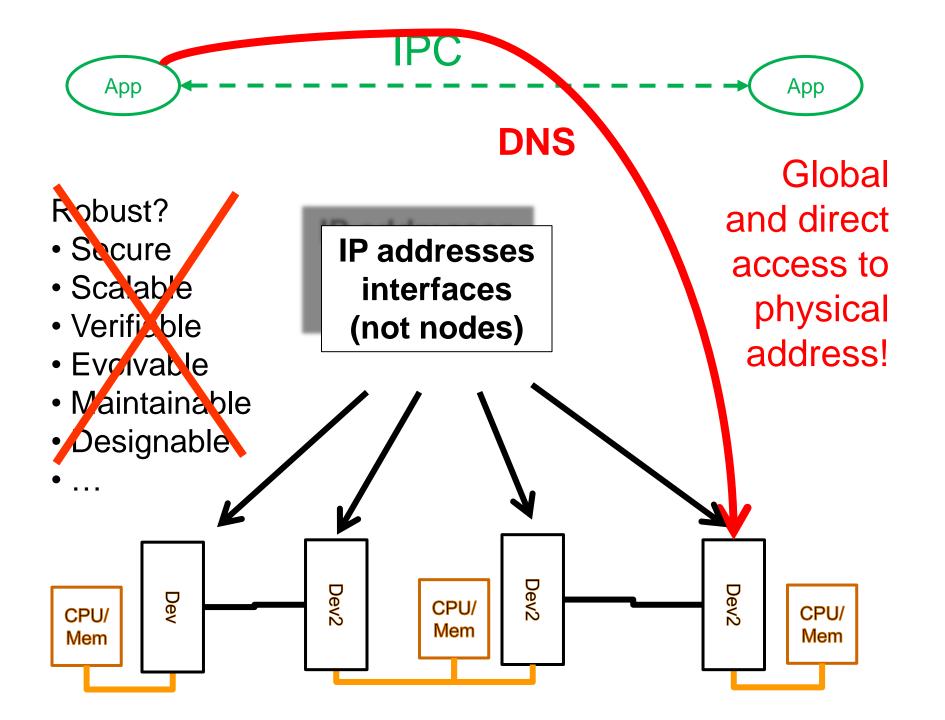


Networking









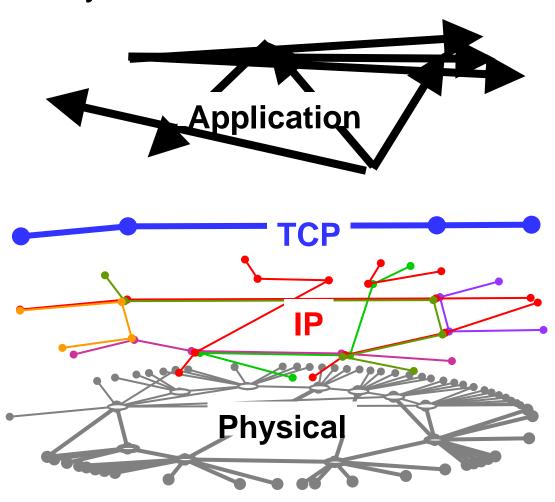
Naming and addressing need to have scope and

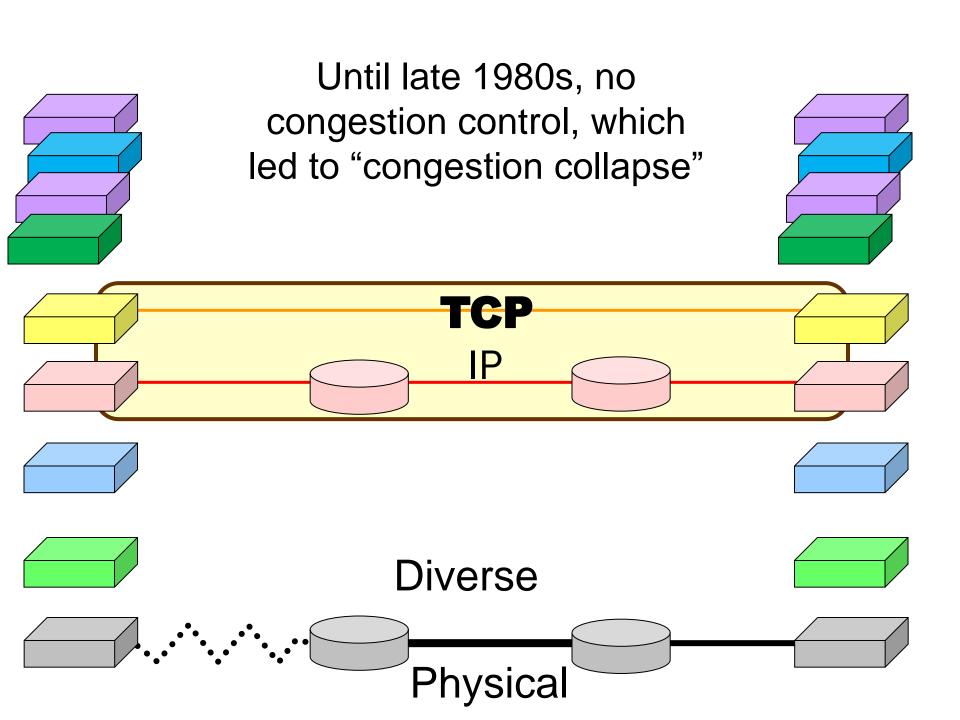
- resolved within layer
- translated between layers
- not exposed outside of layer

Related "issues"

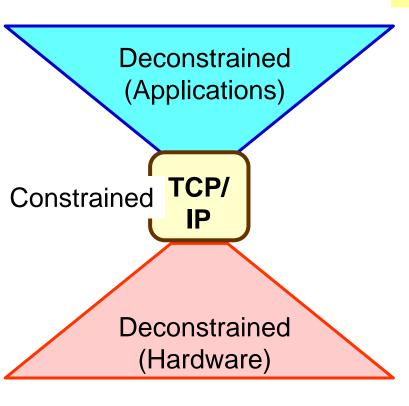
- VPNs
- NATS
- Firewalls
- Multihoming
- Mobility
- Routing table size
- Overlays

• . . .





Original design challenge?

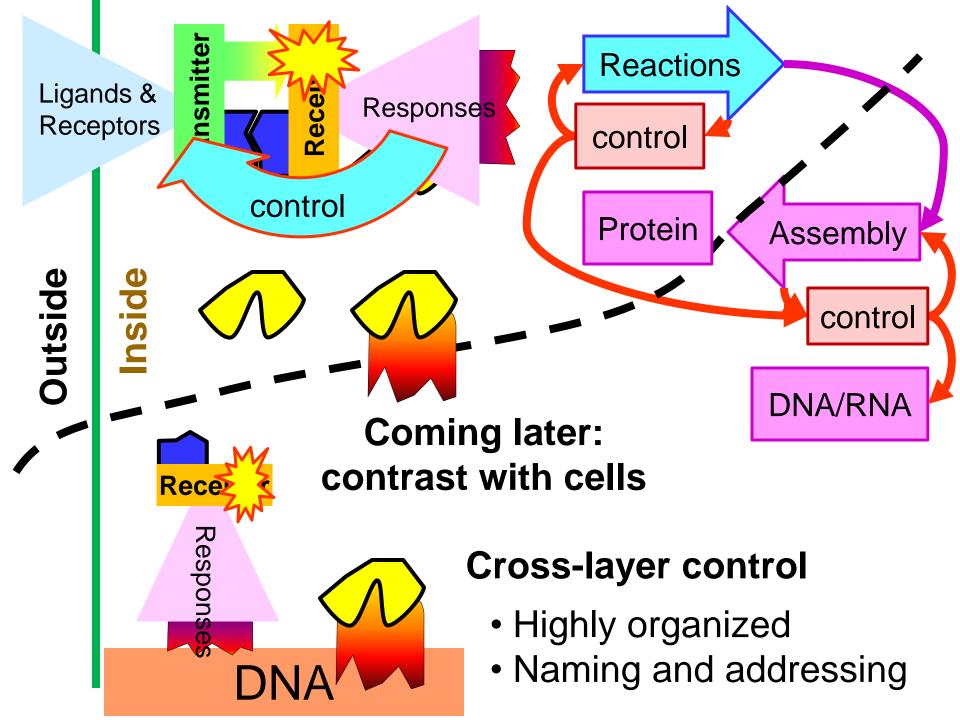


Networked OS

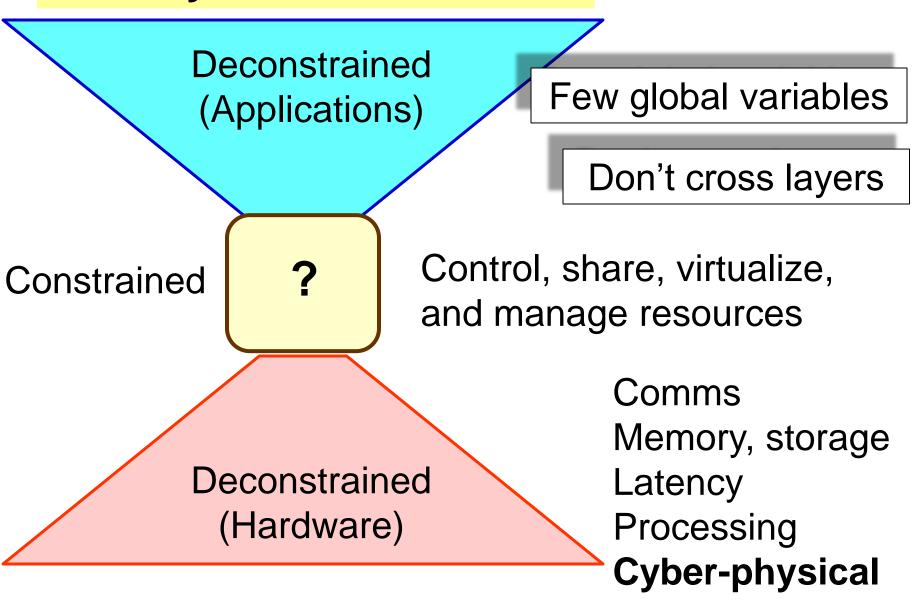
- Expensive mainframes
- Trusted end systems
- Homogeneous
- Sender centric
- Unreliable comms

Facilitated wild evolution Created

- whole new ecosystem
- completely opposite

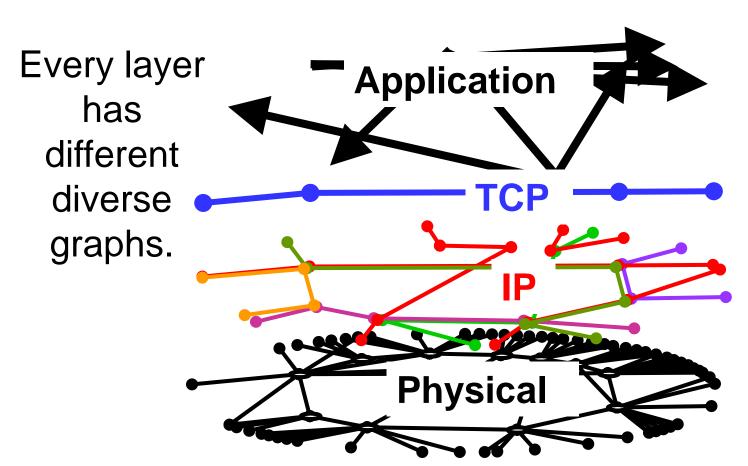


Next layered architectures



Persistent errors and confusion ("network science")

Architecture is *least* graph topology.



Architecture facilitates arbitrary graphs.

PNAS

The "robust yet fragile" nature of the Internet

John C. Doyle*[†], David L. Alderson*, Lun Li*, Steven Low*, Matthew Roughan[‡], Stanislav Shalunov[§], Reiko Tanaka[¶], and Walter Willinger^{||}

*Engineering and Applied Sciences Division, California Institute of Technology, Pasadena, CA 91125; [‡]Applied Mathematics, University of Adelaide, South Australia 5005, Australia; [§]Internet2, 3025 Boardwalk Drive, Suite 200, Ann Arbor, MI 48108; [¶]Bio-Mimetic Control Research Center, Institute of Physical and Chemical Research, Nagoya 463-0003, Japan; and [¶]AT&T Labs-Research, Florham Park, NJ 07932

Edited by Robert M. May, University of Oxford, Oxford, United Kingdom, and approved August 29, 2005 (received for review February 18, 2005)

The search for unifying properties of complex networks is popular, challenging, and important. For modeling approaches that focus on

no self-loops or parallel edges) having the same graph degree We will say that graphs $g \in G(D)$ have scaling-degree sequen

PNAS | October 11, 2005 | vol. 102 | no. 41 | 14497–14502

Notices of the AMS, 2009

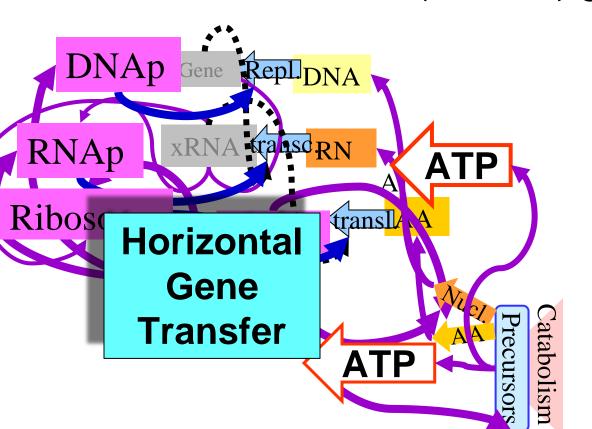
Mathematics and the Internet: A Source of Enormous Confusion and Great Potential

Walter Willinger, David Alderson, and John C. Doyle

Who and what

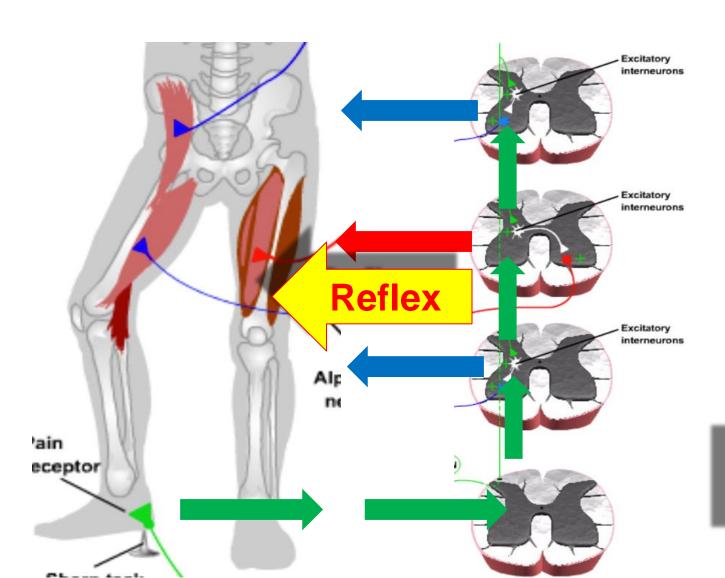
Sequence ~100 E Coli (not chosen randomly)

- ~ 4K genes per cell
- ~20K different genes in total
- ~ 1K universally shared genes
- ~ 300 essential (minimal) genes

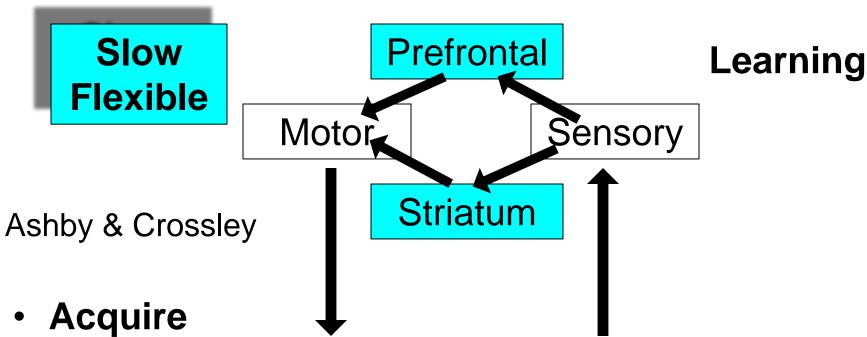


See slides on bacterial biosphere

Neuro motivation



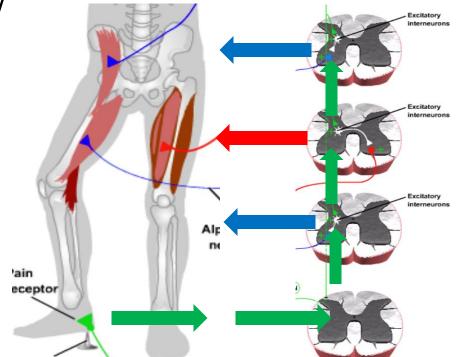
Fast Inflexible



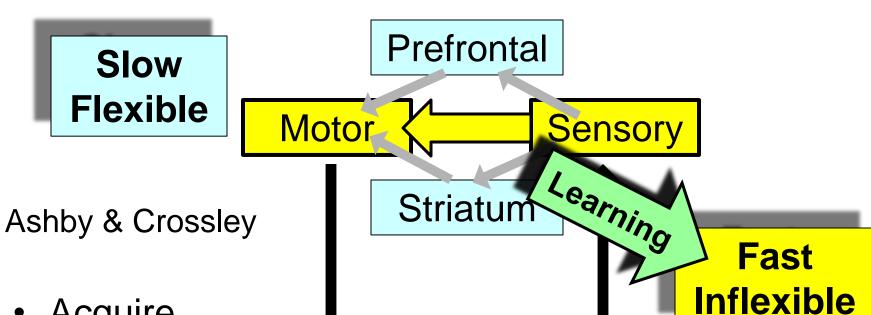
Acquire

 Translate/ integrate

Automate



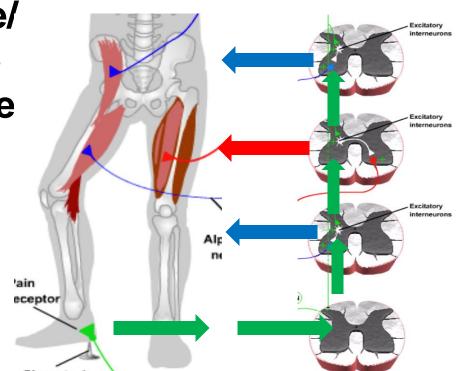
Thanks to **Bassett & Grafton**

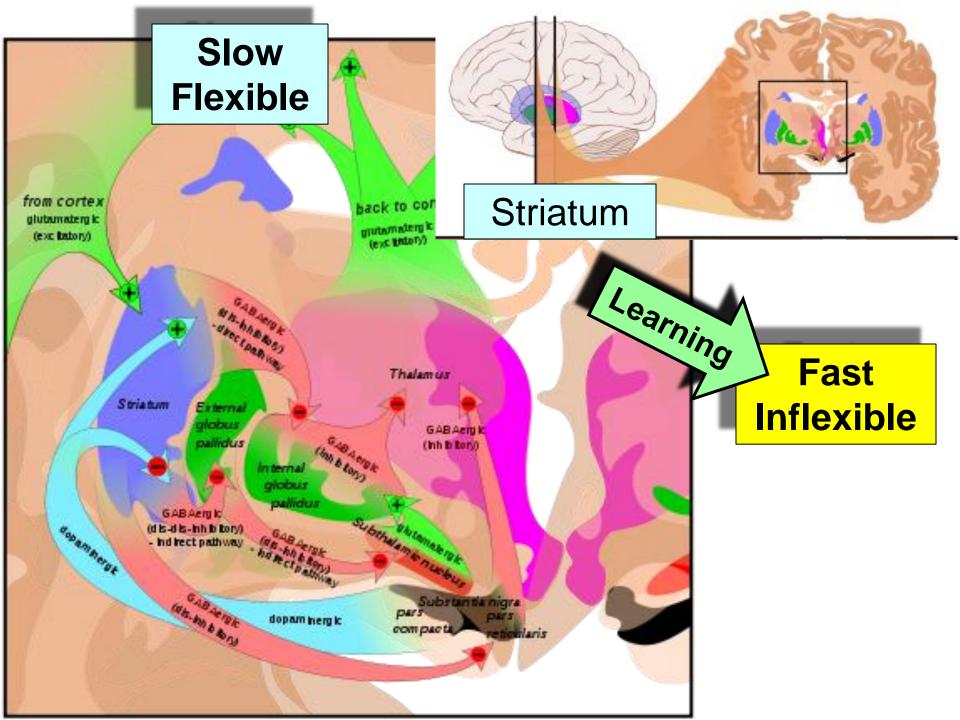


Acquire

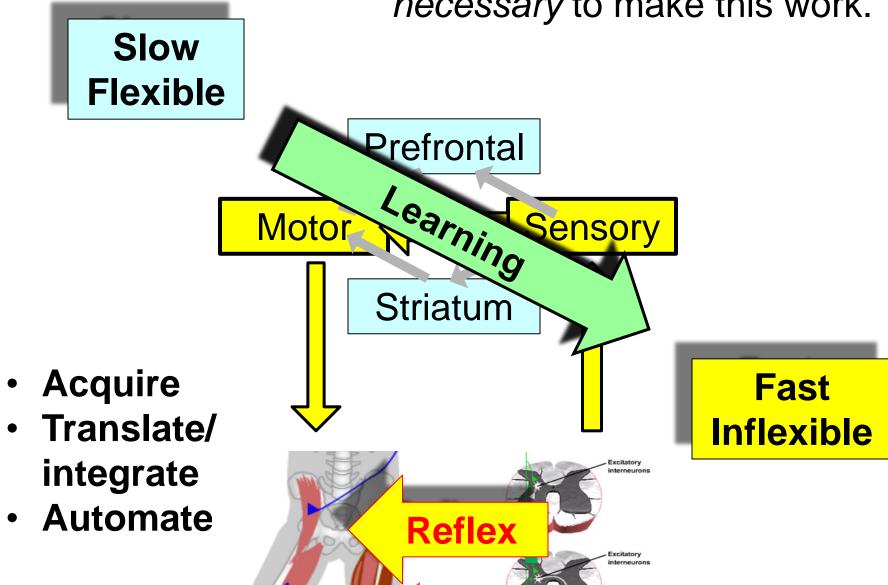
 Translate/ integrate

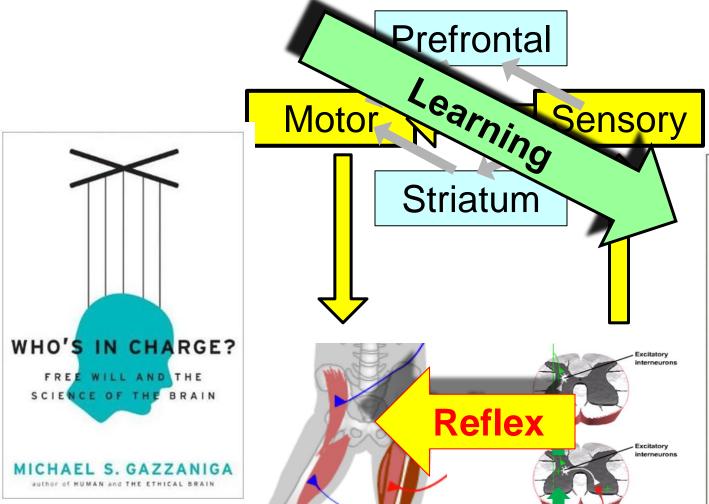
Automate

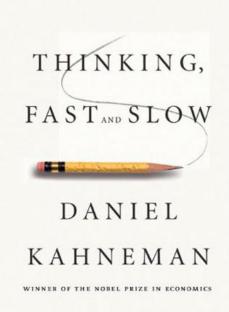


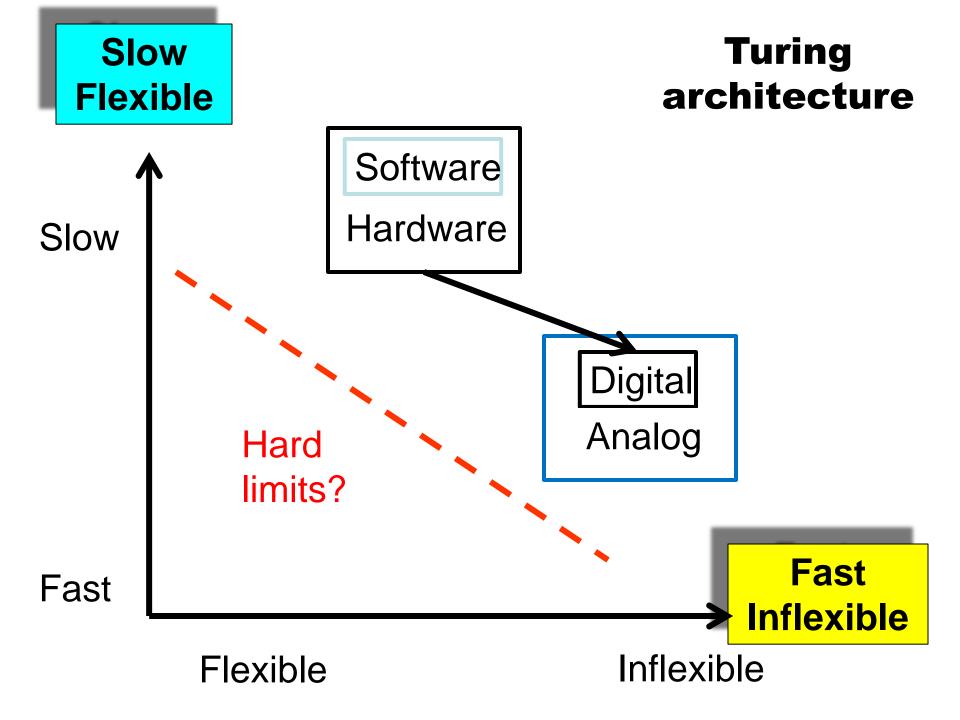


Build on Turing to show what is necessary to make this work.









Flexible

General purpose Large uncertainties Diverse problems

Solve problems Make decisions Take actions

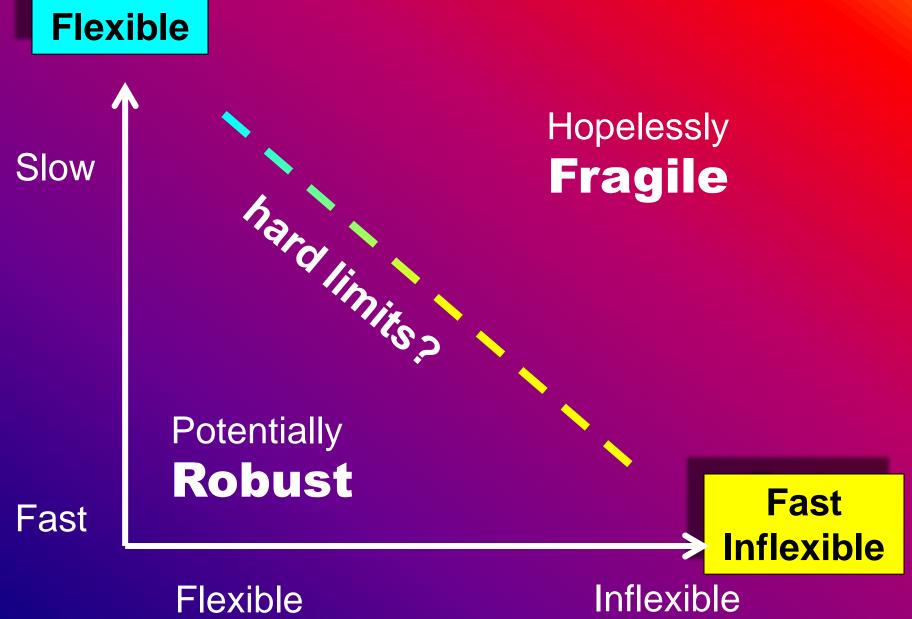
Low latency/delay

Fast

Fast

Flexible





Human complexity

Robust

- Metabolism
- © Regeneration & repair
- Healing wound /infect

Fragile

- Obesity, diabetes
- ⊗ Cancer
- ⊗ AutoImmune/Inflame

Start with physiology

Lots of triage

Benefits

Robust

- Metabolism
- Regeneration & repair
- Healing wound /infect
 - © Efficient
 - Mobility
 - Survive uncertain food supply
 - © Recover from moderate trauma and infection

Mechanism?

Robust

- Metabolism
- © Regeneration & repair
- Healing wound /infect
 - Fat accumulation
 - Insulin resistance
 - Proliferation
 - Inflammation

Fragile

- Obesity, diabetes
- ⊗ Cancer
- AutoImmune/Inflame
 - Second Fat accumulation
 - Insulin resistance
 - Proliferation
 - Inflammation

What's the difference?

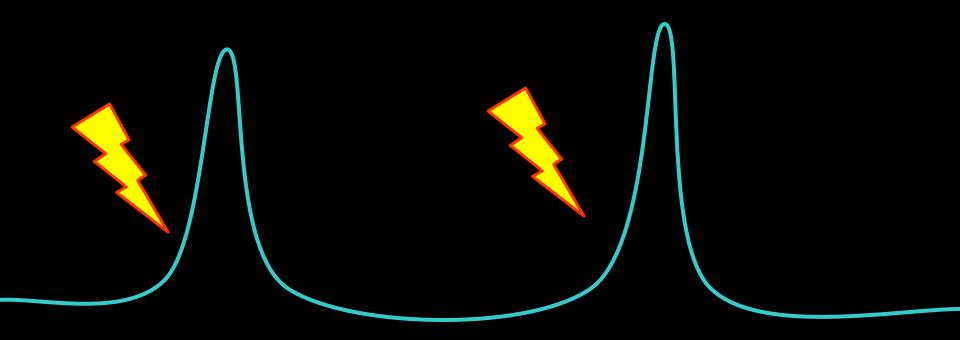
Robust Fragile

- Metabolism
- © Regeneration & repair
- Healing wound /infect

- ⊗ Obesity, diabetes
- ⊗ Cancer
- AutoImmune/Inflame
- Second Fat accumulation
- Insulin resistance
- Proliferation
- Inflammation

Controlled Dynamic

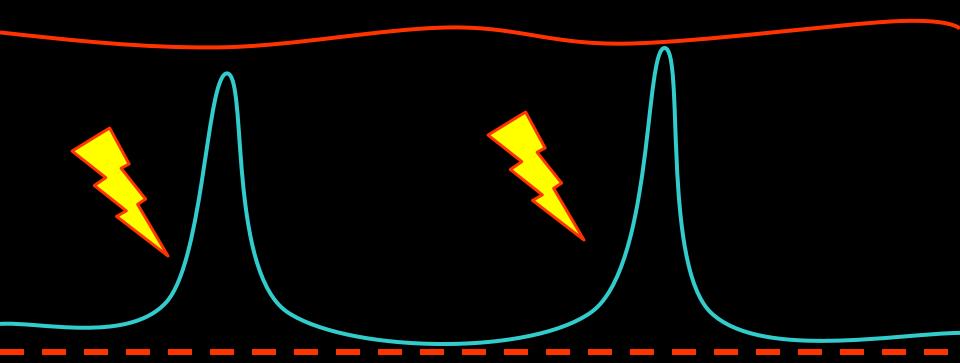
Uncontrolled Chronic



- Fat accumulation Insulin resistance
- Proliferation
- Inflammation

Controlled Dynamic

Low mean
High variability



Death

S Fat accumulation

S Insulin resistance

Proliferation

Inflammation

Controlled Dynamic

Low mean High variability

Uncontrolled Chronic

High mean Low variability

Restoring robustness?

Robust

- Metabolism
- © Regeneration & repair
- Healing wound /infect
 - ⊗ Fat accumulation
 - Solution in the second seco
 - Proliferation
 - Inflammation

Controlled Dynamic

Low mean
High variability

Fragile

- Obesity, diabetes
- Cancer
- AutoImmune/Inflame
 - S Fat accumulation
 - Insulin resistance
 - Proliferation
 - Simple strain in the strain

Uncontrolled Chronic

High mean Low variability

Human complexity

Robust

- Metabolism
- © Regeneration & repair
- Immune/inflammation
- Microbe symbionts
- Neuro-endocrine
- Complex societies
- Advanced technologies
- Risk "management"

Yet Fragile

- Obesity, diabetes
- ⊗ Cancer
- AutoImmune/Inflame
- Parasites, infection
- Addiction, psychosis,...
- Epidemics, war,...
- ► Disasters, global &!%\$#
- Obfuscate, amplify,...

Accident or necessity?

Robust Fragile

Metabolism

Obesity, diabetes

- Regenerati
- Second Fat accumulation
- Healing wc
- Insulin resistance
- Proliferation
- **®** Inflammation

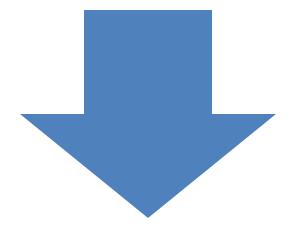
une/Inflame

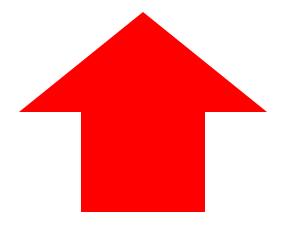
- Fragility ← Hijacking, side effects, unintended...
- Of mechanisms evolved for robustness
- Complexity ← control, robust/fragile tradeoffs
- Math: robust/fragile constraints ("conservation laws")

Both Accident or necessity?



fragile

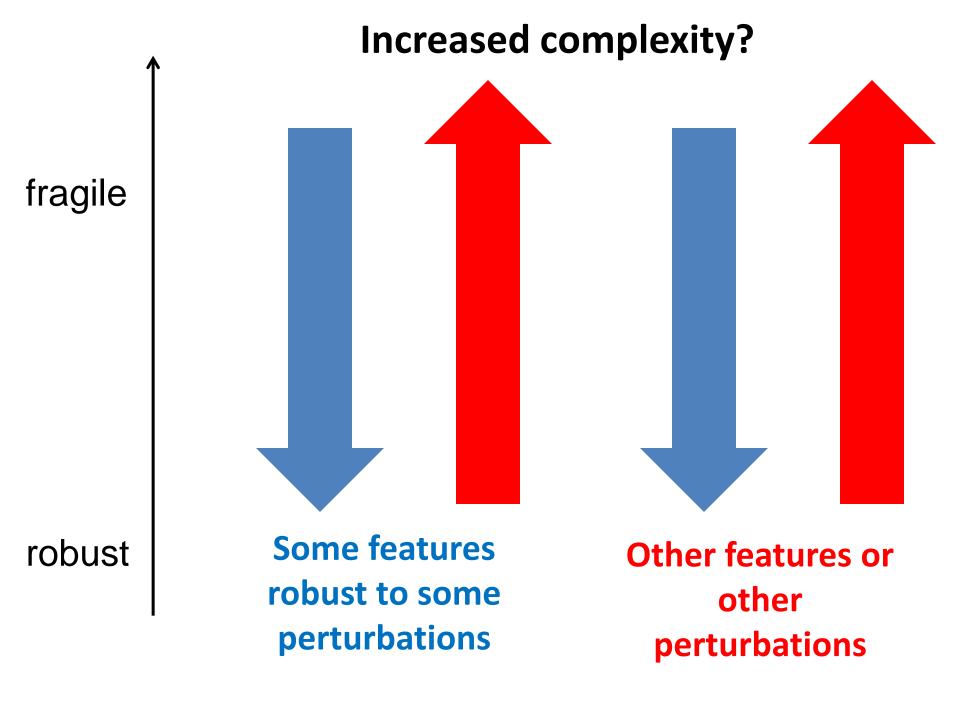




robust

Some features robust to some perturbations

Other features or other perturbations



Robust

Modular

Simple

Plastic

Evolvable

and

XOT

Fragile

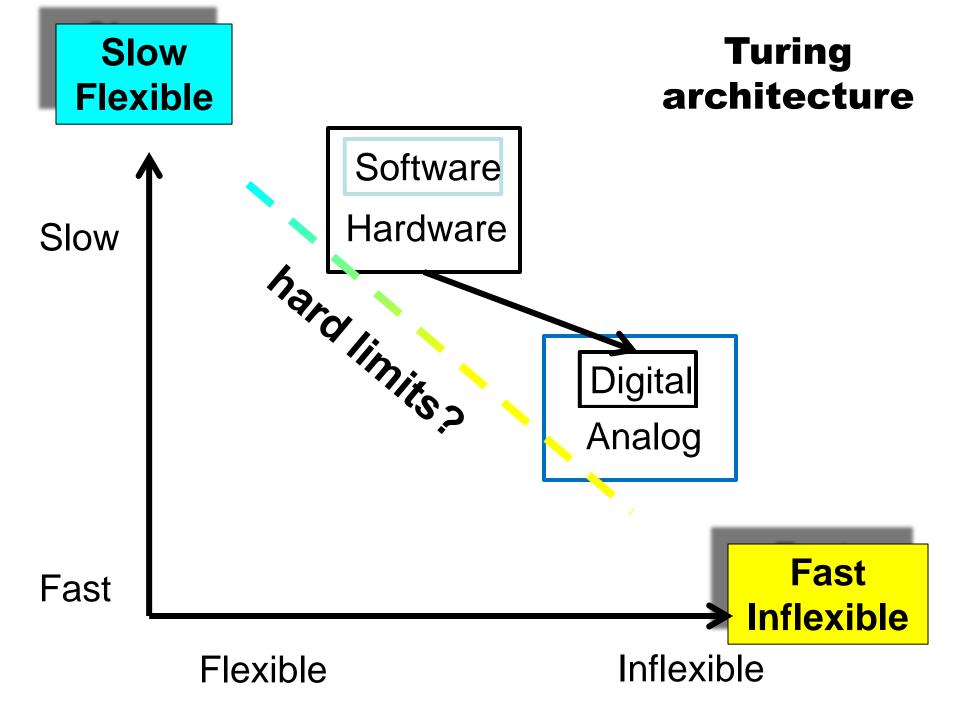
Distributed

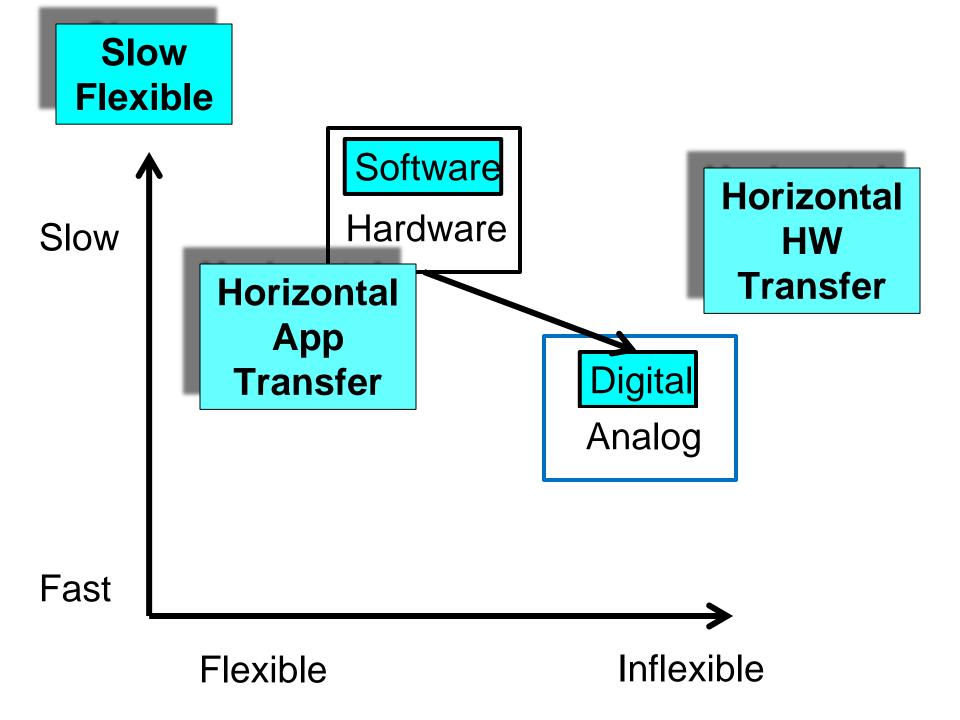
Complex

Frozen

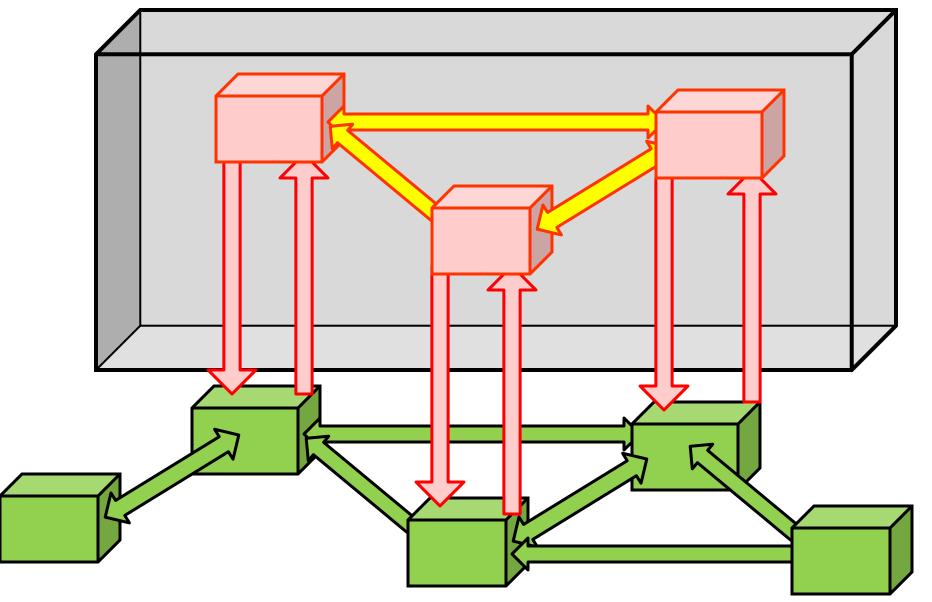
Frozen

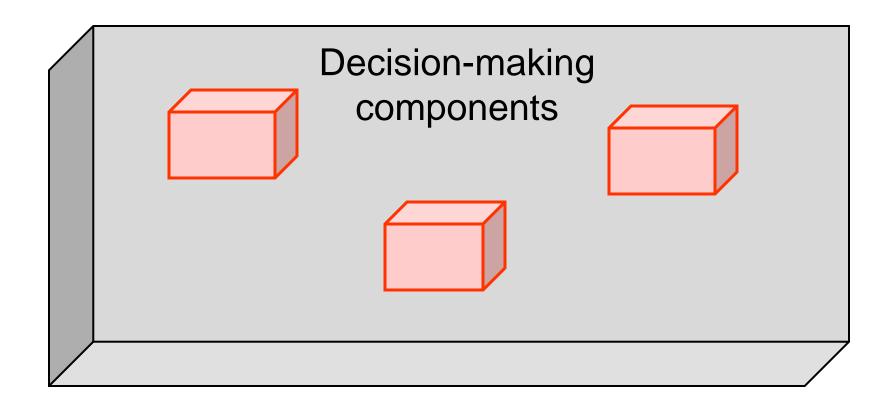




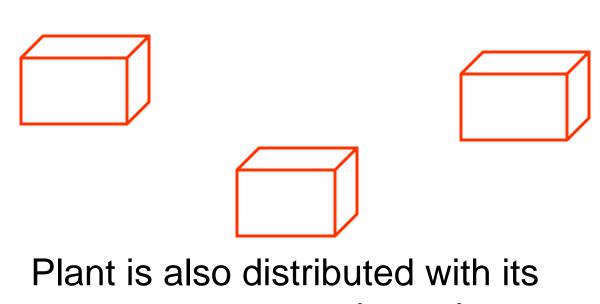


Cyber-physical: decentralized control with internal delays.

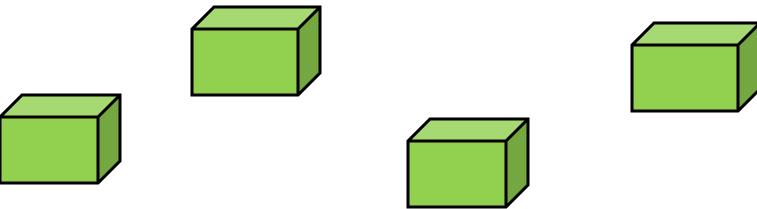




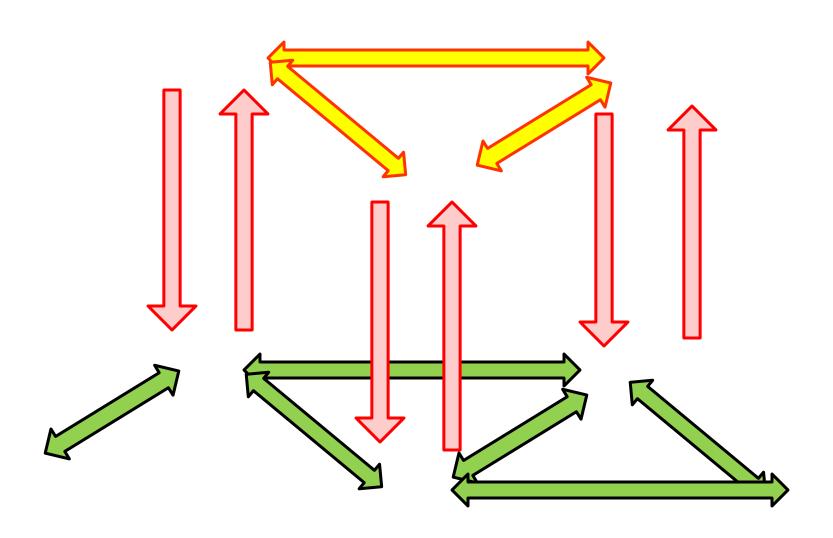
Decentralized, but initially assume computation is fast and memory is abundant.



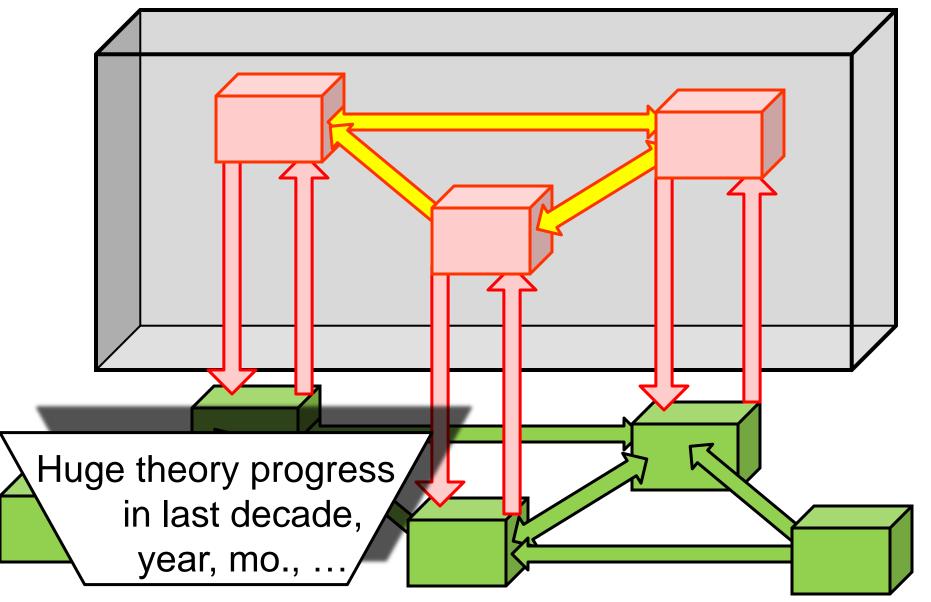




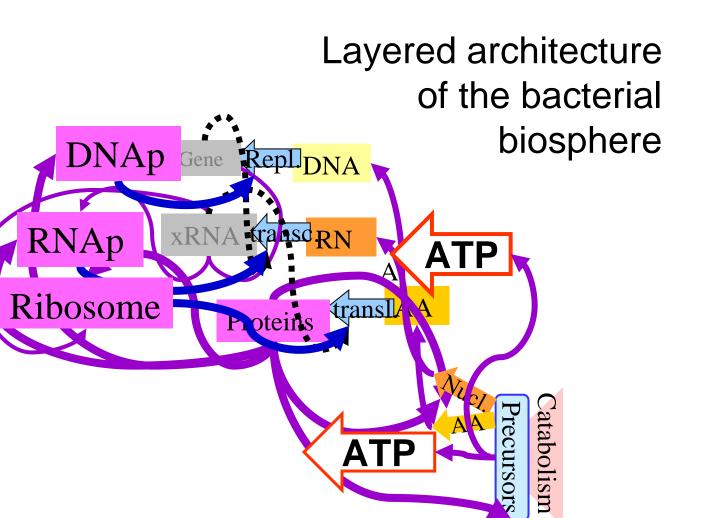
Internal delays between components, and their sensor and actuators, and also externally between plant components



Going beyond black box: control is decentralized with internal delays.



The best case study so far



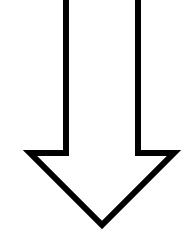
Not done here in detail, see slides elsewhere

How?

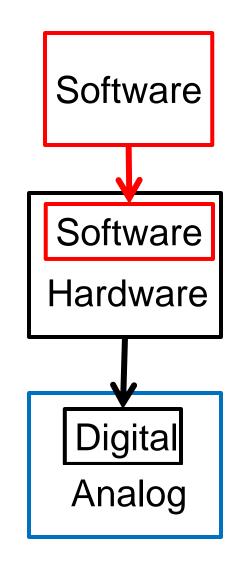
Universal architectures

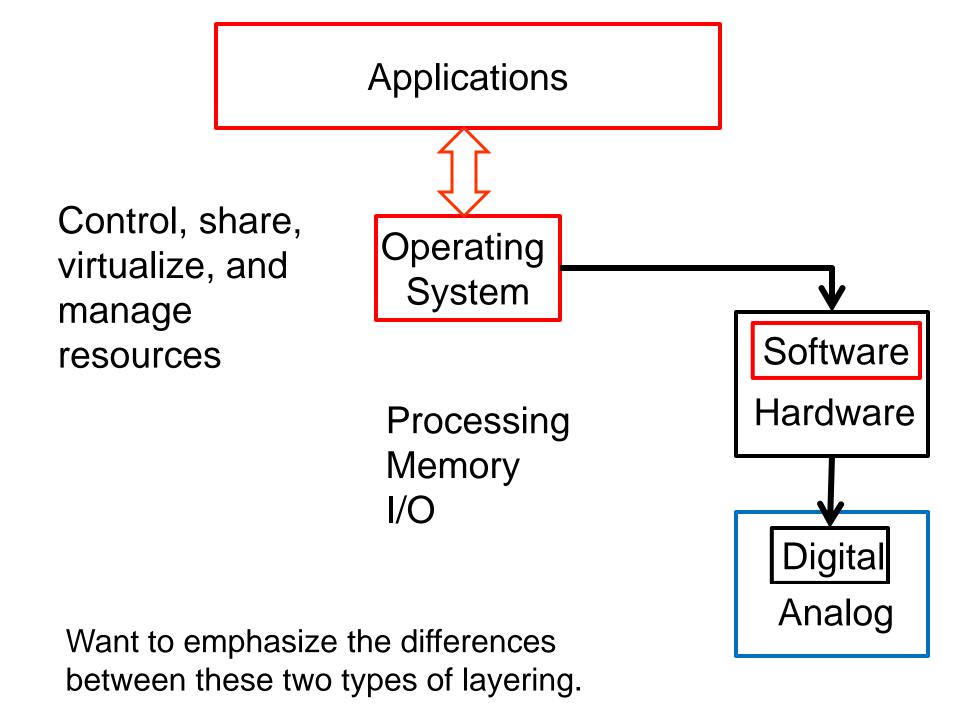
Slow execution Flexible reprogramming

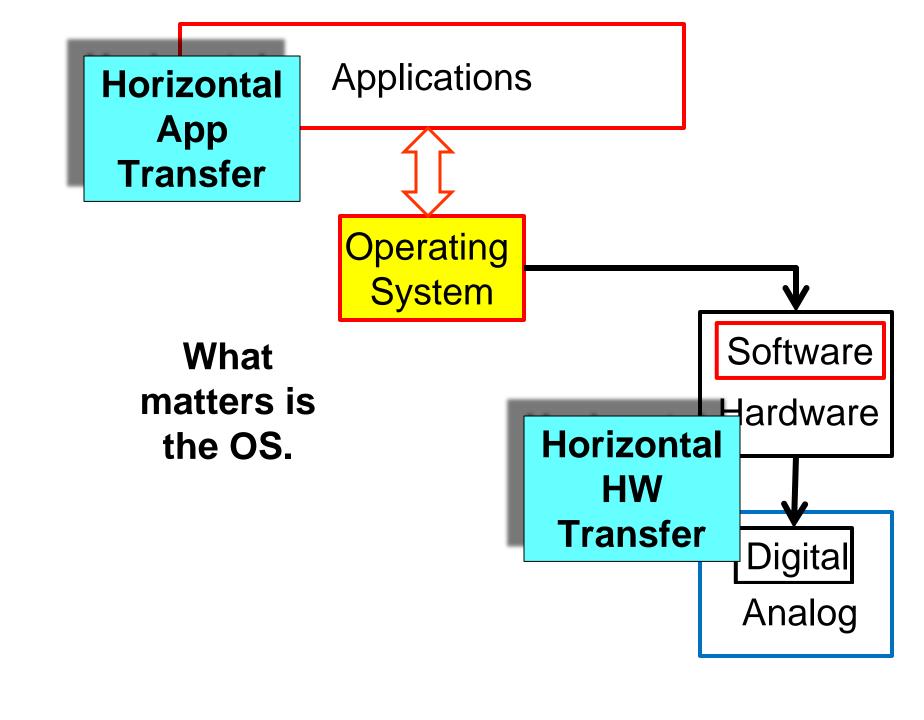
Faster execution Less flexible

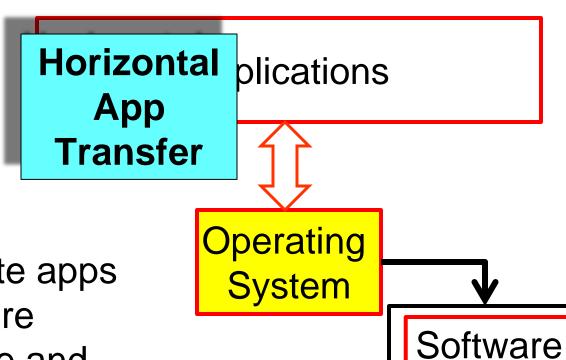


Modern technology gives lots of intermediate alternatives.









Hardware

Analog

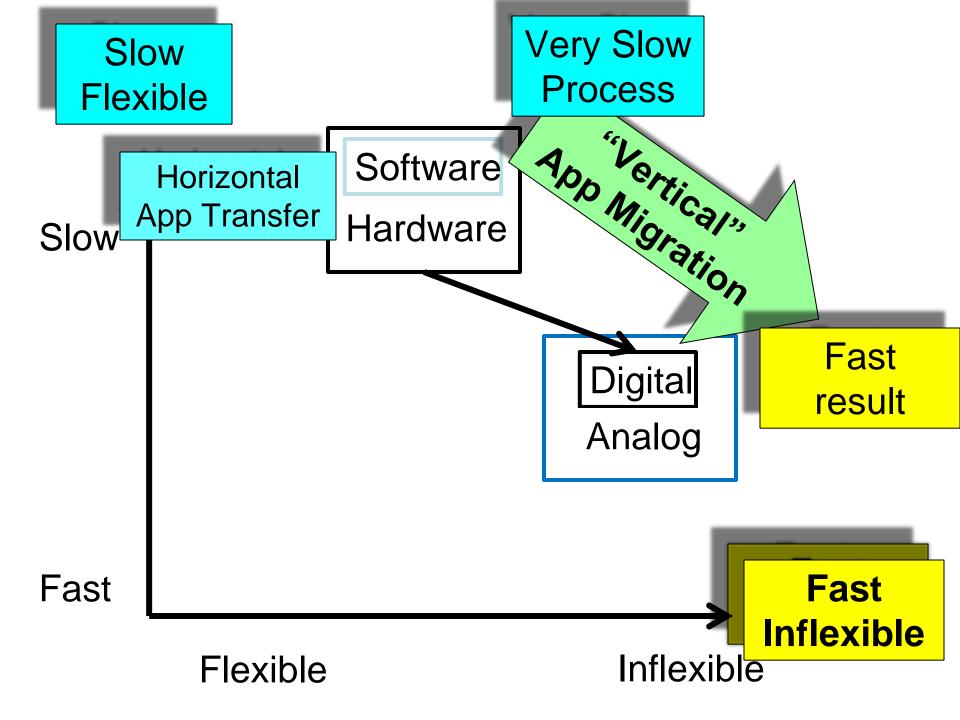
tal

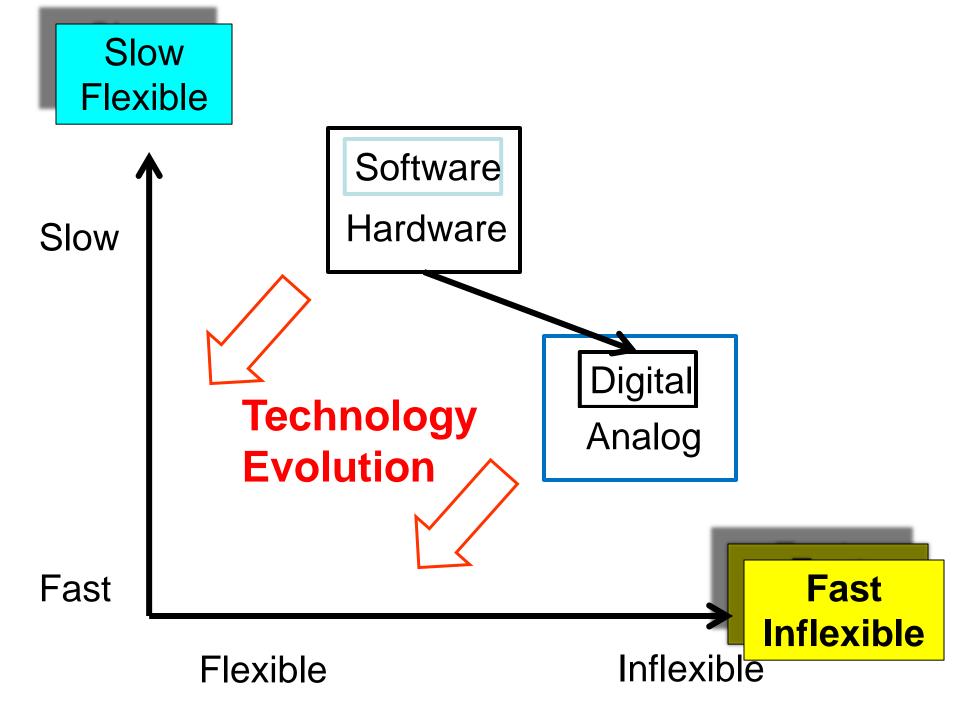
Horizontal

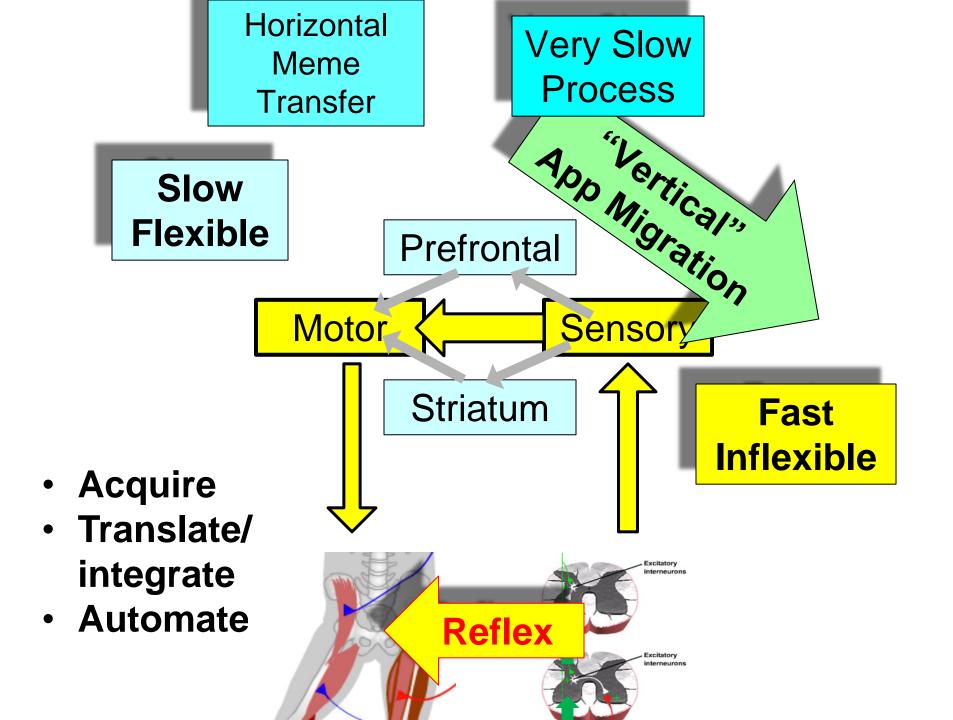
HW

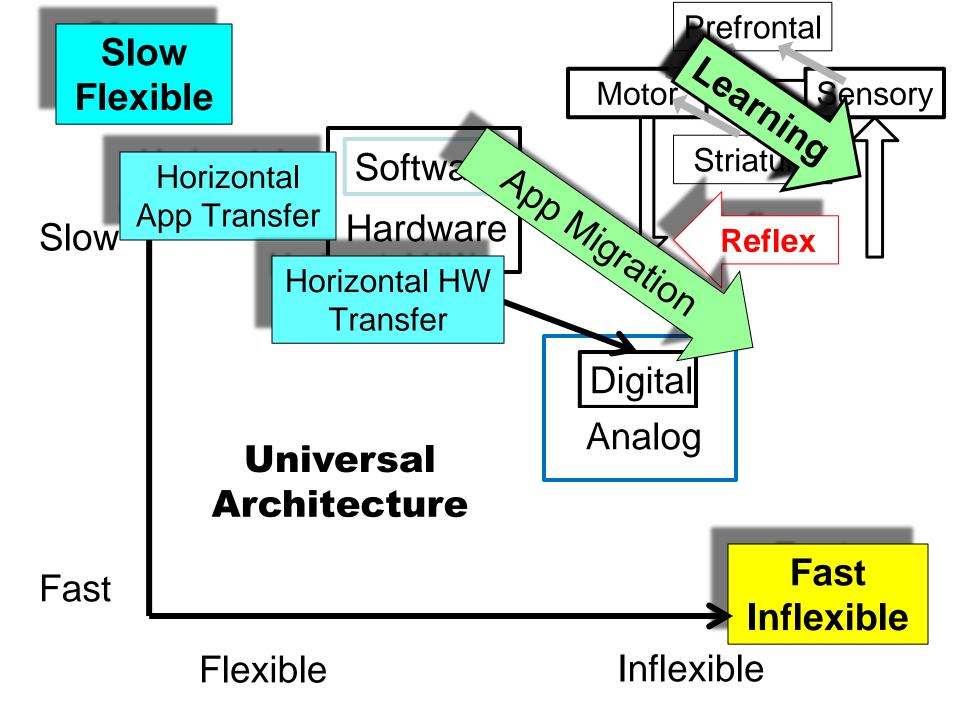
Transfer

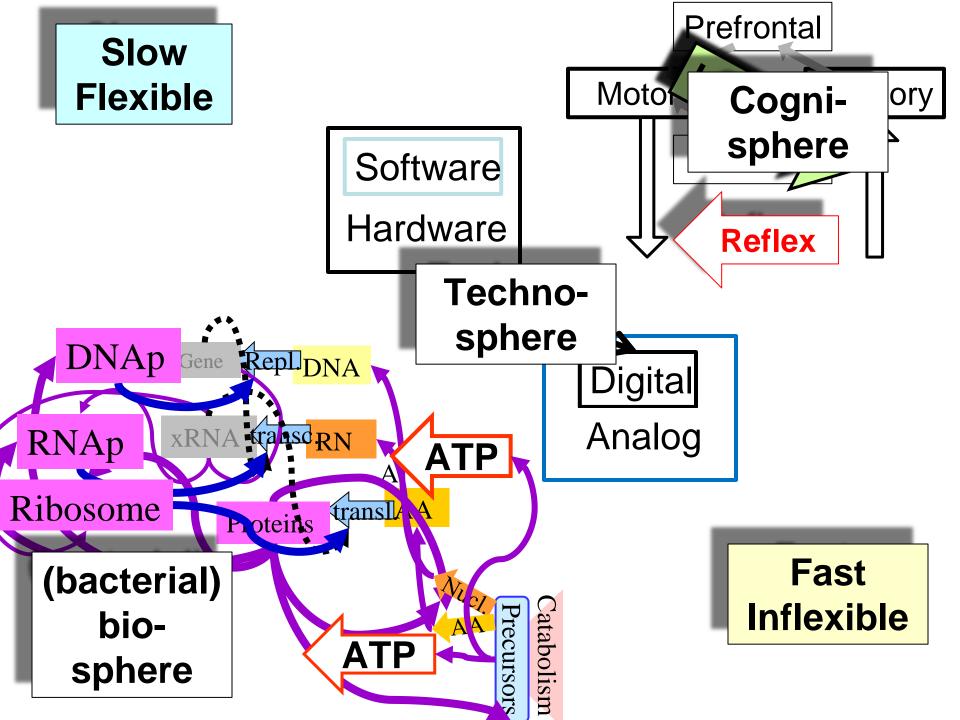
- Some people write apps and build hardware
- But most software and hardware is acquired by "horizontal" transfer from others
- Similarly, most new ideas (humans) and new genes (bacteria) are acquired horizontally

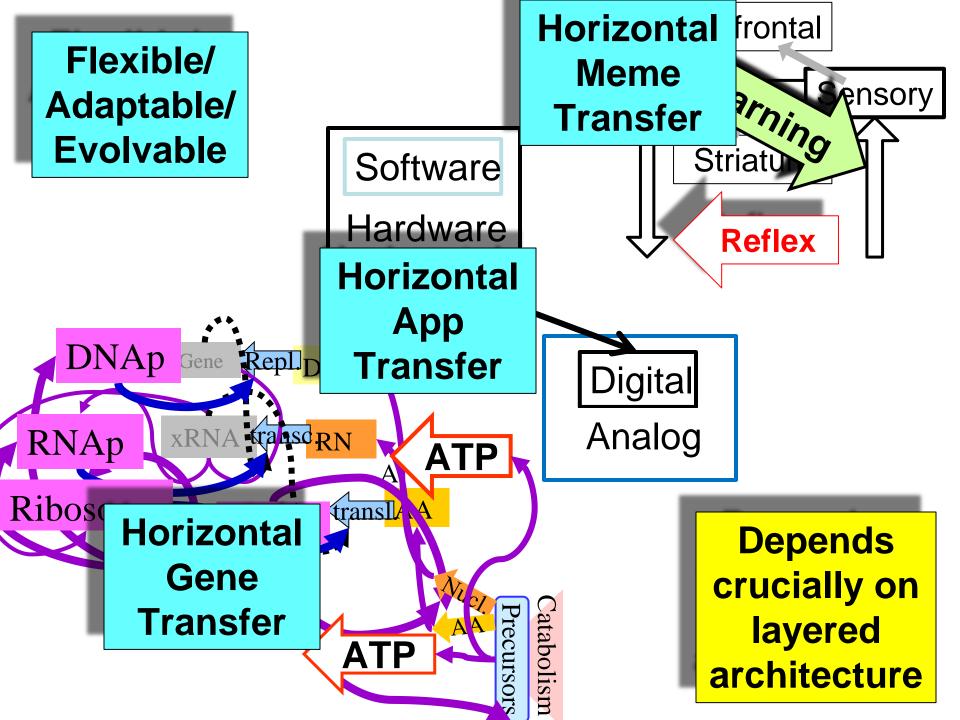












Horizontal Meme Transfer

Horizontal App Transfer

Horizontal Gene Transfer

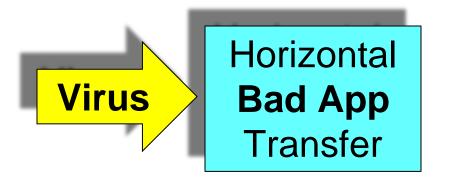
Most

- software and hardware
- new ideas (humans)
- new genes (bacteria)

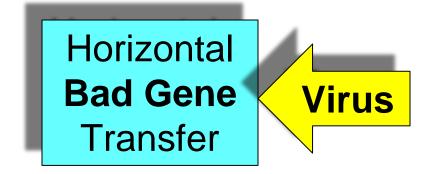
is acquired by "horizontal" transfer, though sometimes it is evolved locally

Exploiting layered architecture

Horizontal **Bad Meme**Transfer



Fragility?



Parasites & Hijacking

Depends crucially on layered architecture

Build on Turing to show what is *necessary* to make this work.

Horizontal Meme Transfer

- Acquire
- Translate/ integrate
- Automate

Horizontal Gene Transfer Horizontal
App
Transfer

Amazingly Flexible/ Adaptable

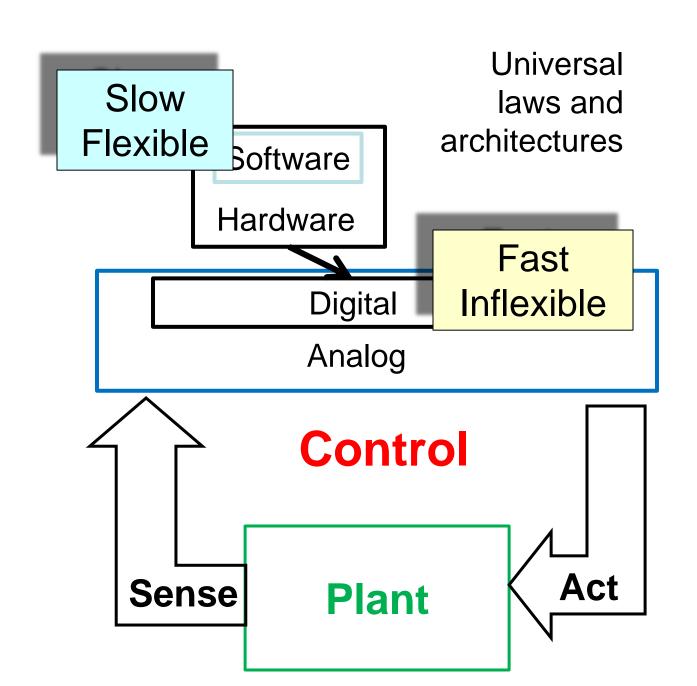
Compute

Turing

Delay is even more important

Bode

Control

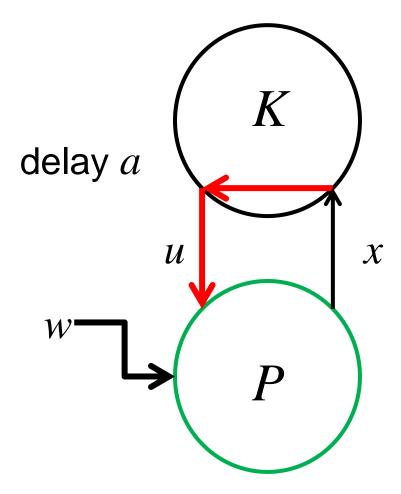


Compute

Turing

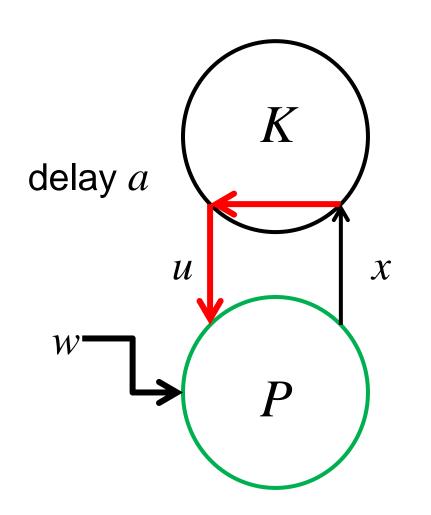
Why

Necessity



$$x_{t+1} = px_t + w_t + u_{t-a}$$

delay a



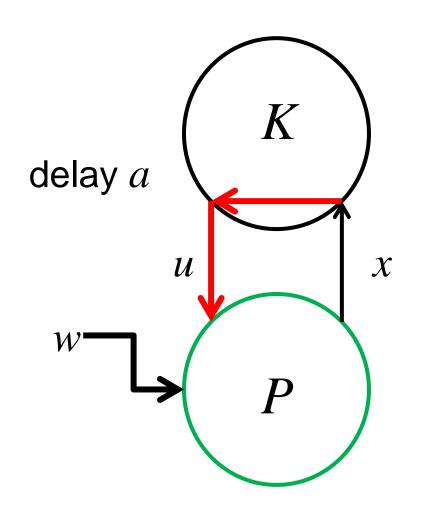
No delay or no uncertainty

$$u_{t-a} = -(px_t + w_t)$$

$$\Rightarrow ||x|| \approx 0 \quad ||u|| \approx ||w||$$

$$x_{t+1} = px_t + w_t + u_{t-a}$$

$$p > 1$$



$$x_{t+1} = px_t + w_t + u_{t-a}$$
$$p > 1$$

No delay or no uncertainty

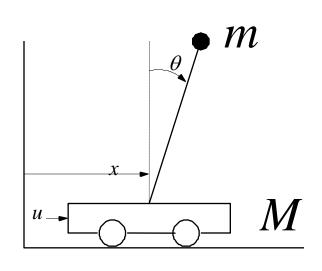
$$u_{t-a} = -(px_t + w_t)$$

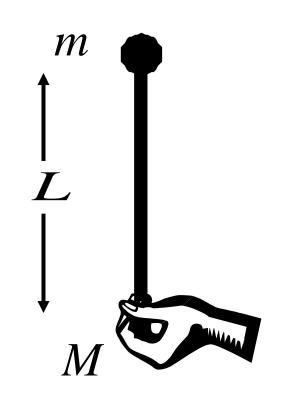
$$\Rightarrow ||x|| \approx 0 \quad ||u|| \approx ||w||$$

With delay *and* uncertainty

$$\Rightarrow \|x\| \approx \|u\| \approx p^a \|w\|$$

Linearized pendulum on a cart





$$\frac{d}{dt} \begin{bmatrix} x \\ \theta \\ \dot{x} \\ \dot{\theta} \end{bmatrix} = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & \frac{m^2 g l^2}{q} & \frac{-(J+ml^2)b}{q} & 0 \\ 0 & \frac{mgl(M+m)}{q} & \frac{-mlb}{q} & 0 \end{bmatrix} x + \begin{bmatrix} 0 \\ 0 \\ J+ml^2 \\ \frac{ml}{q} \end{bmatrix} u$$

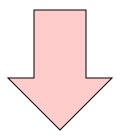
$$q = J(M+m) + Mml^2$$

$$(M + m)\ddot{x} + ml(\ddot{\theta}\cos\theta - \dot{\theta}^2\sin\theta) = u$$

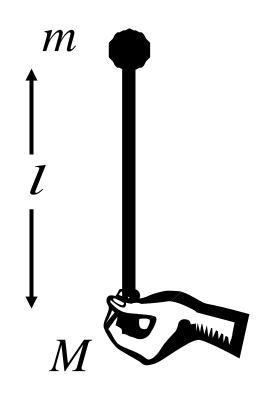
$$\ddot{x}\cos\theta + l\ddot{\theta} + g\sin\theta = 0$$

$$y = x + \alpha l\sin\theta$$



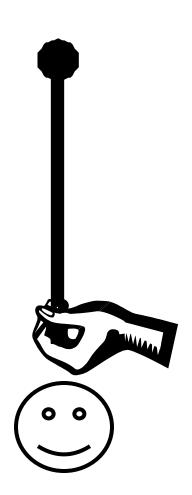


$$(M + m)\ddot{x} + ml\ddot{\theta} = u$$
$$\ddot{x} + l\ddot{\theta} \pm g\theta = 0$$
$$y = x + \alpha l\theta$$



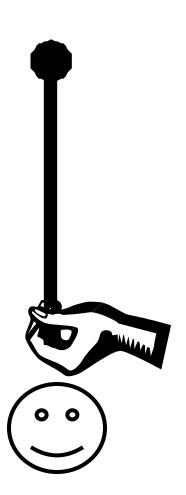
Robust =agile and balancing

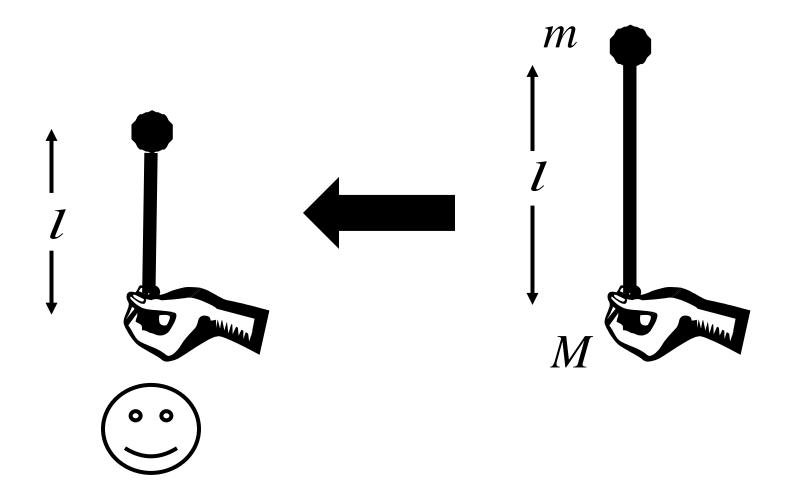




Robust =agile and balancing







Efficient=length of pendulum (artificial)

$$\begin{bmatrix} x \\ \theta \end{bmatrix} = \frac{1}{D(s)} \begin{bmatrix} ls^2 \pm g \\ -s^2 \end{bmatrix} u$$

$$D(s) = s^{2} (Mls^{2} \pm (M + m)g)$$

$$y = x + \alpha l\theta = \frac{\varepsilon l s^2 \pm g}{D(s)}$$

$$\varepsilon = 1 - \alpha$$

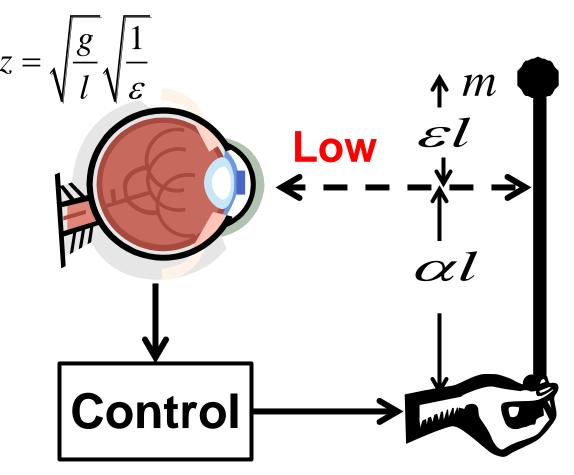
$$p = \sqrt{\frac{g}{l}}\sqrt{1+r} \quad r = \frac{m}{M} \quad z = \sqrt{\frac{g}{l}}\sqrt{\frac{1}{\varepsilon}}$$

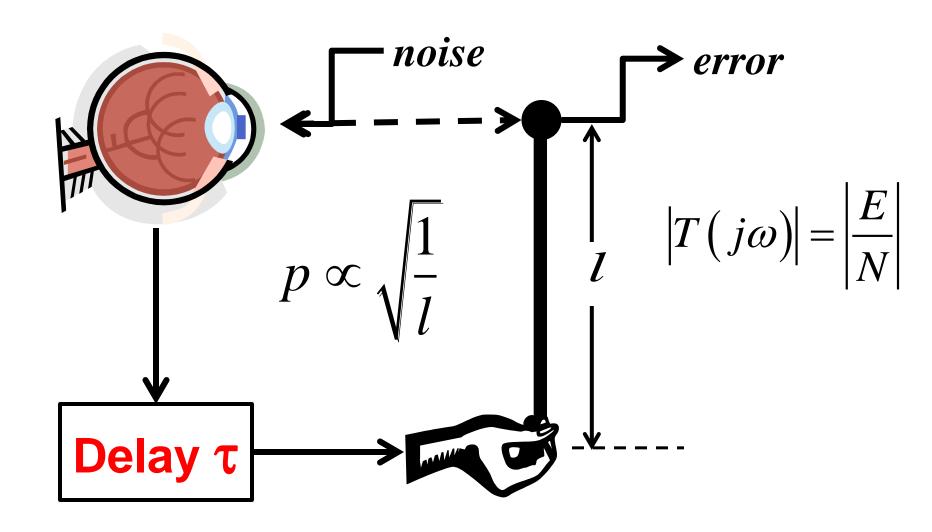


$$(M+m)\ddot{x}+ml\ddot{\theta}=u$$

$$\ddot{x} + l\ddot{\theta} \pm g\theta = 0$$

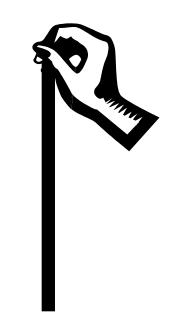
$$y = x + \alpha l\theta$$







$$\frac{1}{\pi} \int_{0}^{\infty} \ln |T(j\omega)| d\omega \ge 0$$

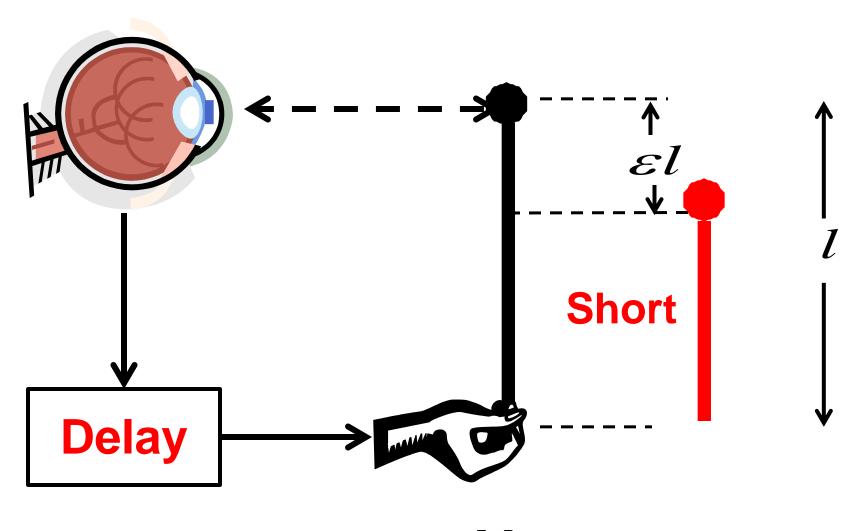


Easy, even with eyes closed No matter what the length

Proof: Standard UG control theory:

Easy calculus, easier contour integral,
easiest Poisson Integral formula

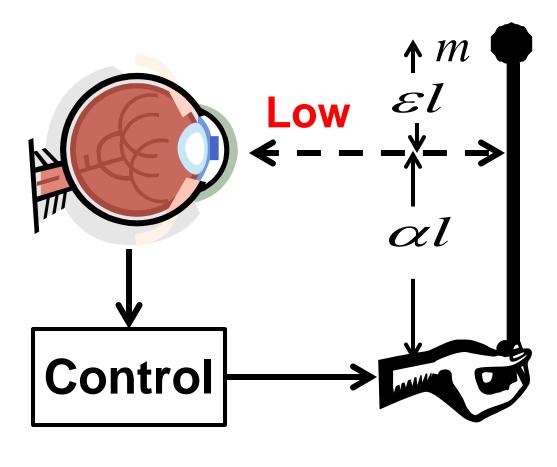
Harder if delayed or short



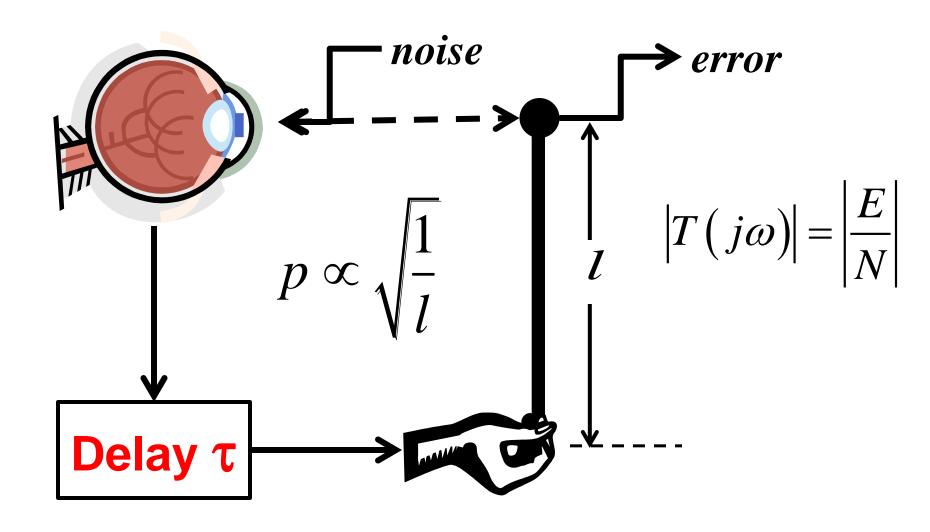
M

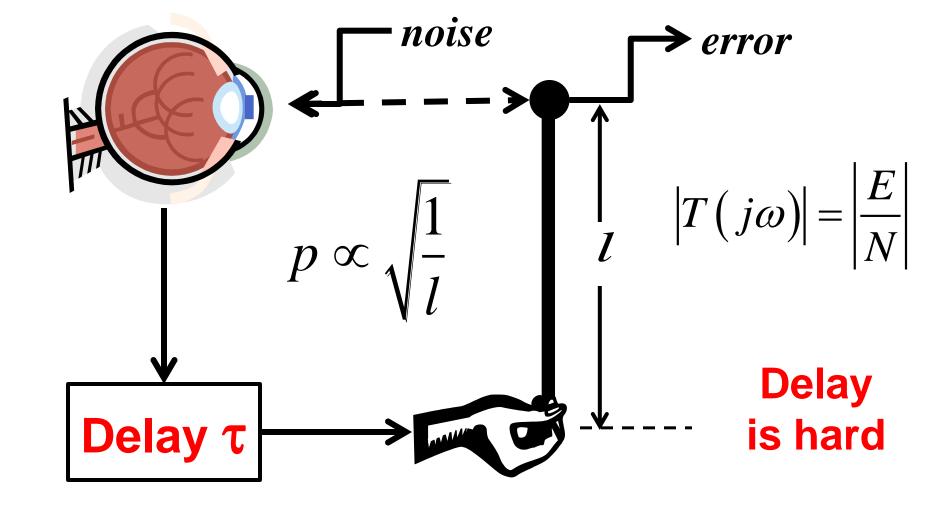
Also harder if sensed low

$$r = \frac{m}{M}$$

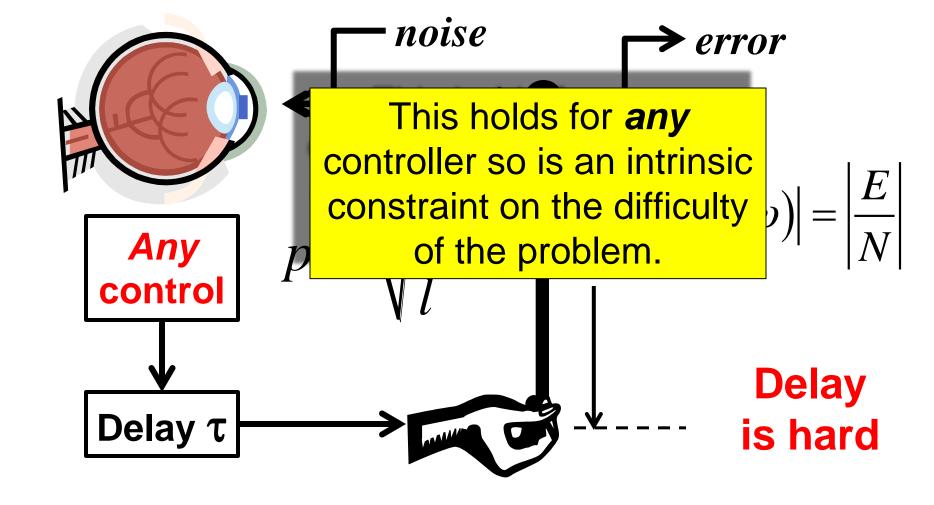








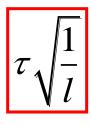
$$\frac{1}{\pi} \int_{0}^{\infty} \ln |T(j\omega)| \frac{2p}{p^{2} + \omega^{2}} d\omega \ge \ln |T_{mp}(p)| = p\tau \propto \tau \sqrt{\frac{1}{l}}$$

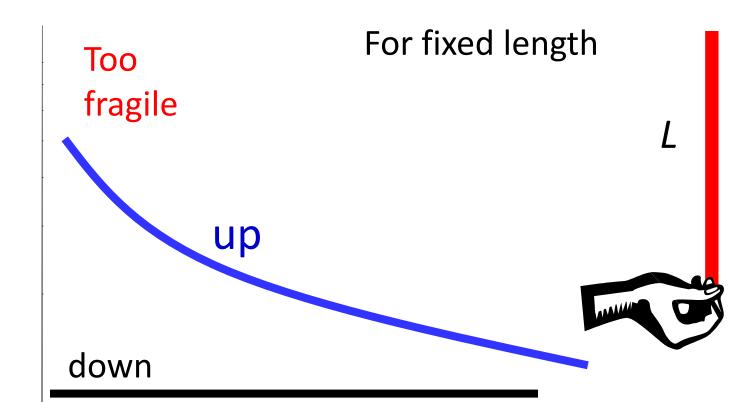


$$\frac{1}{\pi} \int_{0}^{\infty} \ln |T(j\omega)| \frac{2p}{p^{2} + \omega^{2}} d\omega \ge \ln |T_{mp}(p)| = p\tau \propto \tau \sqrt{\frac{1}{l}}$$

$$\frac{1}{\pi} \int_{0}^{\infty} \ln |T(j\omega)| \frac{2p}{p^{2} + \omega^{2}} d\omega \ge p\tau \propto \tau \sqrt{\frac{1}{l}}$$

Fragility





large τ small 1/τ small τ large 1/τ

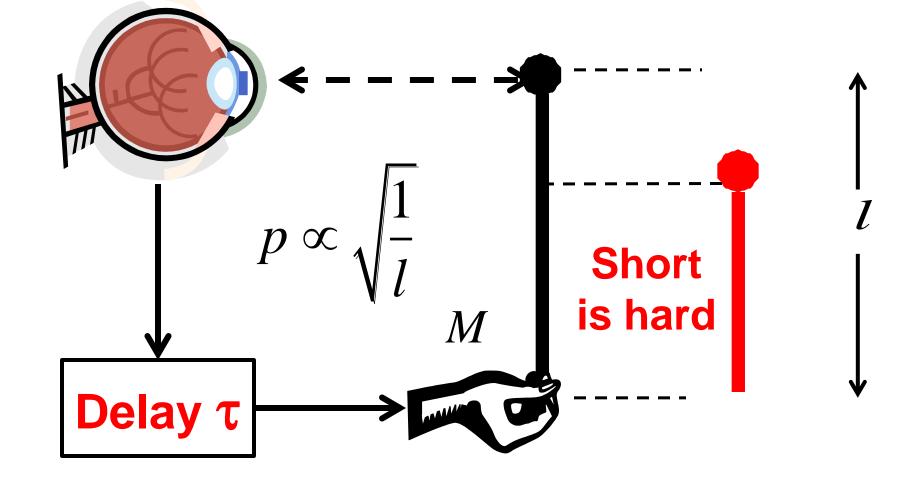
1/delay

$$\frac{1}{\pi} \int_{0}^{\infty} \ln |T(j\omega)| \frac{2p}{p^{2} + \omega^{2}} d\omega \ge p\tau \propto \tau \sqrt{\frac{1}{l}}$$

We would like to tolerate large delays (and small lengths), but large delays severely constrain the achievable robustness.

large τ small $1/\tau$

small τ large $1/\tau$



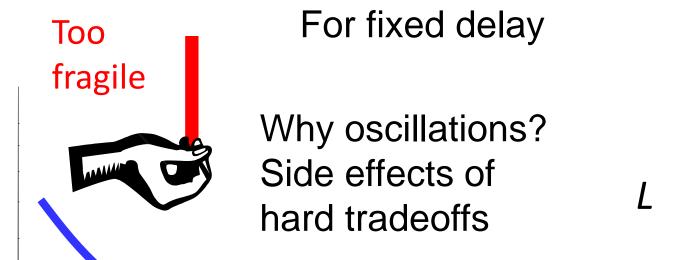
$$\frac{1}{\pi} \int_{0}^{\infty} \ln |T(j\omega)| \frac{2p}{p^{2} + \omega^{2}} d\omega \ge \ln |T_{mp}(p)| = p\tau \propto \tau \sqrt{\frac{1}{l}}$$

$$\frac{1}{\pi} \int_{0}^{\infty} \ln |T(j\omega)| \frac{2p}{p^{2} + \omega^{2}} d\omega \ge \ln |T_{mp}(p)| = p\tau \propto \tau \sqrt{\frac{1}{l}}$$

Fragility

$$p \propto \sqrt{\frac{1}{l}}$$

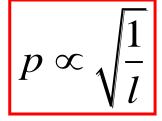
down

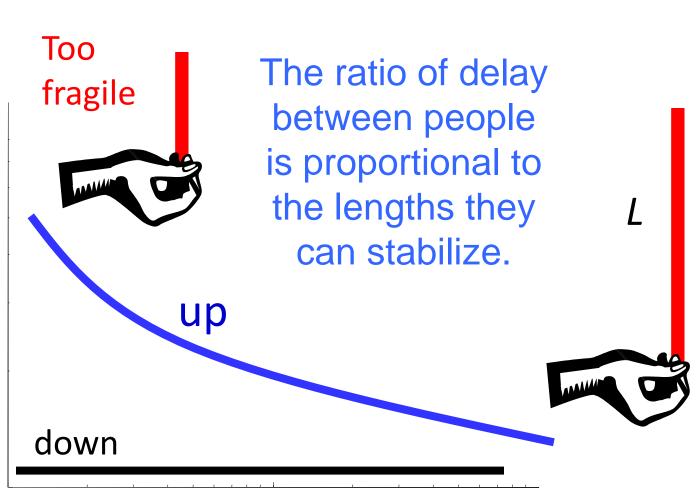


lenath

$$\frac{1}{\pi} \int_{0}^{\infty} \ln |T(j\omega)| \frac{2p}{p^{2} + \omega^{2}} d\omega \ge \ln |T_{mp}(p)| = p\tau \propto \tau \sqrt{\frac{1}{l}}$$

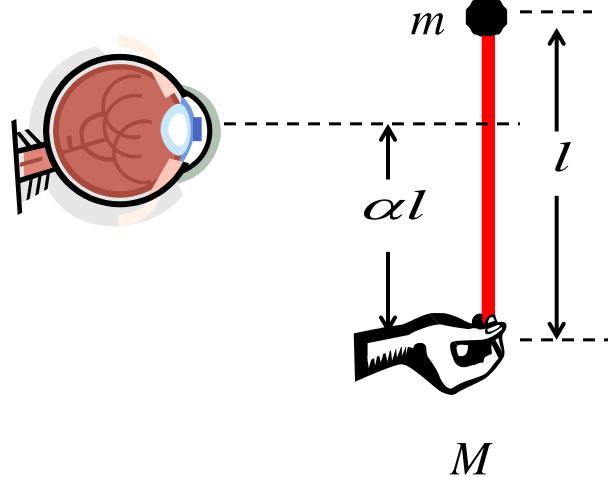






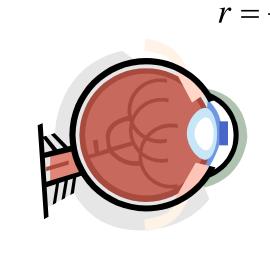
length L

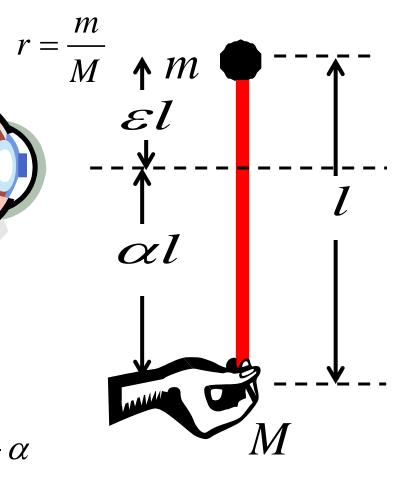
Eyes moved down is harder (RHP zero) Similar to delay



Suppose
$$r = \frac{m}{M} << 1$$

Units $\Rightarrow M = g = 1$





$$y = x + \alpha l\theta = \frac{\varepsilon l s^2 \pm g}{s^2 (l s^2 \pm g)} \qquad \varepsilon = 1 - \alpha$$

$$p \approx \sqrt{\frac{g}{l}} \qquad z = \sqrt{\frac{g}{l}} \sqrt{\frac{1}{\varepsilon}} \Rightarrow \frac{z + p}{z - p} = \frac{1 + \sqrt{\varepsilon}}{1 - \sqrt{\varepsilon}}$$

Compare

$$p = \sqrt{\frac{g}{l(1-\varepsilon)}} \sqrt{1+r} = p_0 \sqrt{\frac{1}{(1-\varepsilon)}} \approx p_0 \left(1 + \frac{\varepsilon}{2}\right)$$

Move eyes

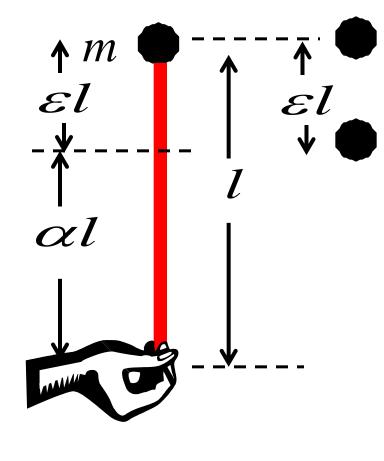
$$p = \sqrt{\frac{g}{l}}\sqrt{1+r} \quad r = \frac{m}{M} \quad z = \sqrt{\frac{g}{l}}\sqrt{\frac{1}{\varepsilon}}$$

$$p = z \Rightarrow 1+r = \frac{1}{\varepsilon} \Rightarrow \varepsilon = \frac{1}{1+r}$$

$$p\left(1+\frac{1}{3}\frac{p^2}{z^2}\right) = \sqrt{\frac{g}{l}}\sqrt{1+r}\left(1+\frac{1}{3}\varepsilon\right) = p\left(1+\frac{\varepsilon}{3}\right)$$

$$= p\left(1+\frac{1-\alpha}{3}\right)$$

$$r = \frac{m}{M}$$



M

$$\frac{1}{\pi} \int_{0}^{\infty} \ln |T(j\omega)| \left(\frac{2p}{p^{2} + \omega^{2}}\right) d\omega \ge \ln \left|\frac{z + p}{z - p}\right|$$

$$\varepsilon = \frac{1}{1 + r}$$

$$\ln \left|\frac{z + p}{z - p}\right|$$

$$\frac{z + p}{z - p} = \frac{1 + \sqrt{\varepsilon}}{1 - \sqrt{\varepsilon}}$$

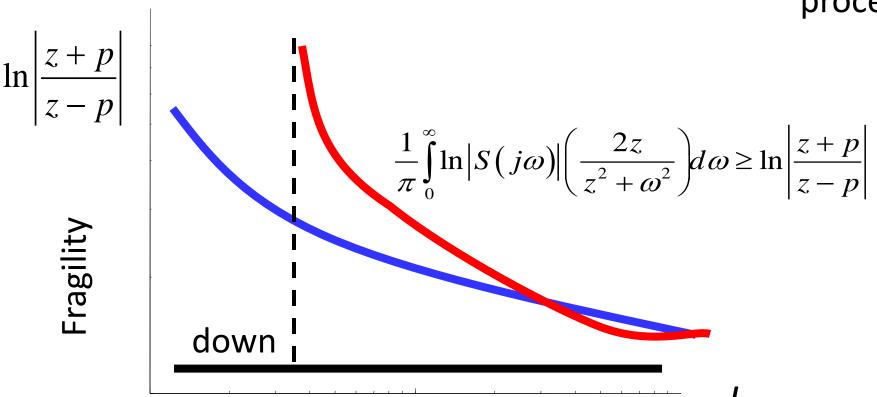
$$\frac{change}{down}$$

$$\frac{sense}{down}$$
This is a cartoon, but can be made precise.

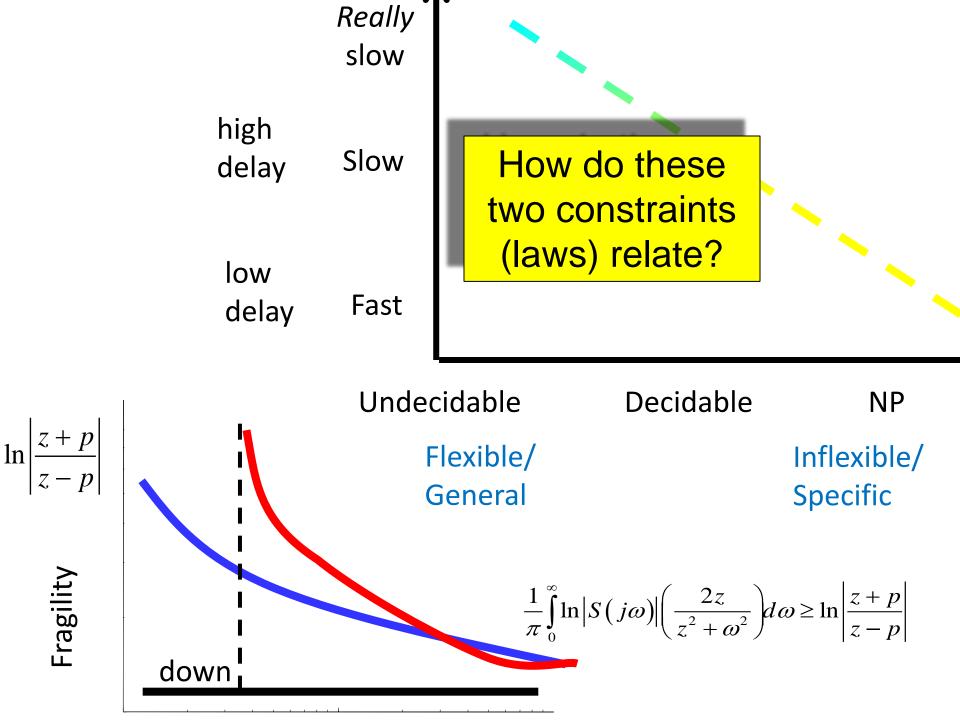
 $\frac{1}{\pi} \int_{0}^{\infty} \ln |S(j\omega)| \left(\frac{2z}{z^{2} + \omega^{2}}\right) d\omega \ge \ln \left|\frac{z + p}{z - p}\right|$

Hard limits on the *intrinsic* robustness of control *problems*.

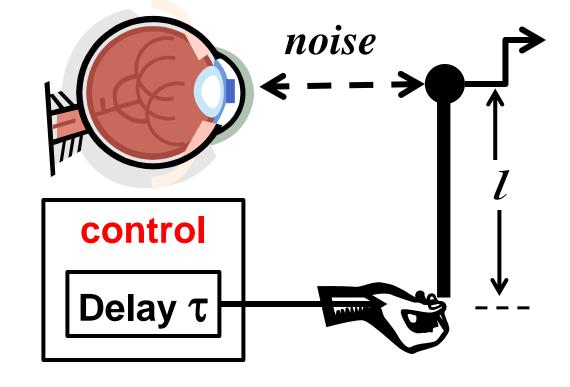
Must (and do) have algorithms that achieve the limits, and architectures that support this process.



This is a cartoon, but can be made precise.



Delay comes from sensing, communications, computing, and actuation.
Delay limits robust performance.

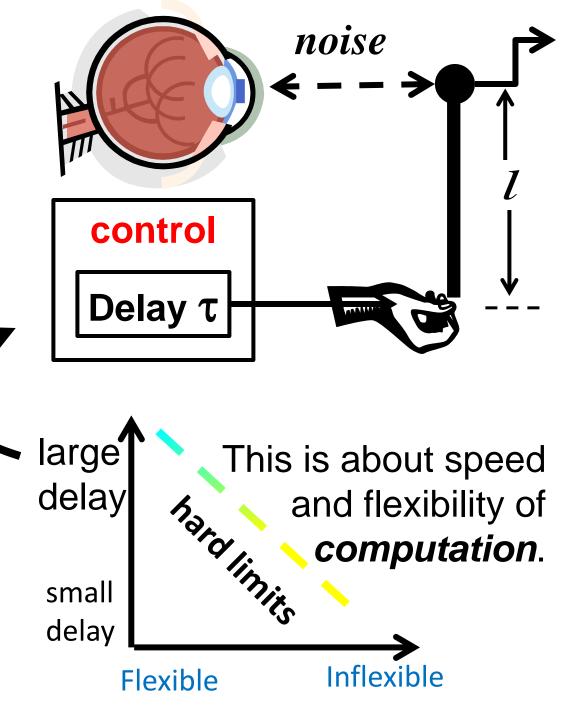


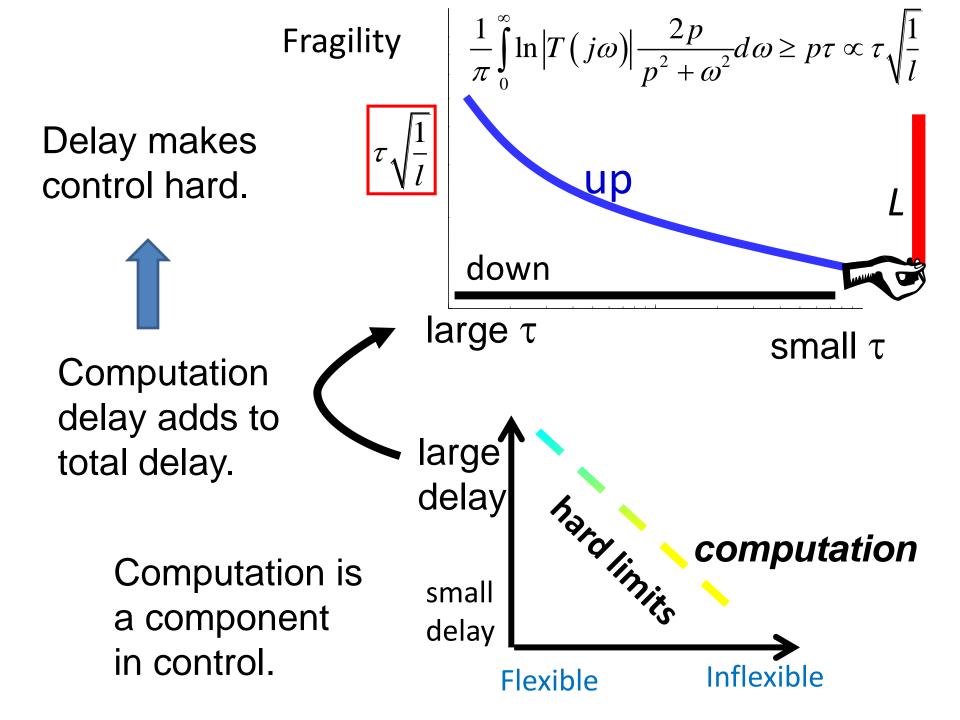
$$\frac{1}{\pi} \int_{0}^{\infty} \ln |T(j\omega)| \frac{2p}{p^{2} + \omega^{2}} d\omega \ge \ln |T_{mp}(p)| = p\tau \propto \tau \sqrt{\frac{1}{l}}$$

How do these two constraints (laws) relate?

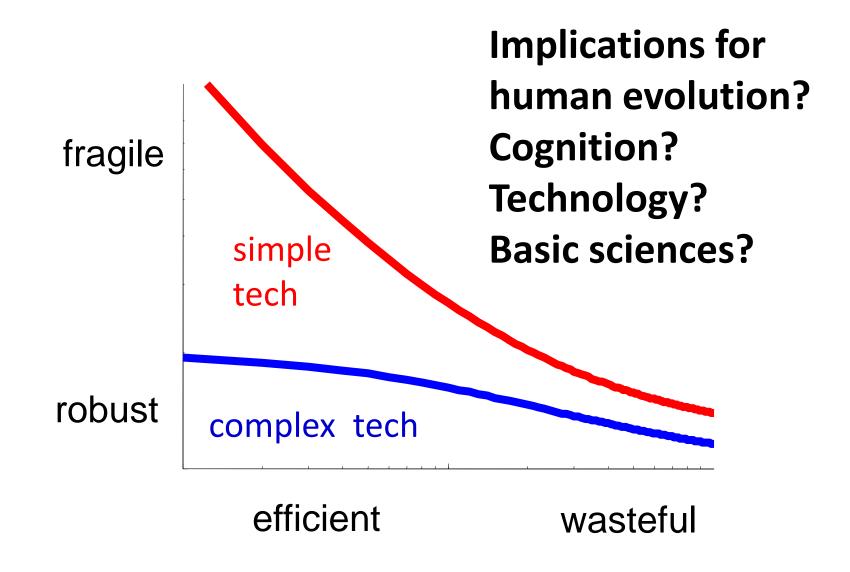
Computation delay adds to total delay.

Computation is a component in control.





How general is this picture?



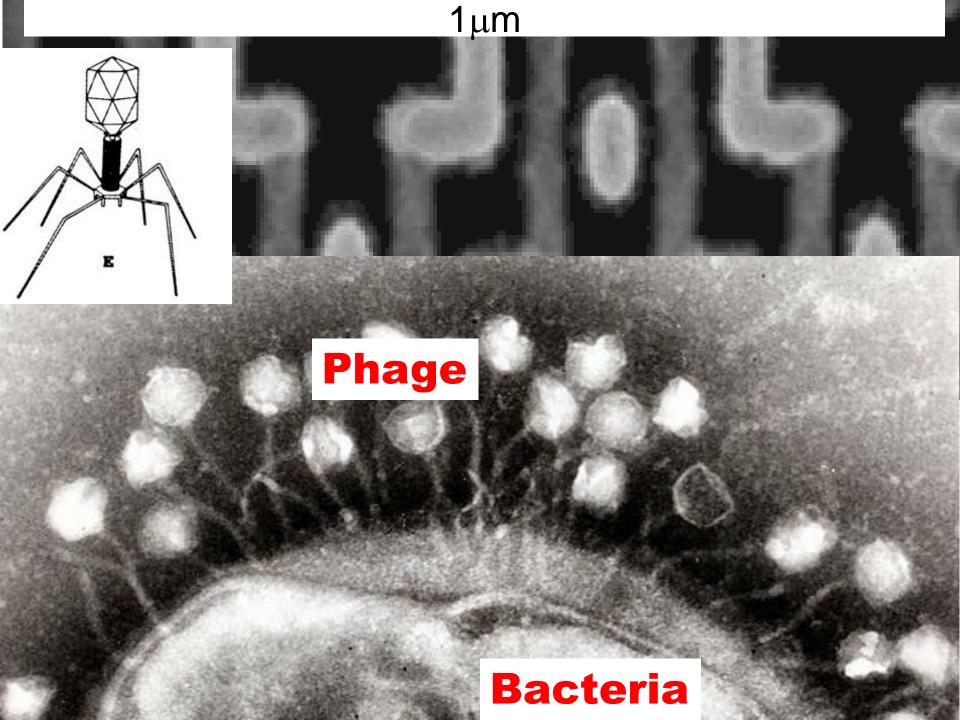
Viruses' Life History: Towards a Mechanistic Basis of a Trade-Off between Survival and Reproduction among Phages

Marianne De Paepe, François Taddei*

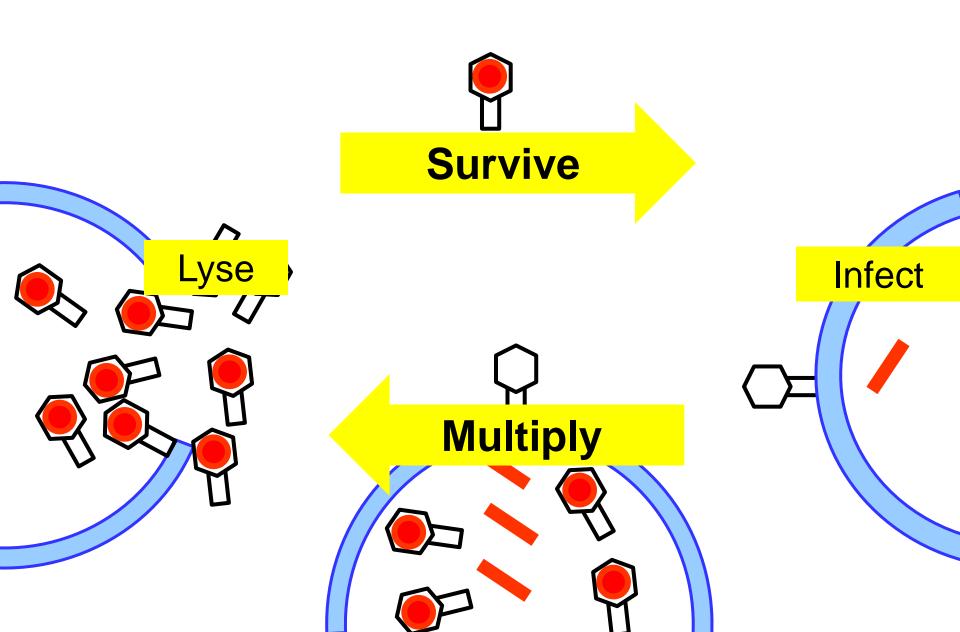
Laboratoire de Genetique Moleculaire, Evolutive et Medicale, University of Paris 5, INSERM, Paris, France

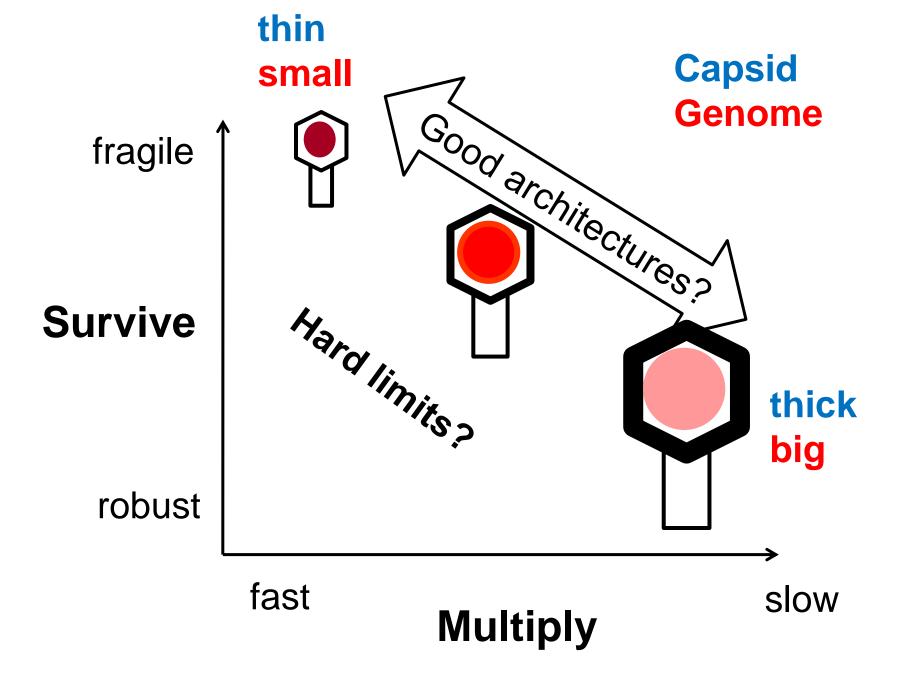
July 2006 | Volume 4 | Issue 7 | e193

I recently found this paper, a rare example of exploring an explicit tradeoff between robustness and efficiency. This seems like an important paper but it is rarely cited.



Phage lifecycle





RESEARCH ARTICLES

Glycolytic Oscillations and Limits on Robust Efficiency

Fiona A. Chandra, 1* Gentian Buzi, 2 John C. Doyle 2

Both engineering and evolution are constrained by trade-offs between efficiency and robustness, but theory that formalizes this fact is limited. For a simple two-state model of glycolysis, we explicitly derive analytic equations for hard trade-offs between robustness and efficiency with oscillations as an inevitable side effect. The model describes how the trade-offs arise from individual parameters, including the interplay of feedback control with autocatalysis of network products necessary to power and catalyze intermediate reactions. We then use control theory to prove that the essential features of these hard trade-off "laws" are universal and fundamental, in that they depend minimally on the details of this system and generalize to the robust efficiency of any autocatalytic network. The theory also suggests worst-case conditions that are consistent with initial experiments.

Chandra, Buzi, and Doyle

Most important paper so far.

UG biochem, math, control theory

the cen's use of ATT. III glycolysis, two ATP molecules are consumed upstream and four are produced downstream, which normalizes to q = 1(each y molecule produces two downstream) with kinetic exponent a = 1. To highlight essential trade-offs with the simplest possible analysis, we normalize the concentration such that the unperturbed ($\delta = 0$) steady states are $\overline{y} = 1$ and $\bar{x} = 1/k$ [the system can have one additional steady state, which is unstable when (1, 1/k) is stable]. [See the supporting online material (SOM) part I]. The basal rate of the PFK reaction and the consumption rate have been normalized to 1 (the 2 in the numerator and feedback coefficients of the reactions come from these normalizations). Our results hold for more general systems on discussed below and in SOM, but the analysis



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VOL 333

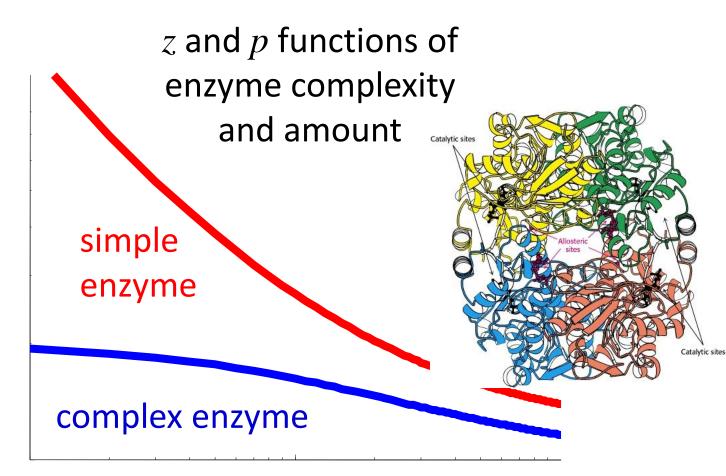
8 JULY 2011

Theorem!

$$\frac{1}{\pi} \int_{0}^{\infty} \ln |S(j\omega)| \left(\frac{z}{z^{2} + \omega^{2}}\right) d\omega \ge \ln \left|\frac{z + p}{z - p}\right|$$



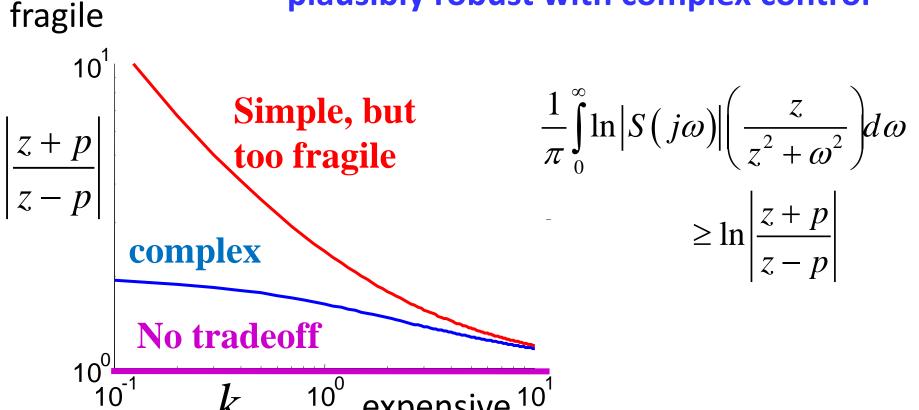
$$\ln \left| \frac{z+p}{z-p} \right|$$



Enzyme amount

Hard tradeoff in glycolysis is

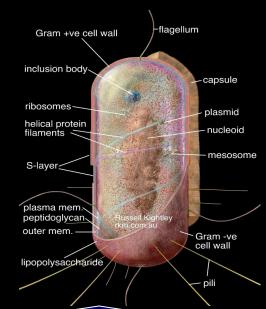
- robustness vs efficiency
- absent without autocatalysis
- too fragile with simple control
- plausibly robust with complex control



System

"Emergent":
"Nontrivial"
consequences
of other
constraints

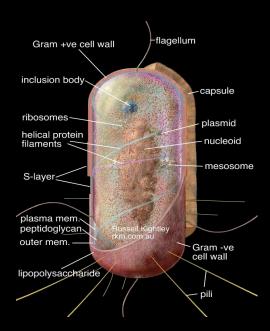
Architecture = Constraints



Protocols

Components

Systems requirements: Survive in hostile environments



Constraints

Components and materials: "Chemistry"

Constrained ("conserved"):

Moieties

- 1. NAD
- 2. Adenylate
- 3. Carbon
- 4. phosphate
- 5. oxygen
- 6. Oxidized state of metabolites
- 7. Reduced state of metabolites
- 8. High energy potential release

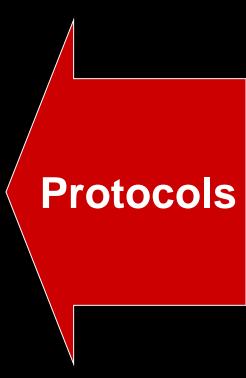
Constraints

Components and materials: "Chemistry"

Bacterial biosphere

- carriers: ATP, NADH, etc
- Precursors, ...
- Enzymes
- Translation
- Transcription
- Replication

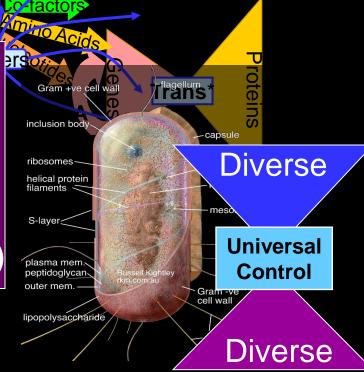
•



Architecture = protocols = "constraints that deconstrain"

Systems requirements: functional, efficient, robust, evolvable

Hard constraints:
Thermo (Carnot)
Info (Shannon)
Control (Bode)
Compute (Turing)



Protocols

Constraints

Components and materials: Energy, moieties

Systems requirements: functional, efficient, robust, evolvable

Constrained ("conserved"):

Moieties

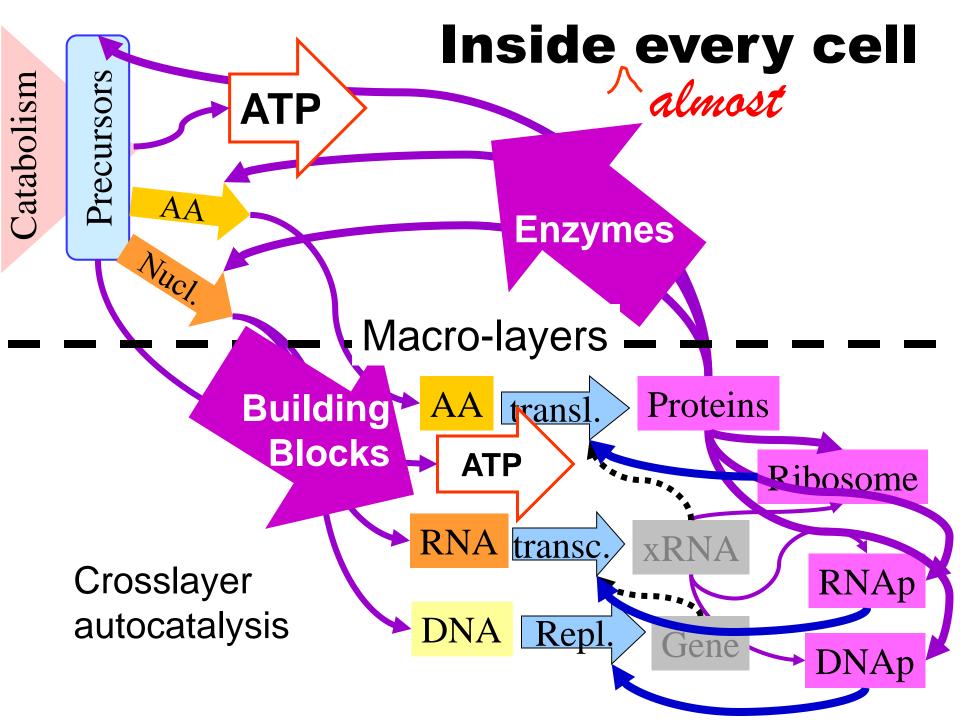
- 1. NAD
- 2. Adenylate
- 3. Carbon
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- 6. Oxidized state of metabolites
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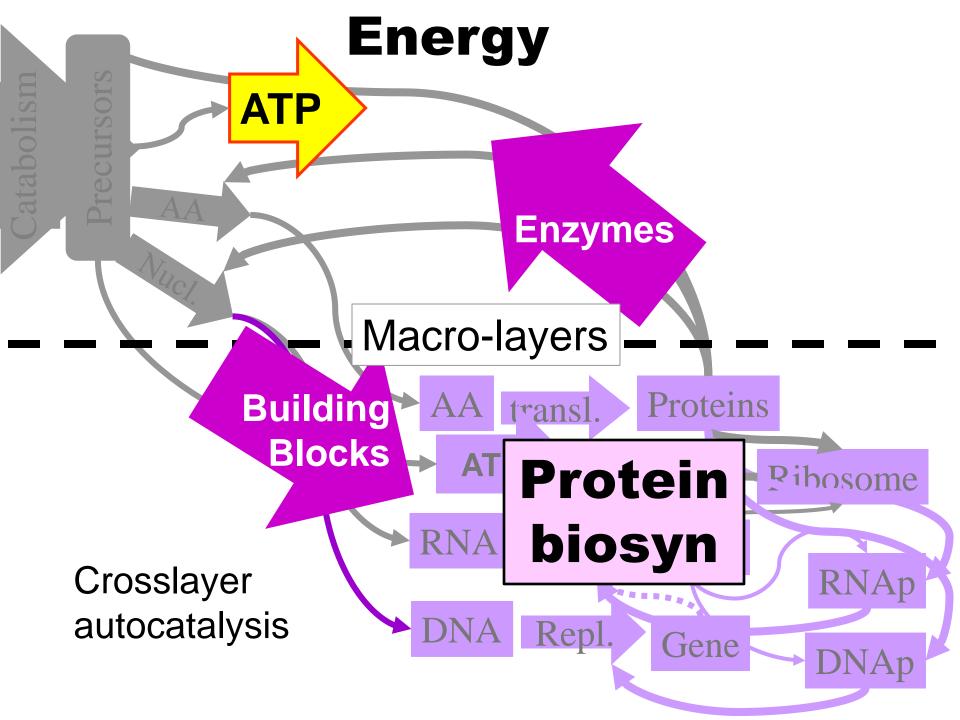
Constraints

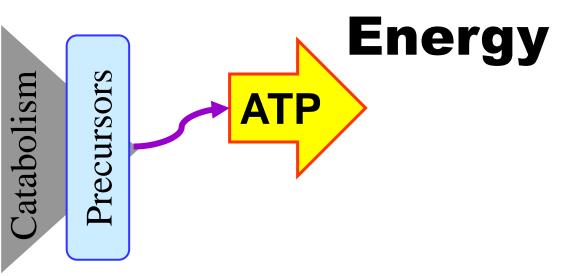
 $\left| \frac{1}{\pi} \int_{0}^{\infty} \ln \left| S(j\omega) \right| \left(\frac{z}{z^{2} + \omega^{2}} \right) d\omega$

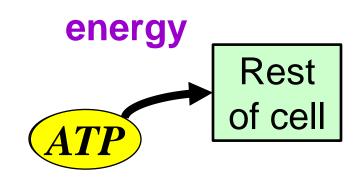
Protocols

Components and materials: Energy, moieties



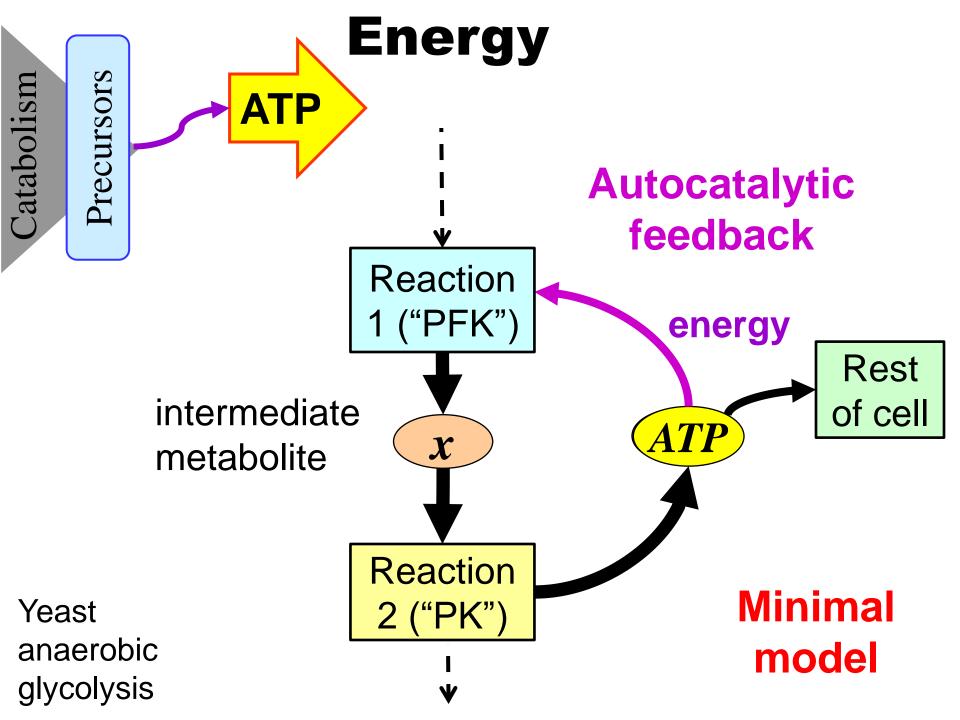




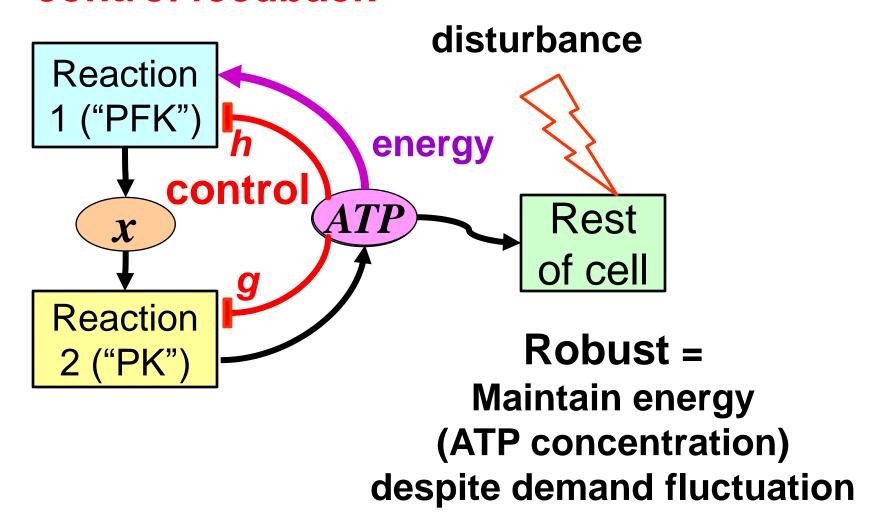


Yeast anaerobic glycolysis

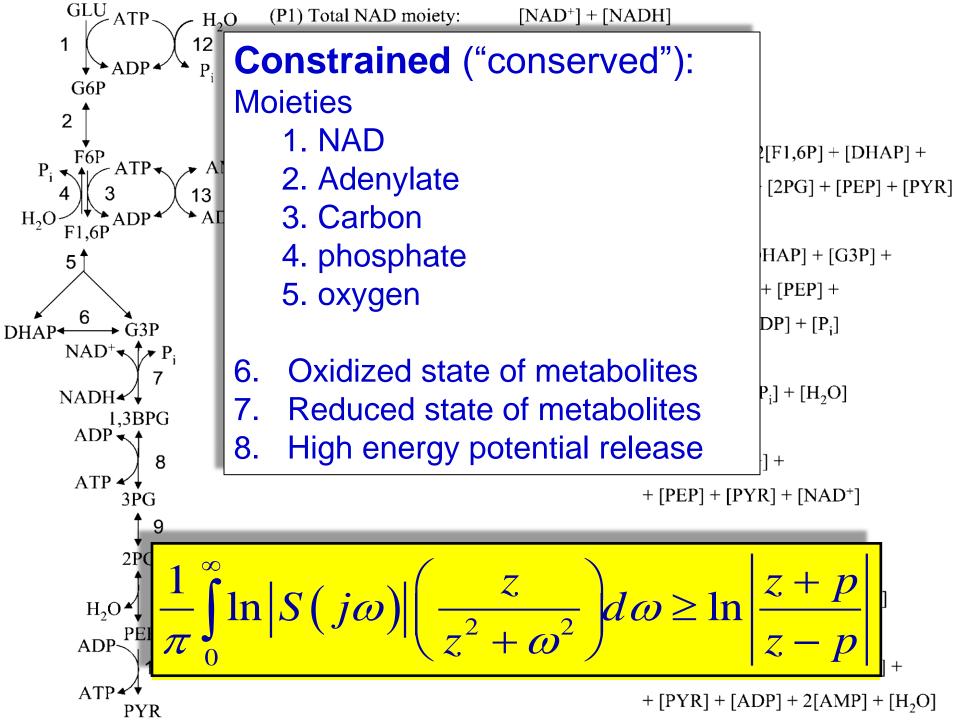
Minimal model



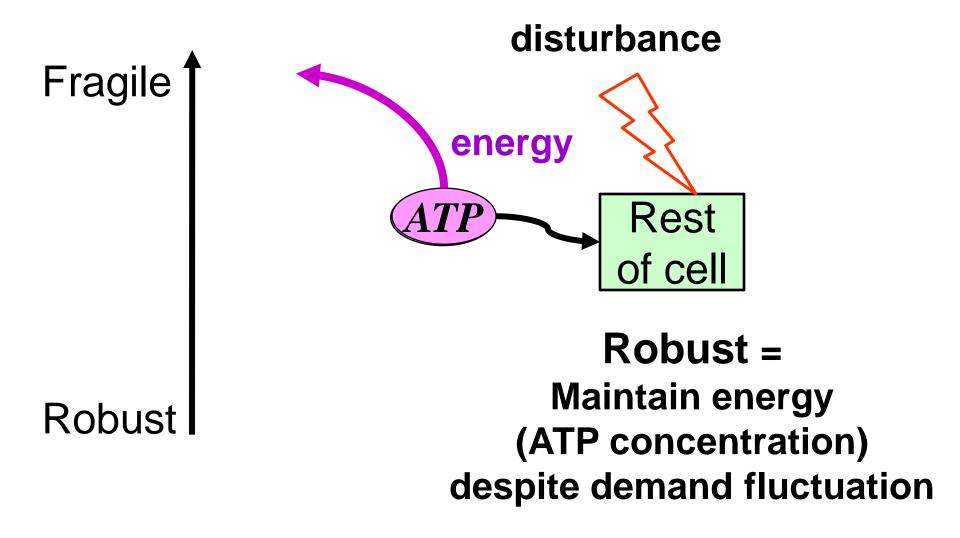
control feedback



Tight control creates "weak linkage" between power supply and demand



Hard tradeoff in glycolysis



disturbance

Accurate vs sloppy

Fragile



What makes this hard?

- 1. Instability (autocatalysis)
- 2. Delay (enzyme amount)

Robust

Robust

≈Disturbance rejection

≈ Accurate

Fragile '

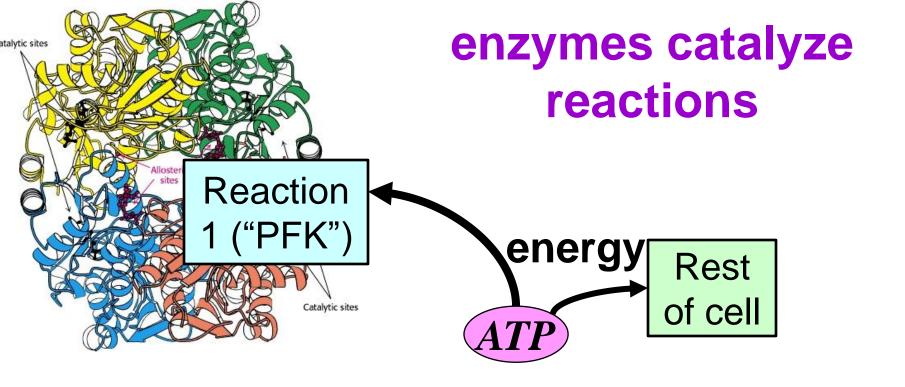
What makes this hard?

- 1. Instability
- 2. Delay

Robust

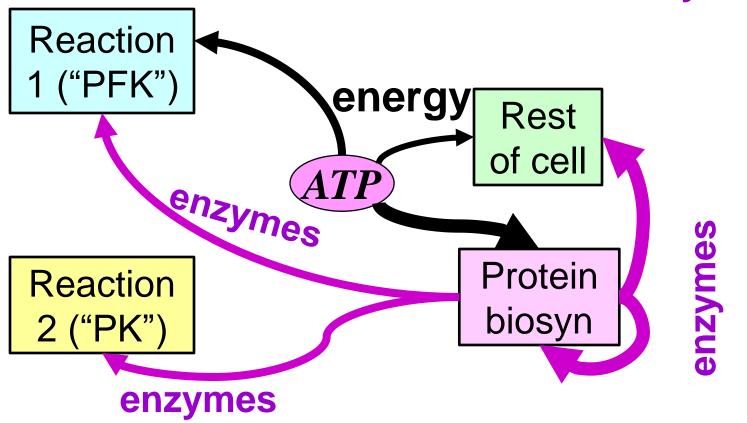
The CNS must cope with both

Today's important point



Reaction 2 ("PK")

enzymes catalyze reactions, another source of autocatalysis

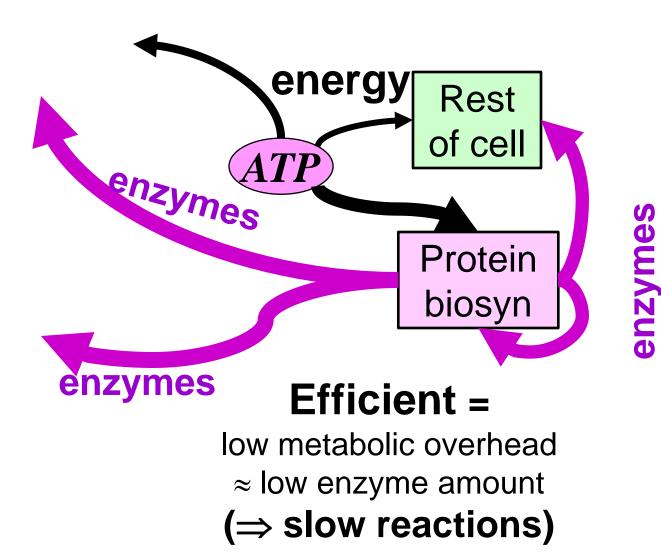


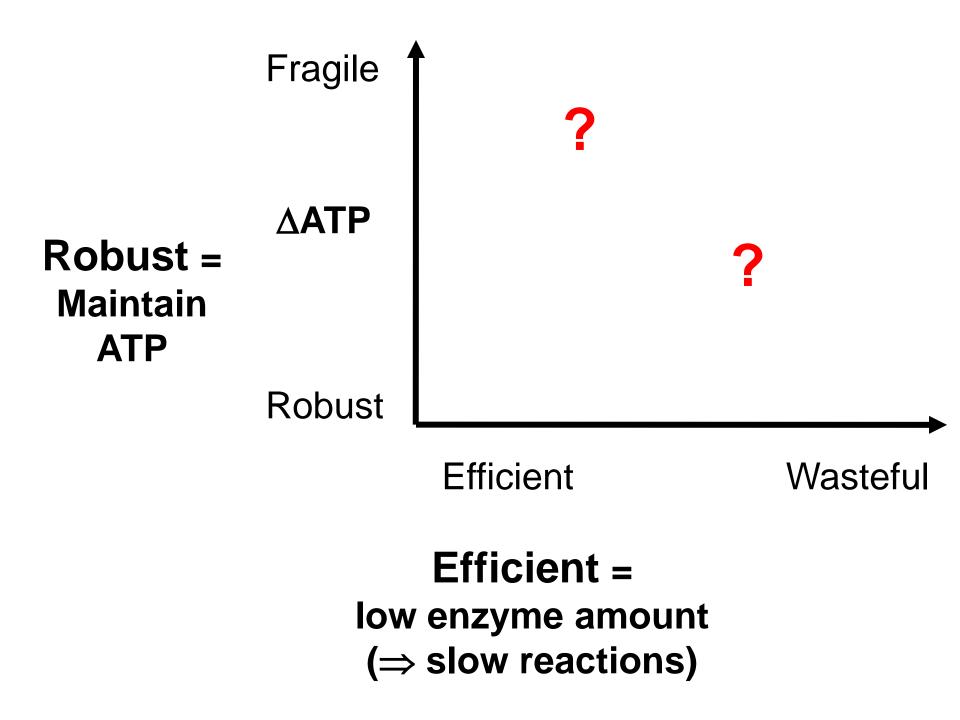
Efficient = low metabolic overhead ≈ low enzyme amount reaction rates

 ∞

enzyme amount

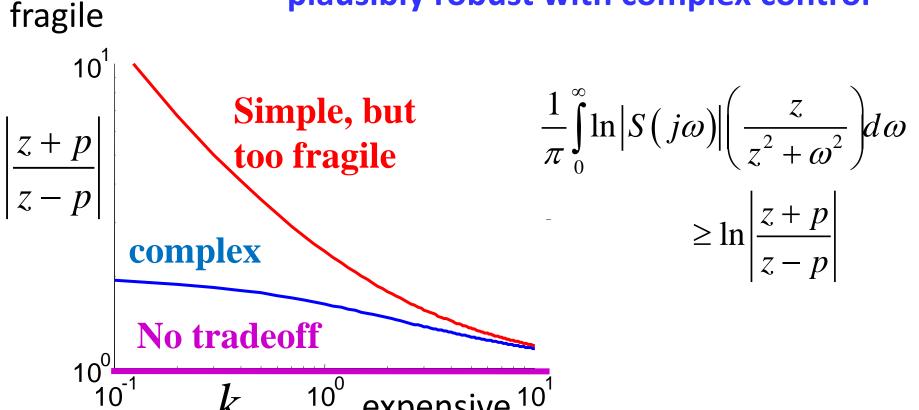
Can't make too many enzymes here, need to supply rest of the cell. enzymes catalyze reactions, another source of autocatalysis





Hard tradeoff in glycolysis is

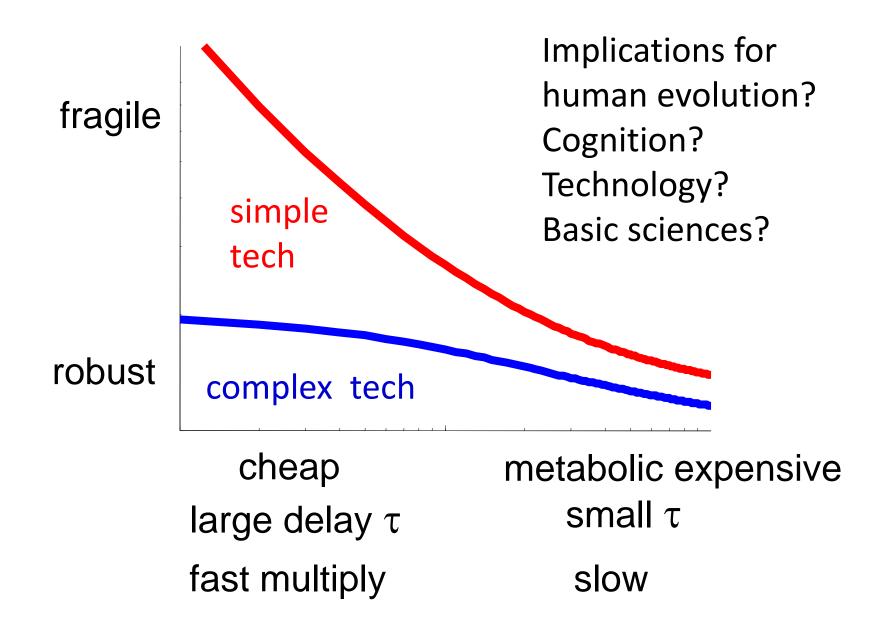
- robustness vs efficiency
- absent without autocatalysis
- too fragile with simple control
- plausibly robust with complex control



What (some) reviewers say

- "...to establish universality for all biological and physiological systems is simply wrong. It cannot be done...
- ... a mathematical scheme without any real connections to biological or medical...
- ...universality is well justified in physics... for biological and physiological systems ...a dream that will never be realized, due to the vast diversity in such systems.
- ...does not seem to understand or appreciate the vast diversity of biological and physiological systems...
- ...a high degree of abstraction, which ...make[s]
 the model useless ...

This picture is very general



This picture is very general

Domain specific costs/tradeoffs

metabolic overhead

cheap

metabolic expensive

CNS reaction time τ (delay)

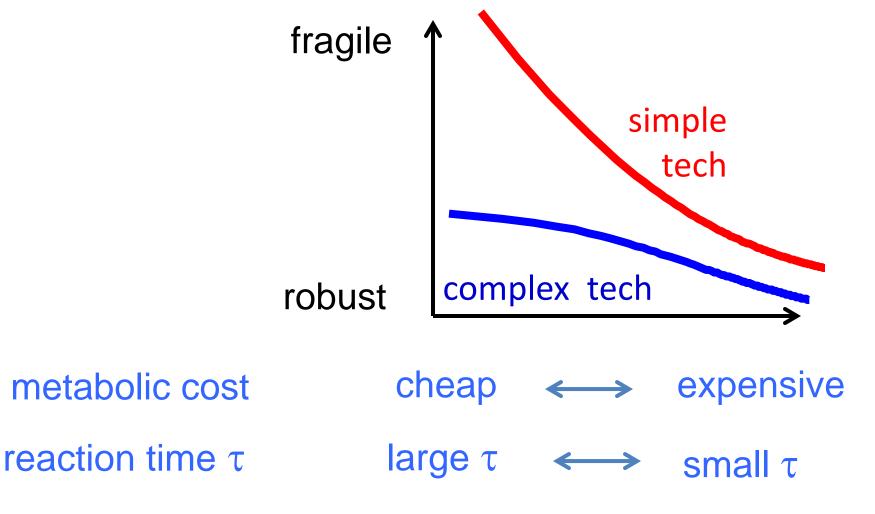
large $\tau \longleftrightarrow small \tau$

phage multiplication rate

fast ←→ slow multiply

This picture is very general

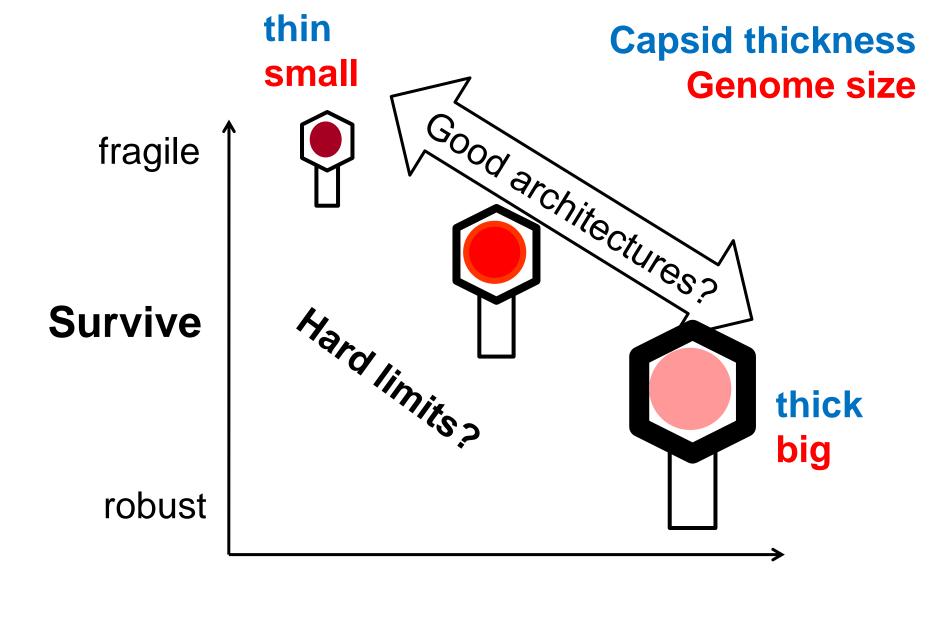
phage x rate



slow

Domain specific costs/tradeoffs

fast

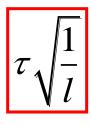


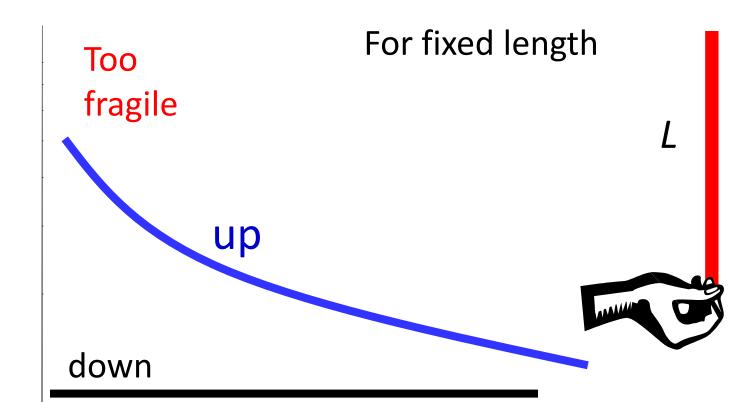
fast multiply

slow

$$\frac{1}{\pi} \int_{0}^{\infty} \ln |T(j\omega)| \frac{2p}{p^{2} + \omega^{2}} d\omega \ge p\tau \propto \tau \sqrt{\frac{1}{l}}$$

Fragility





large τ small 1/τ small τ large 1/τ

1/delay

$$\frac{1}{\pi} \int_{0}^{\infty} \ln |S(j\omega)| \left(\frac{2z}{z^{2} + \omega^{2}}\right) d\omega \ge \ln \left|\frac{z + p}{z - p}\right|$$

$$\varepsilon = \frac{1}{1 + r}$$

$$\frac{z + p}{z - p}$$

$$\sinh \left(\frac{z + p}{z - p}\right)$$

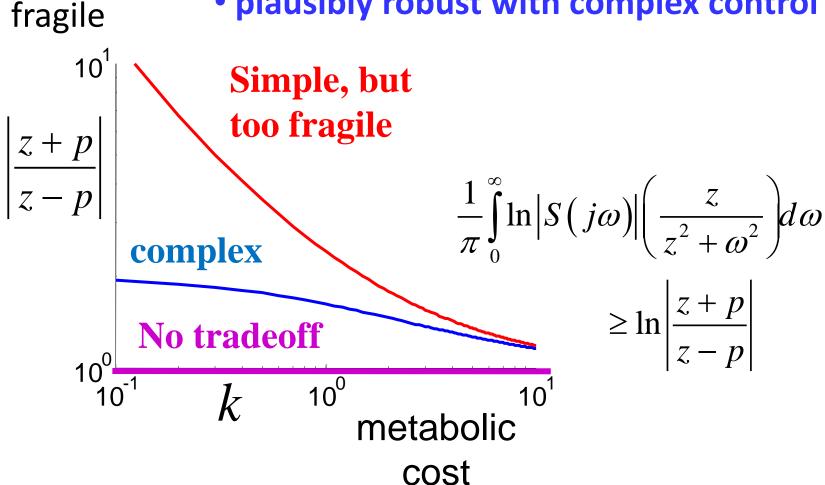
$$\sinh \left(\frac{z + p}{z - p}\right)$$

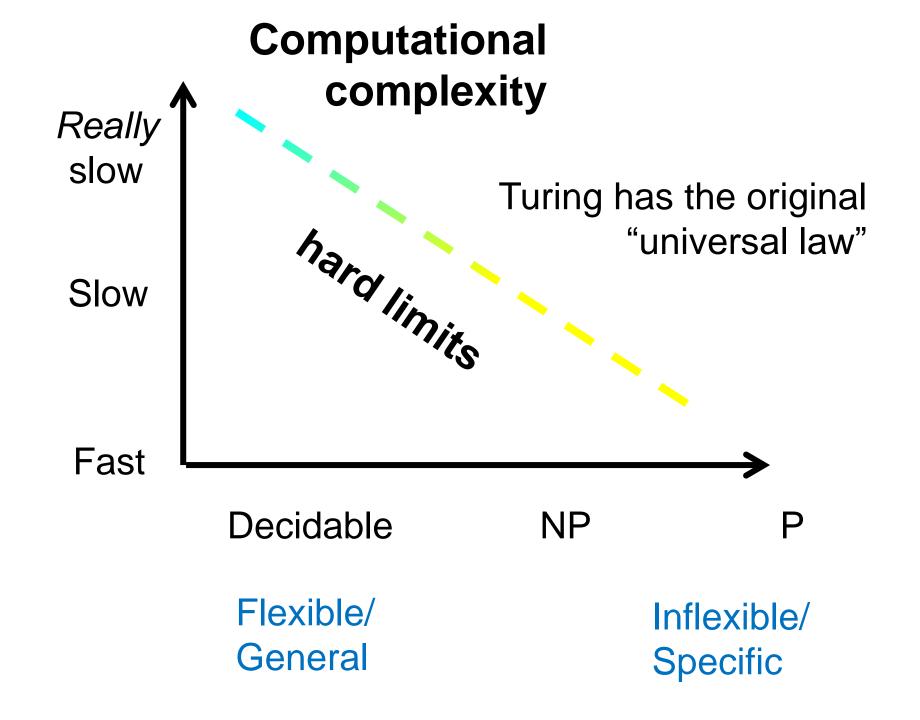
$$\cosh \left(\frac{$$

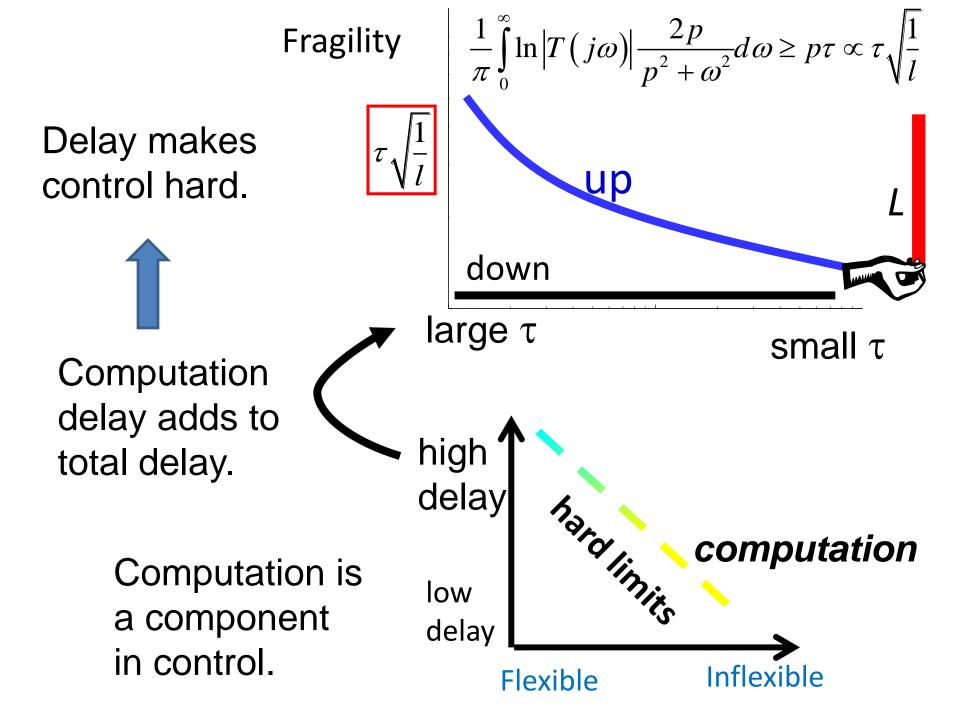
This is a cartoon, but can be made precise.

Hard tradeoff in glycolysis is

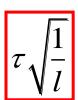
- robustness vs efficiency
- absent without autocatalysis
- too fragile with simple control
- plausibly robust with complex control







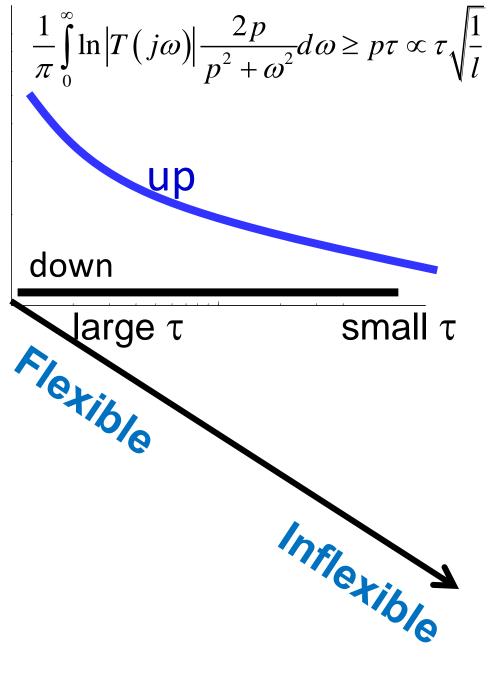
Fragility



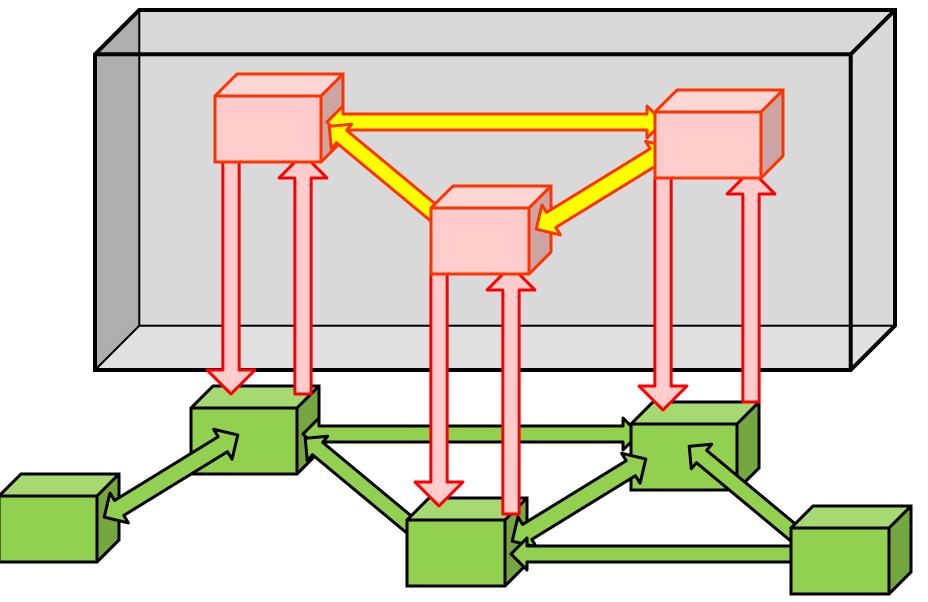
This needs formalization:

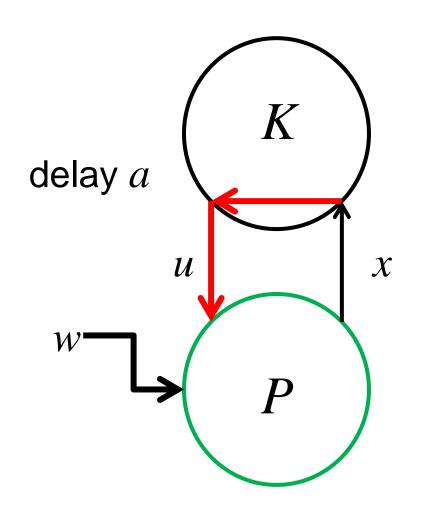
What *flexibility* makes control hard?

Large, structured uncertainty?



What about: Cyber-physical: decentralized control with internal delays?





$$x_{t+1} = px_t + w_t + u_{t-a}$$
$$p > 1$$

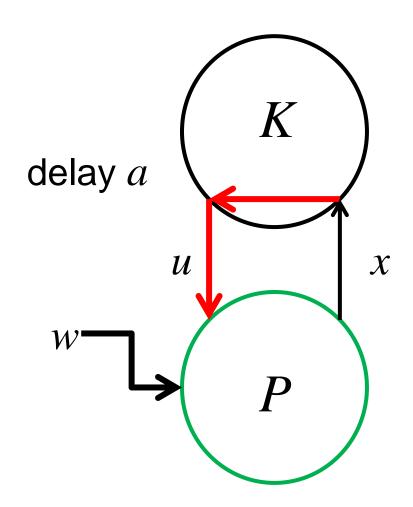
No delay or no uncertainty

$$u_{t-a} = -(px_t + w_t)$$

$$\Rightarrow ||x|| \approx 0 \quad ||u|| \approx ||w||$$

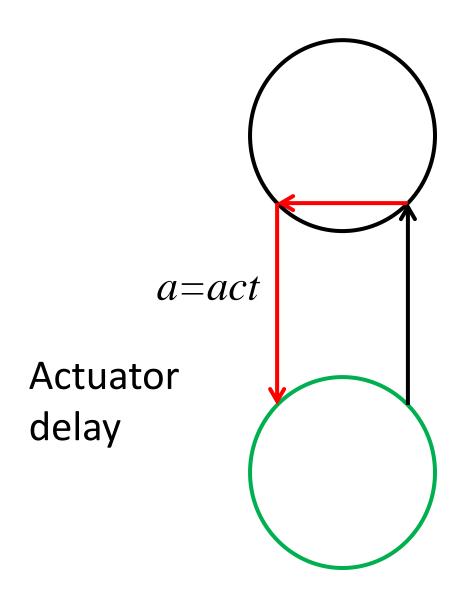
With delay *and* uncertainty

$$\Rightarrow \|x\| \approx \|u\| \approx p^a \|w\|$$

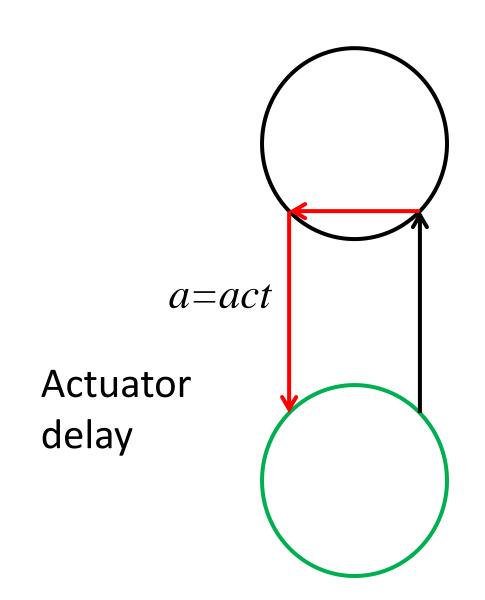


$$x_{t+1} = px_t + w_t + u_{t-a}$$
$$p > 1$$

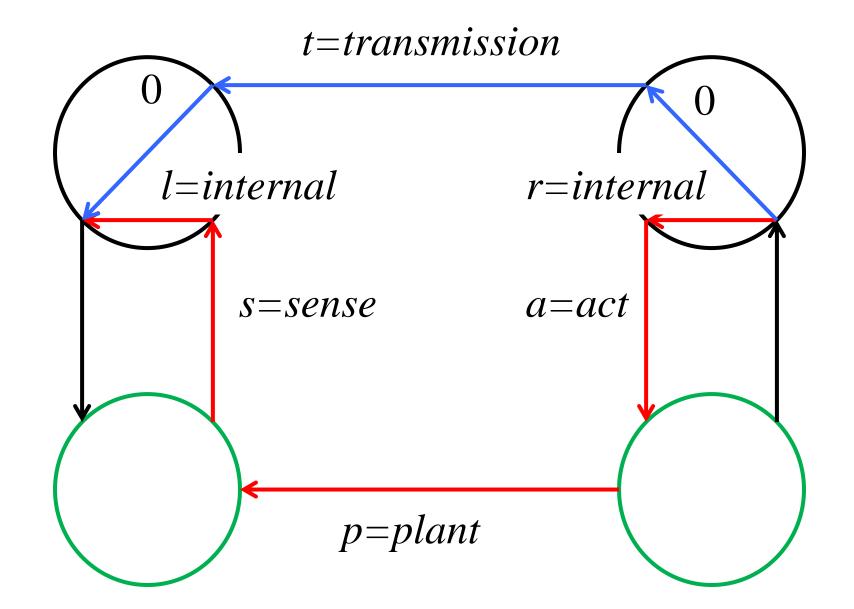
Focus on delays

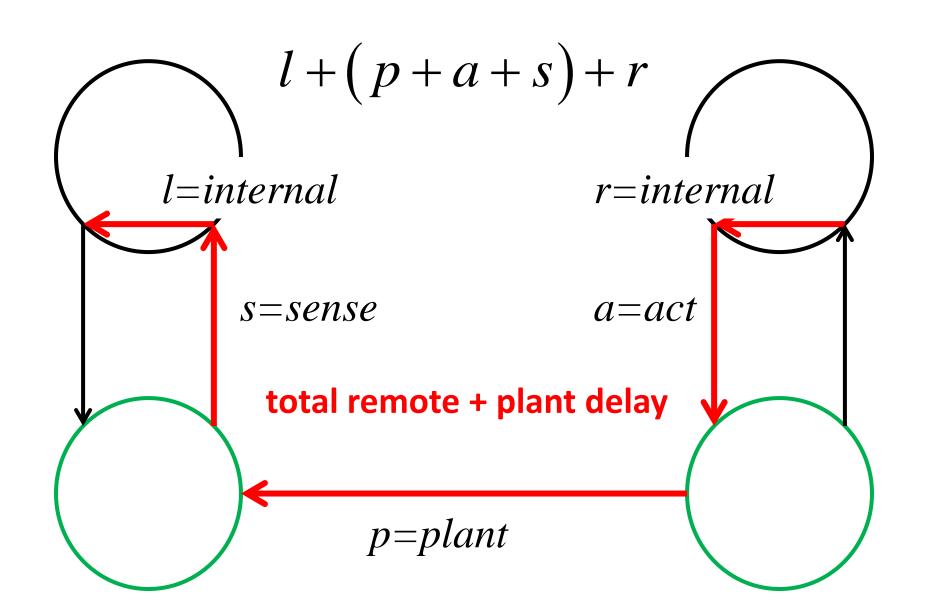


Focus on delays

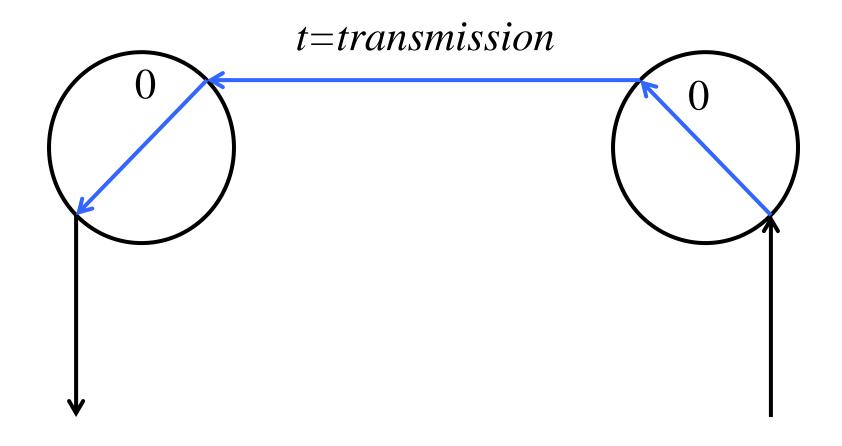


Decentralized control



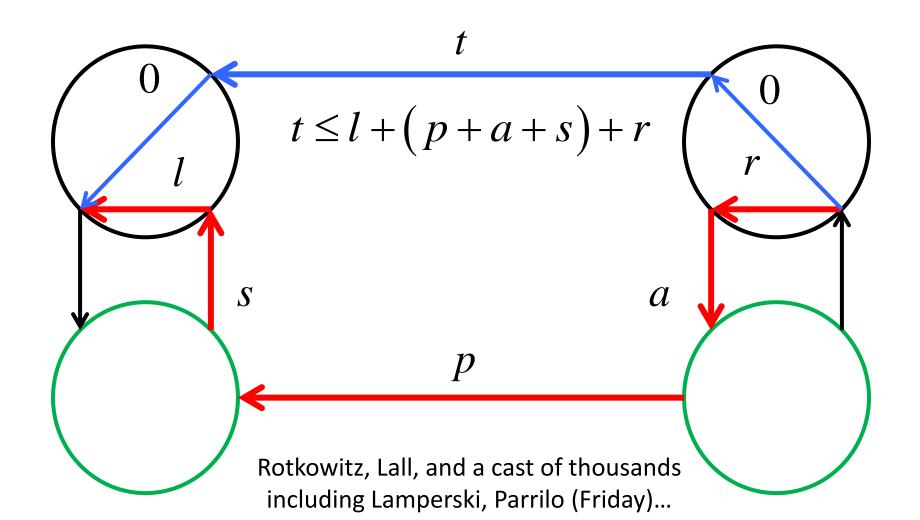


Communications delay

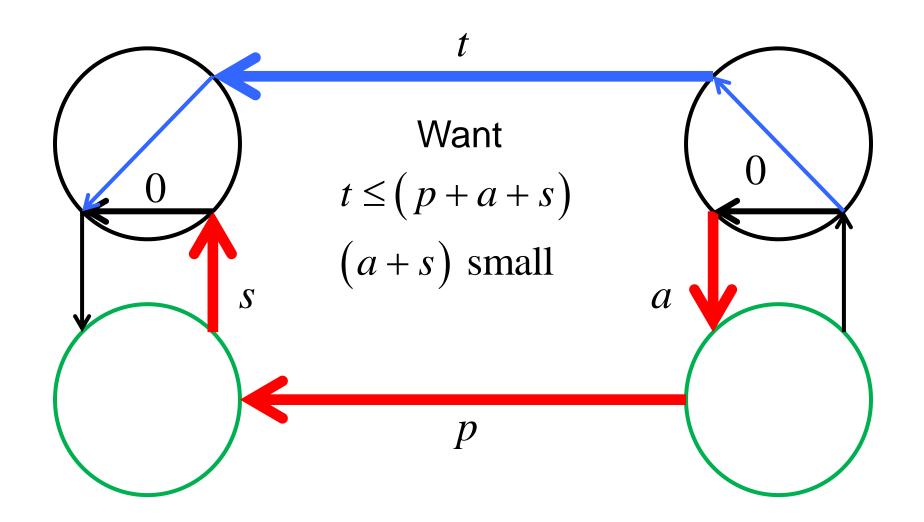


$$t \le l + (p + a + s) + r$$

Then decentralized control design can be made convex



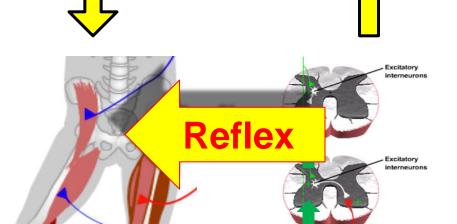
A primary driver of human brain evolution?



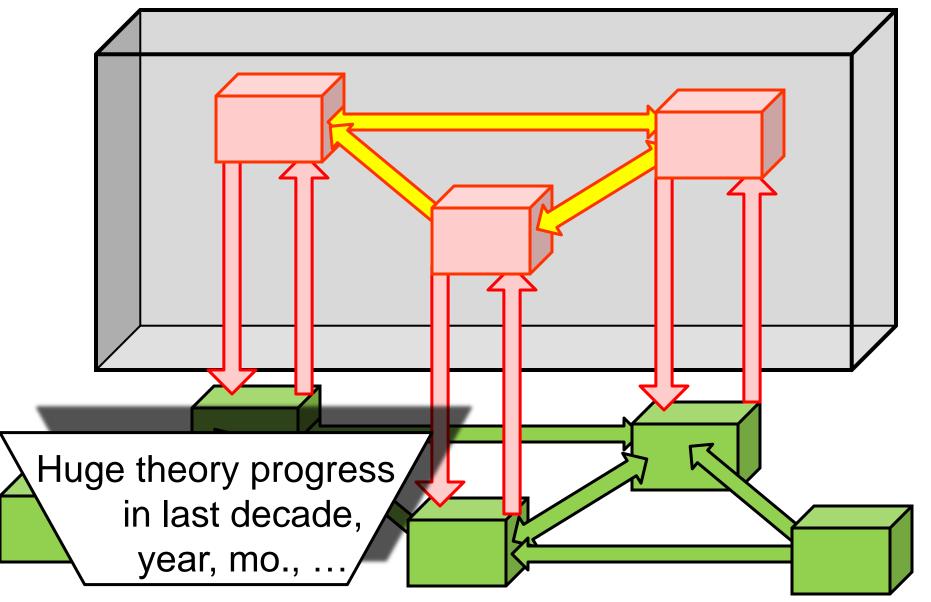


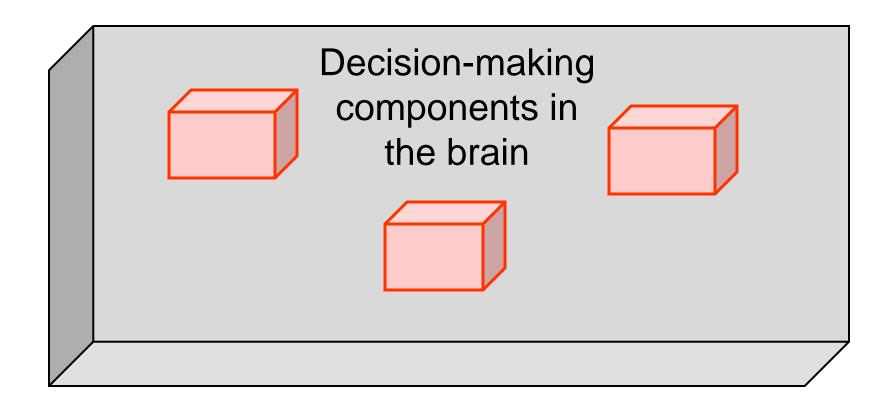
Brain as optimal controller

- Acquire
- Translate/ integrate
- Automate

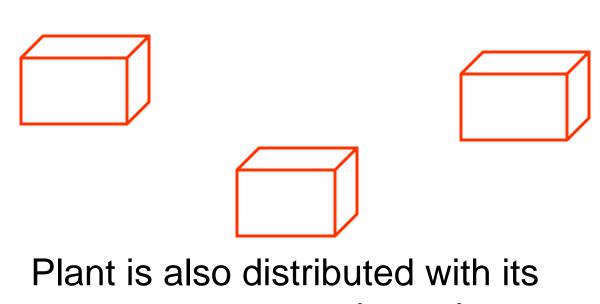


Going beyond black box: control is decentralized with internal delays.

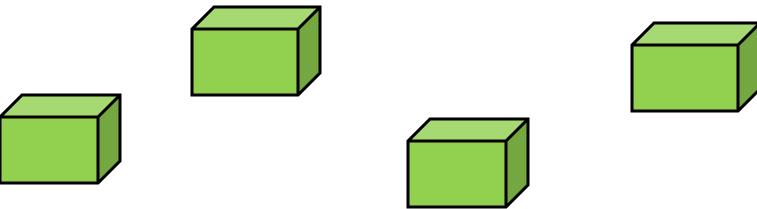




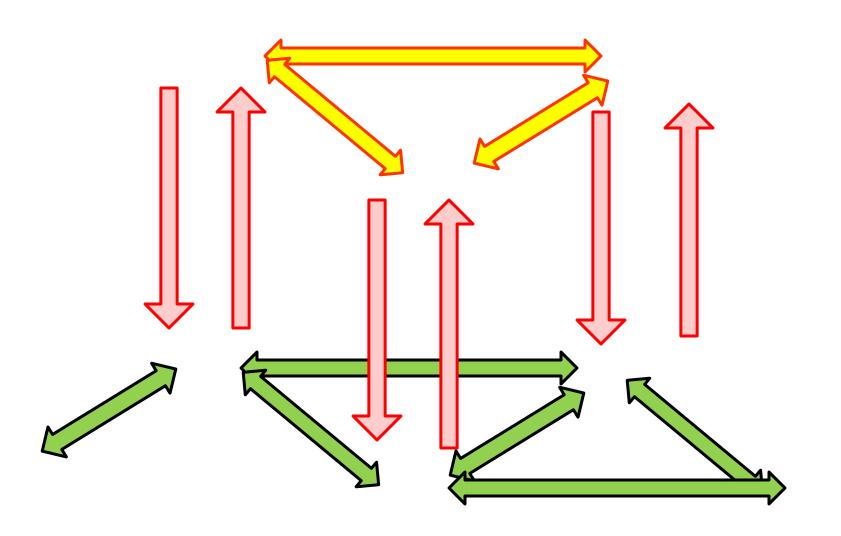
Decentralized, but initially assume computation is fast and memory is abundant.



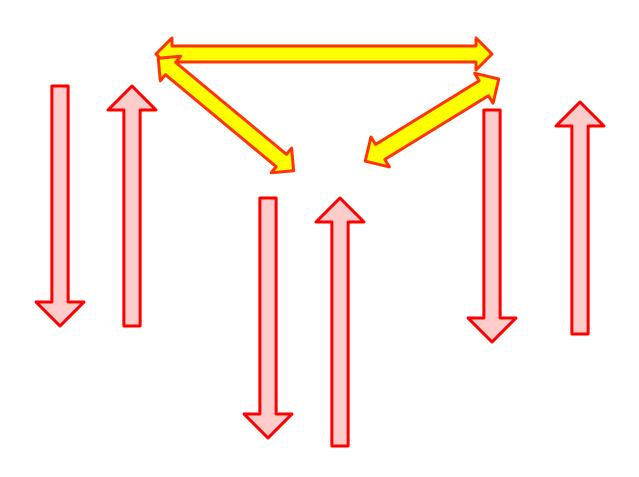




Internal delays between brain components, and their sensor and actuators, and also externally between plant components



Internal delays involve both computation and communication latencies



Compute

Communicate

Turing

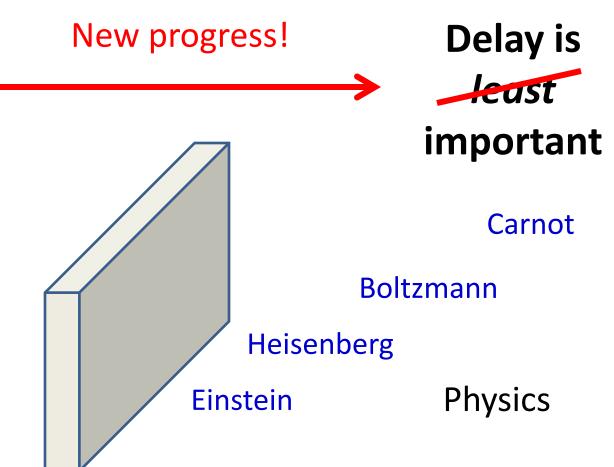
This progress is important.

Shannon

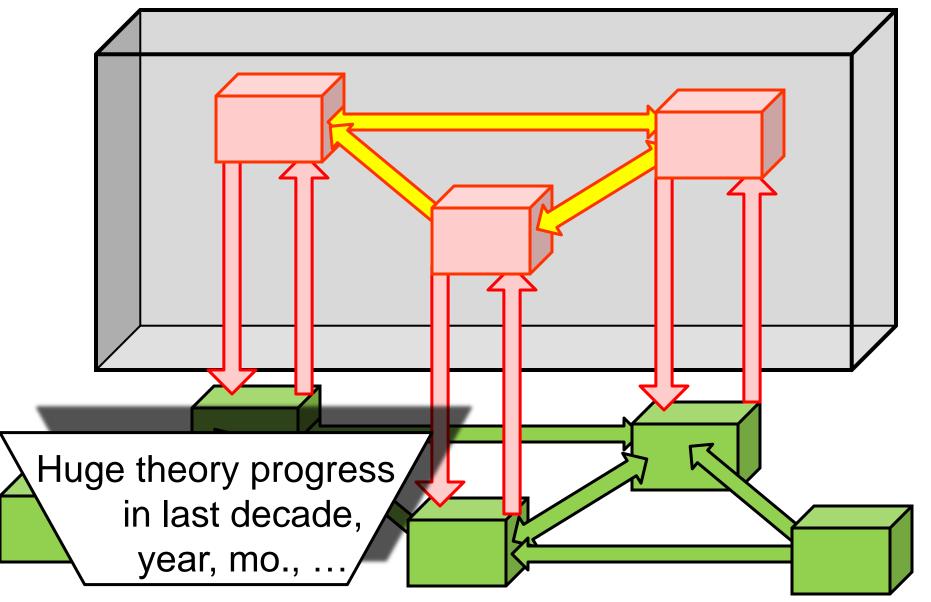
Delay is most important

Bode

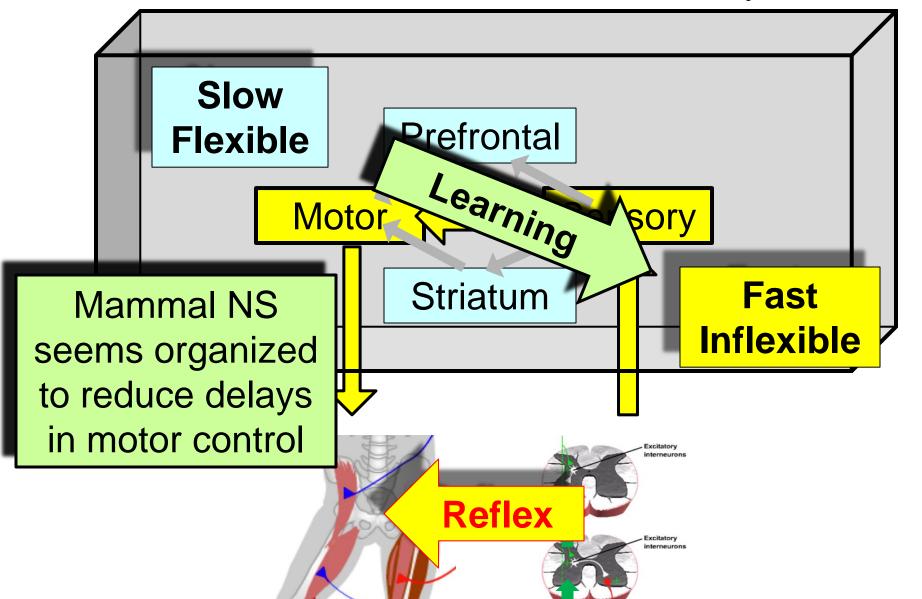
Control, OR



Going beyond black box: control is decentralized with internal delays.



Going beyond black box: control is decentralized with internal delays.



Universal architectures

Implications

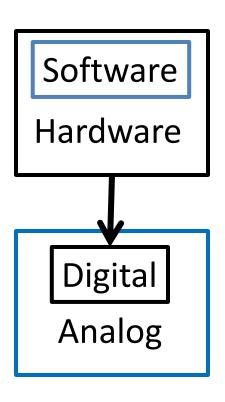
(Layered architectures discussed elsewhere)

Turing as

"new"

starting

point?

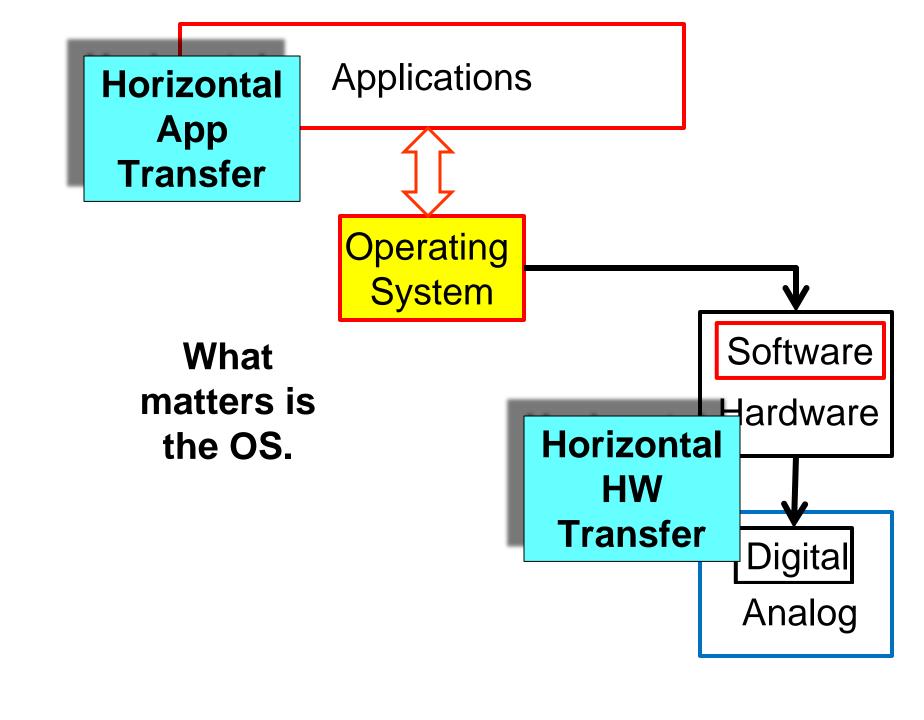


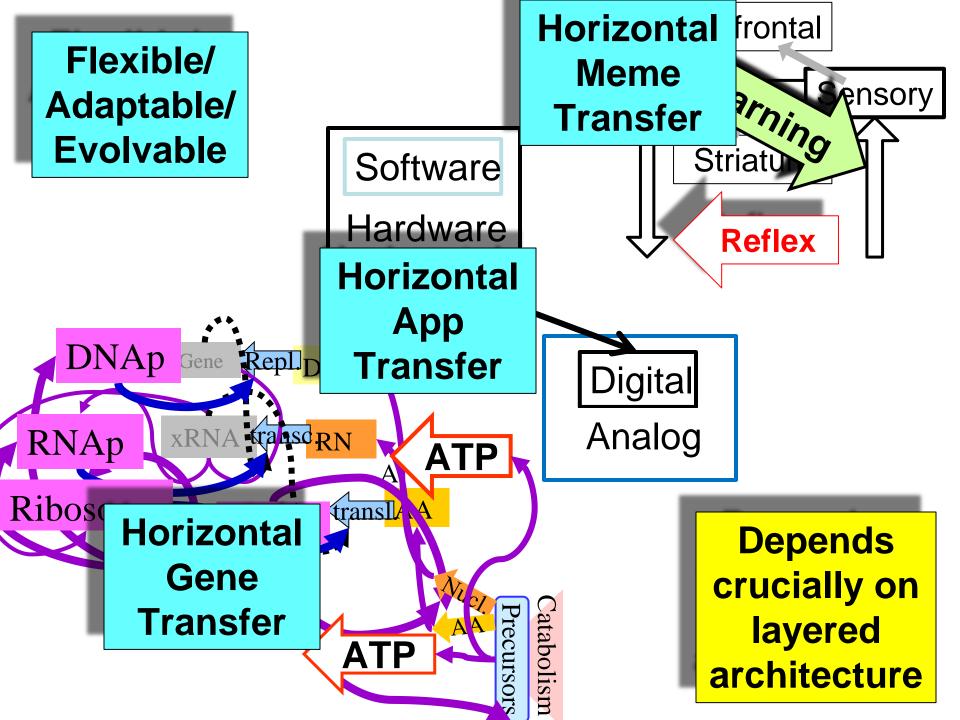
Essentials:

- 0. Model
- 1. Universal laws
- 2. Universal architecture
- 3. Practical implementation

Turing's 3 step research:

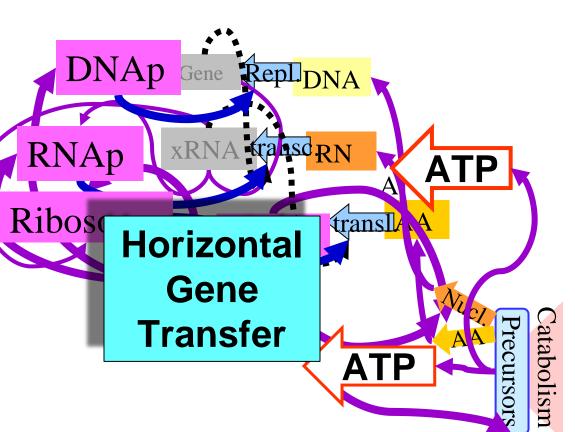
- 0. Virtual (TM) machines
- hard limits, (un)decidability using standard model (TM)
- 2. Universal architecture achieving hard limits (UTM)
- 3. Practical implementation in digital electronics (biology?)





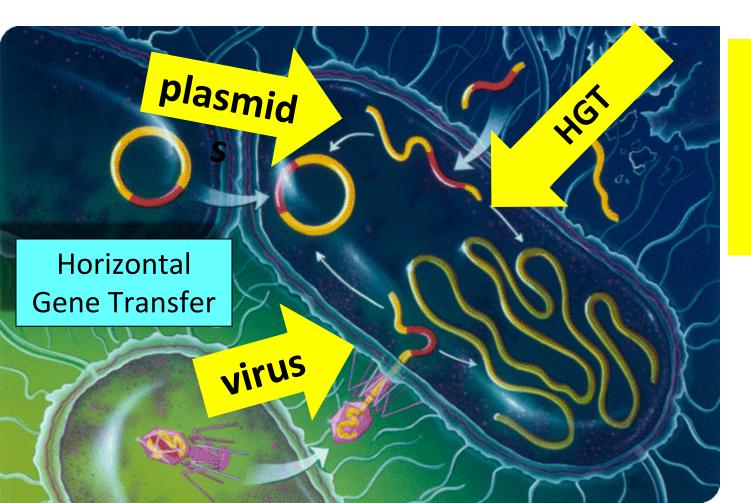
Sequence ~100 E Coli (not chosen randomly)

- ~ 4K genes per cell
- ~20K different genes in total
- ~ 1K universally shared genes



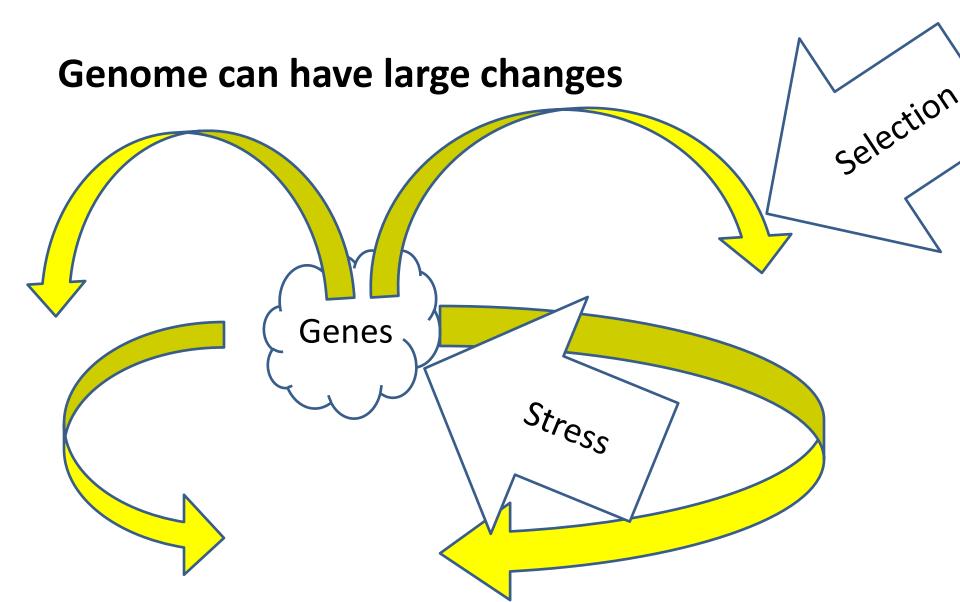
See slides on microbial biosphere laws and architectures.

selection + drift + mutation + gene flow + facilitated *variation*

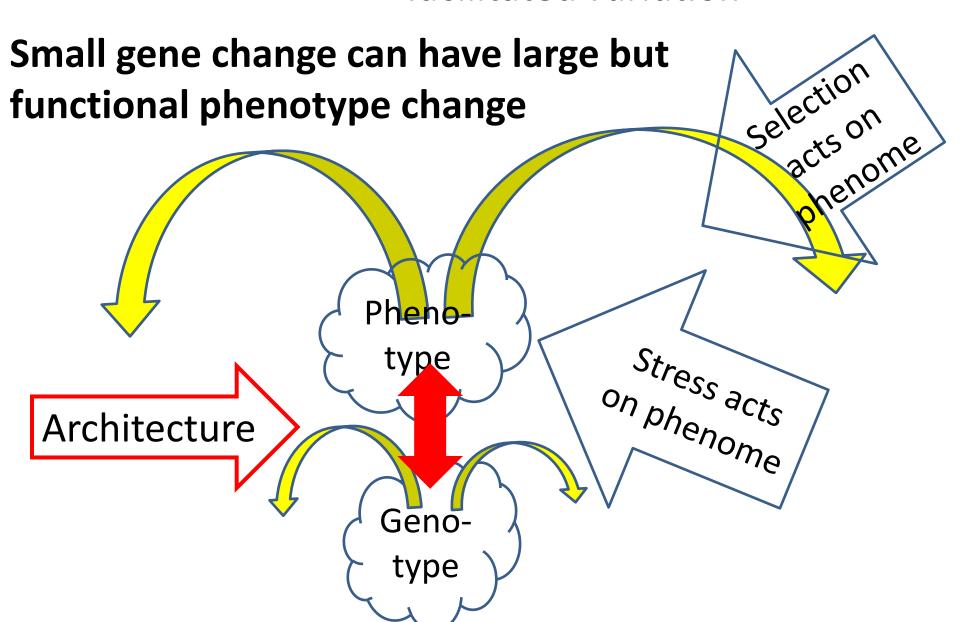


large functional changes in genomes

natural selection + genetic drift + mutation + gene flow + facilitated *variation*

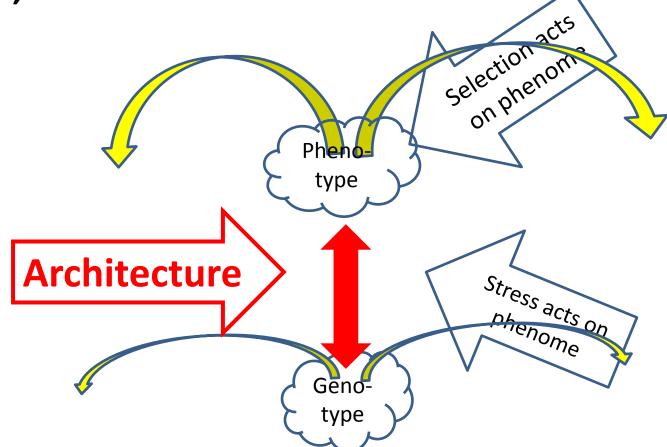


natural selection + genetic drift + mutation + gene flow + facilitated variation



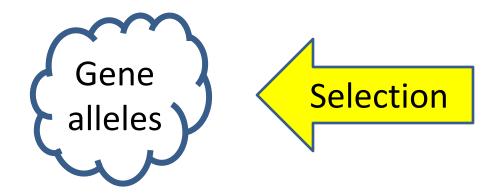
natural selection + genetic drift + mutation + gene flow + facilitated variation

Only possible because of shared, layered, network architecture



Standard theory:
natural selection + genetic drift
+ mutation + gene flow

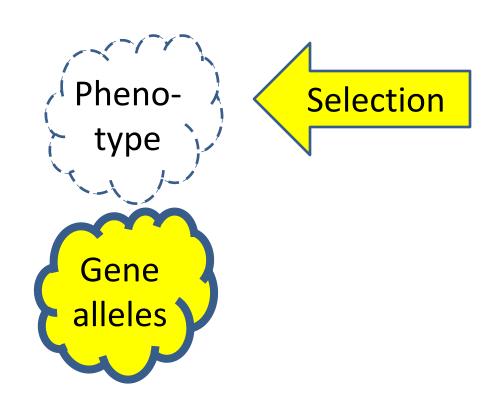
Greatly abridged cartoon here



Shapiro explains well what this is and why it's incomplete (but Koonin is more mainstream)

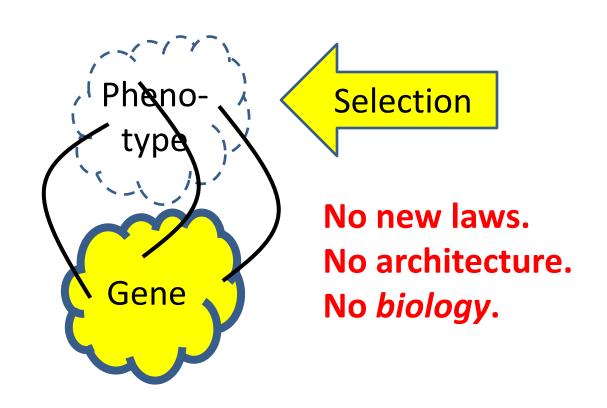
Standard theory:

selection + drift + mutation + gene flow

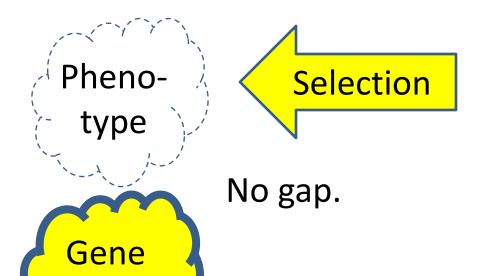


Standard theory:

selection + drift + mutation + gene flow



selection + drift + mutation + gene flow



alleles

All complexity is emergent from random ensembles with minimal tuning.

No new laws.

No architecture.

The battleground



Phenotype

Gene
alleles

No gap. Just physics.

Huge gap.
Need
supernatural



Genes?

What they agree on

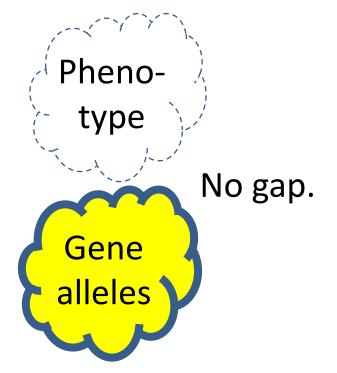
No new laws. No architecture. No biology.

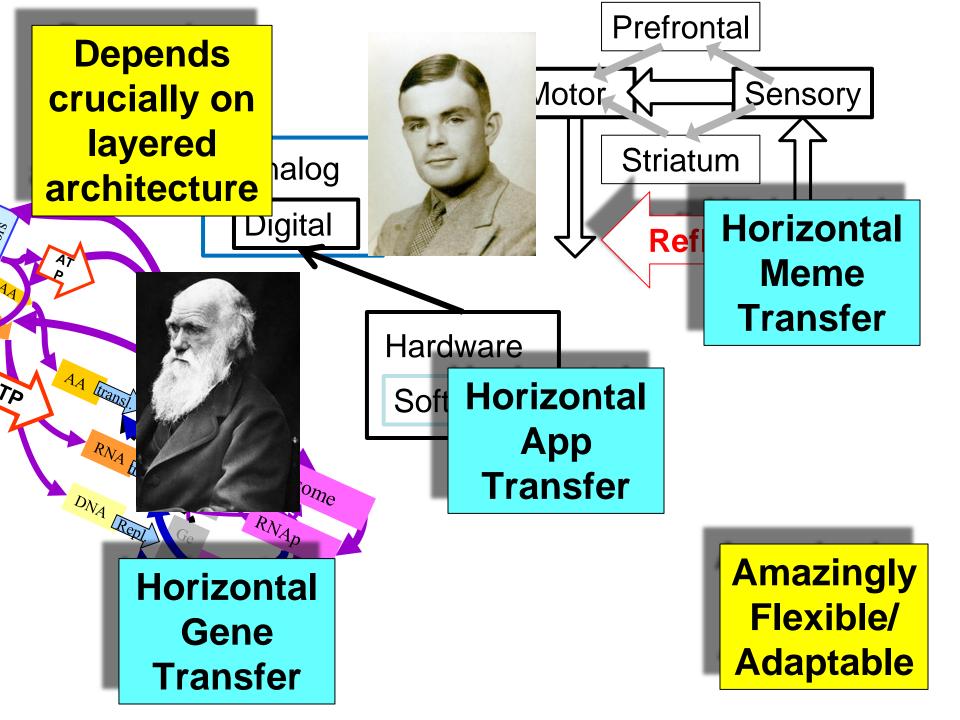


Huge gap.

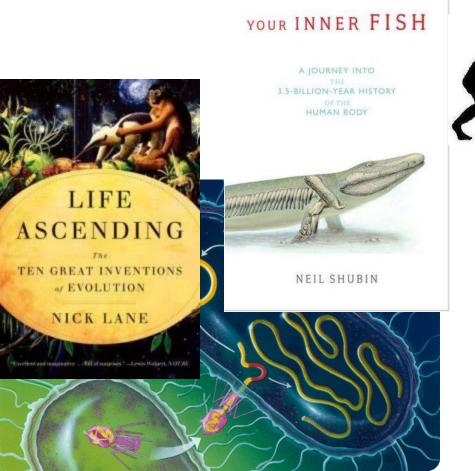


Genes



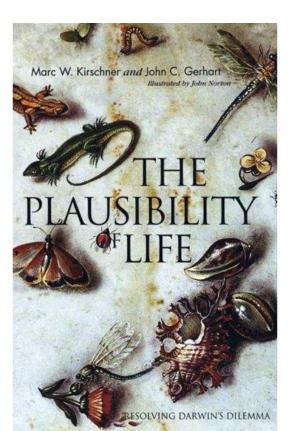


Putting biology back into evolution









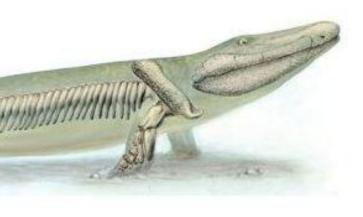
Universal architectures

What can go wrong?

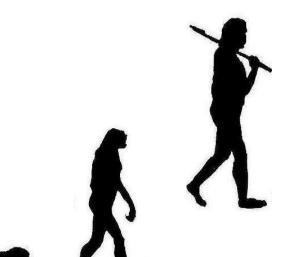
Unfortunately, not intelligent design

YOUR INNER FISH

A JOURNEY INTO
THE
3.5-BILLION-YEAR HISTORY
OF THE
HUMAN BODY

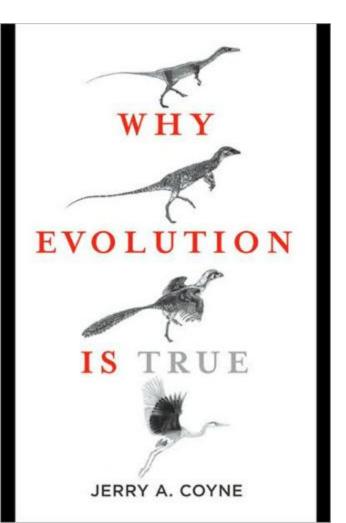


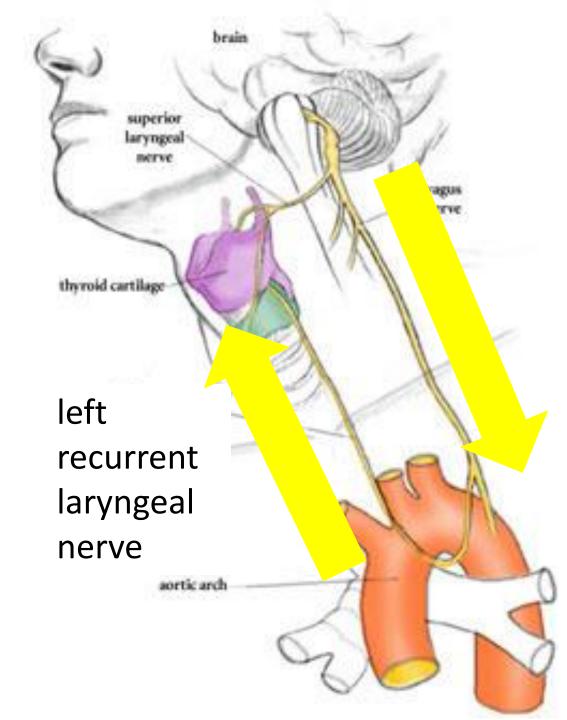
NEIL SHUBIN





Why?





Why? Building humans from fish parts.

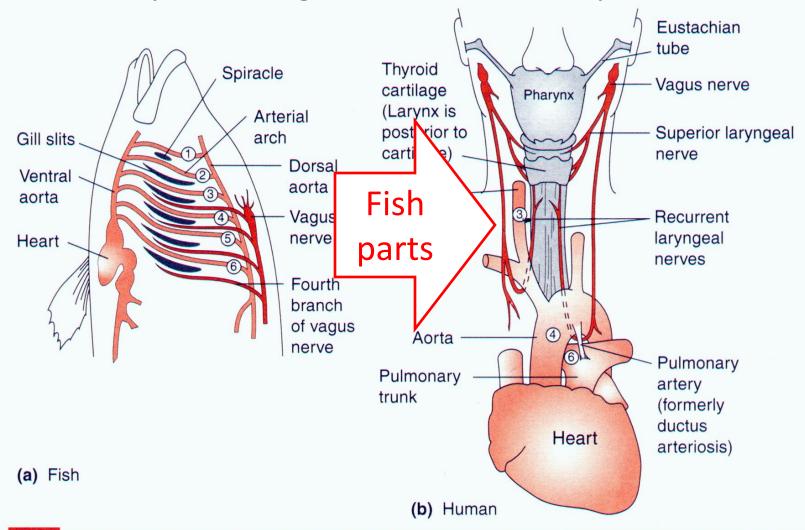
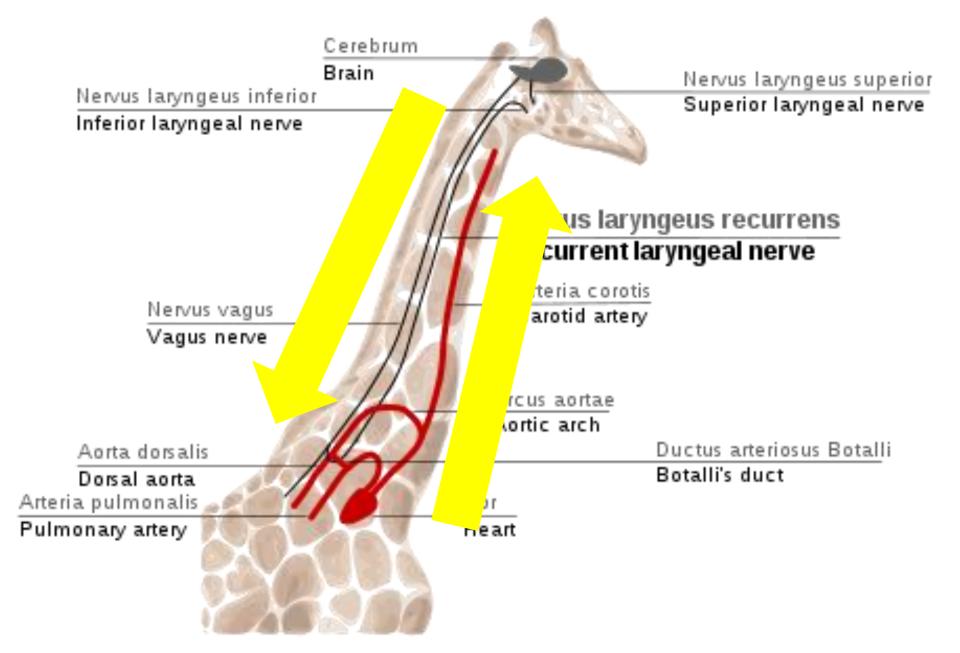
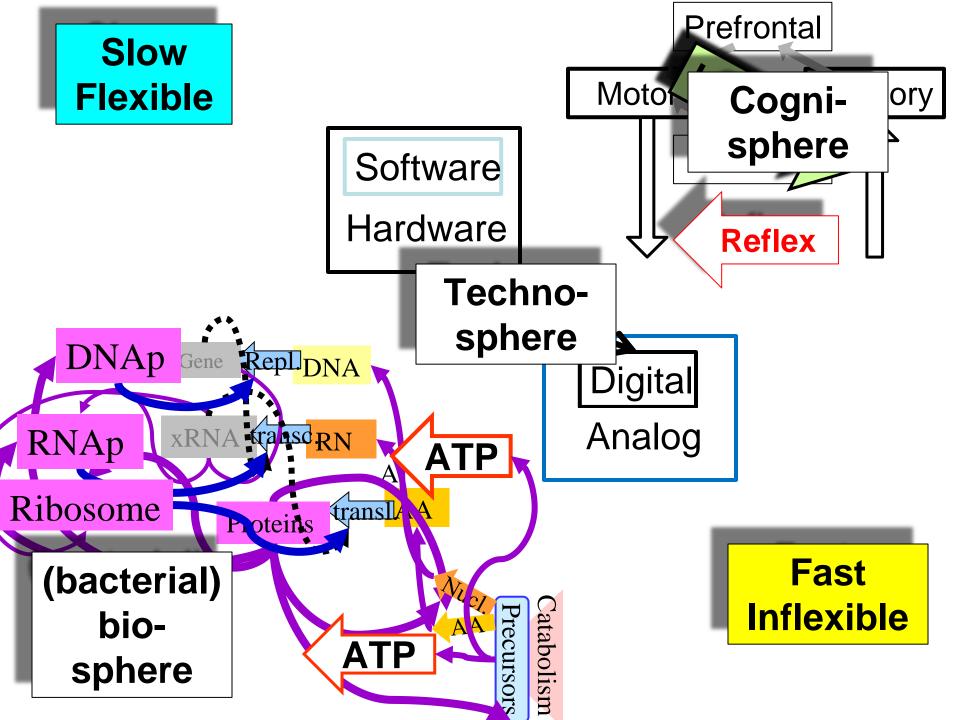
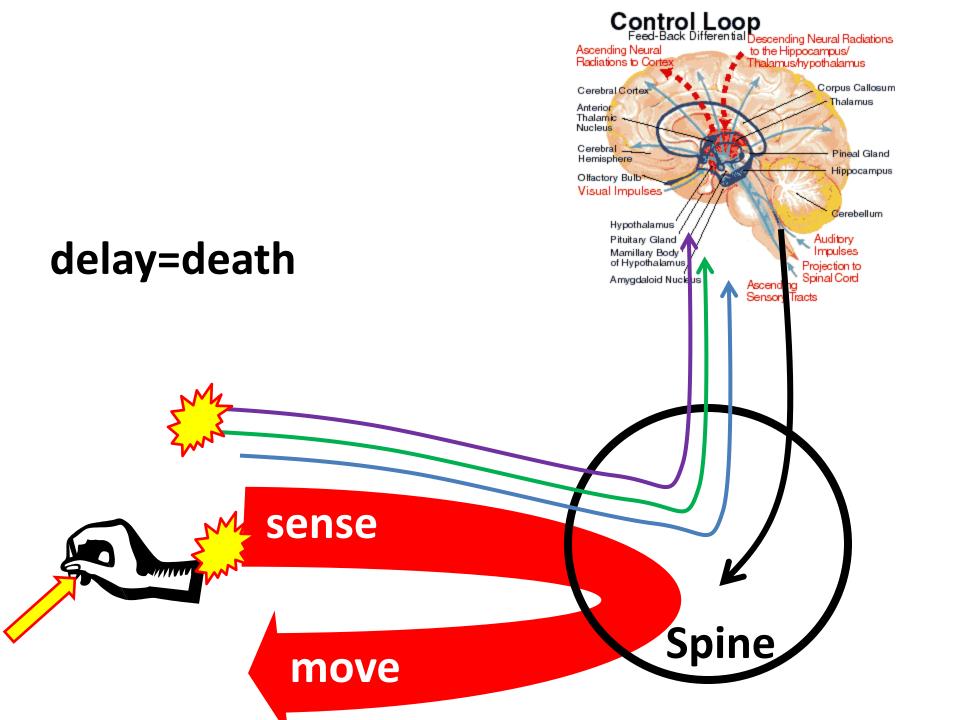


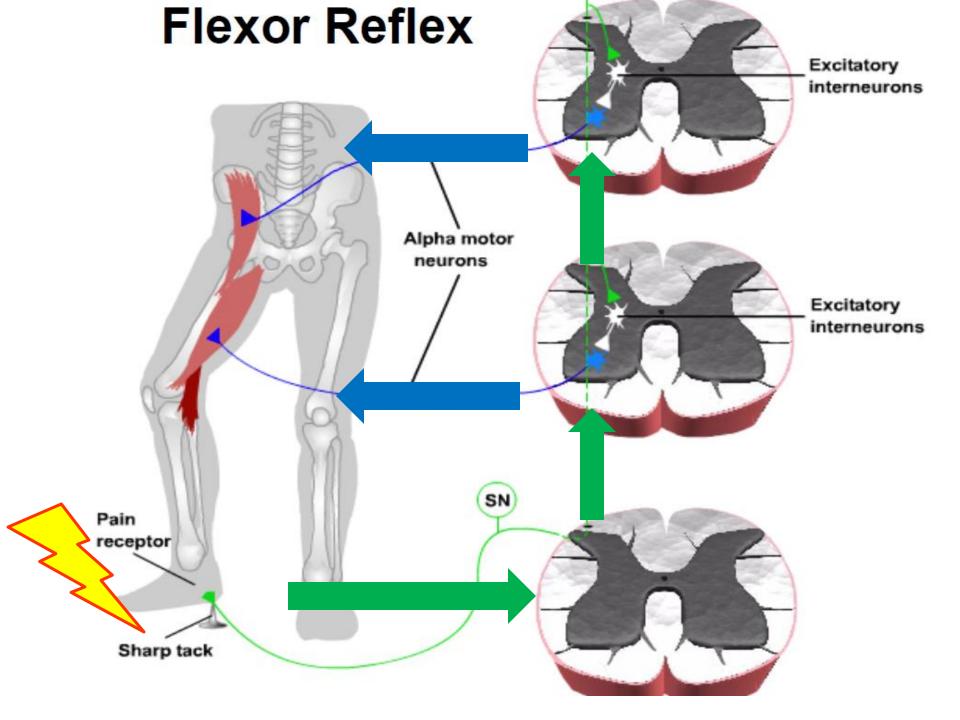
FIGURE 3–11 Schematic diagram showing the relationship between the vagus cranial nerve and the arterial arches in fish (a) and human (b). Only the third, fourth, and part of the sixth arterial arches remain in placental mammals, the sixth acting only during fetal development to carry blood to the placenta. The fourth vagal nerve in mammals (the recurrent laryngeal nerve) loops around the sixth arterial arch just as it did in the original fishlike ancestor, but must now travel a greater distance since the remnant of the sixth arch is in the thorax.

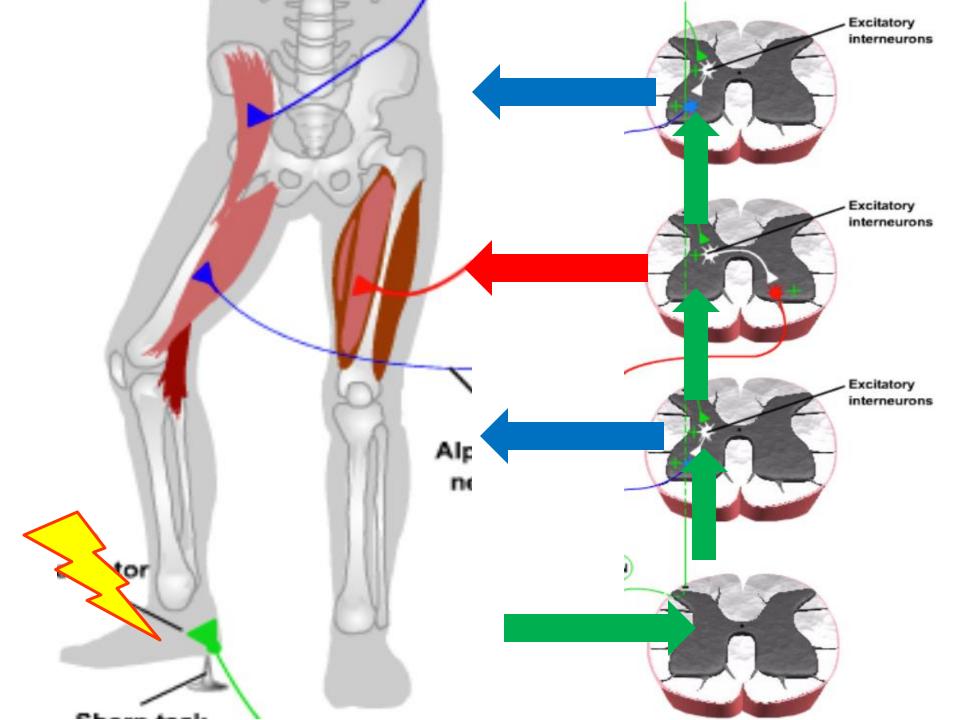
It could be worse.

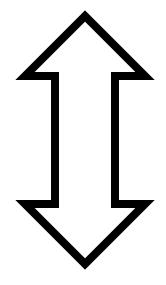


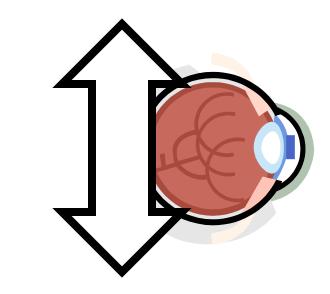


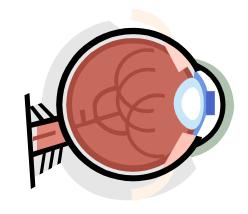


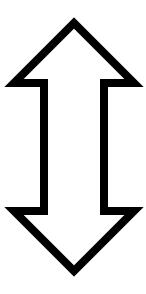






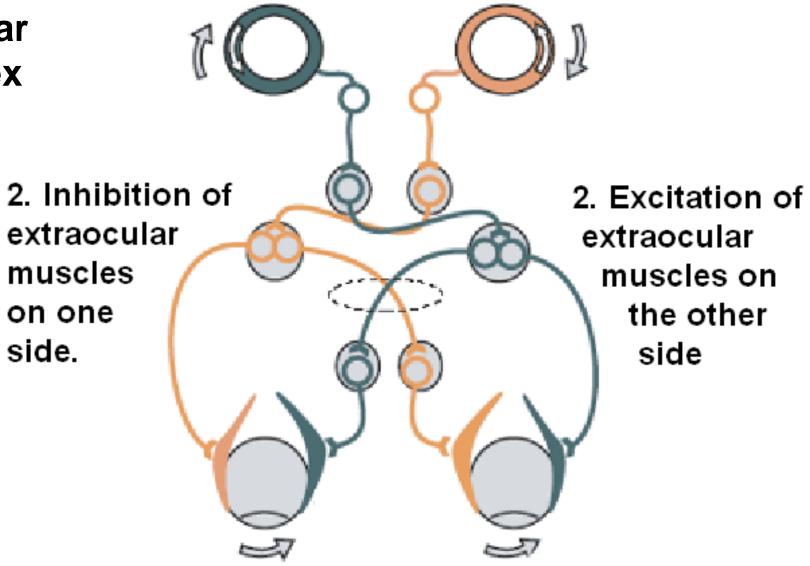




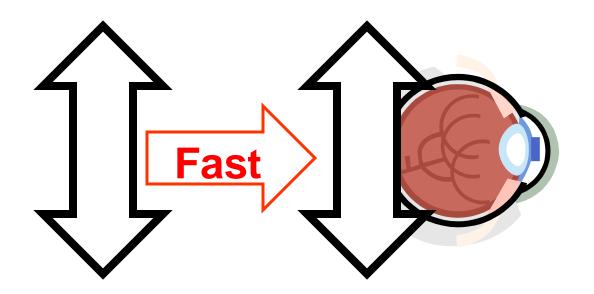


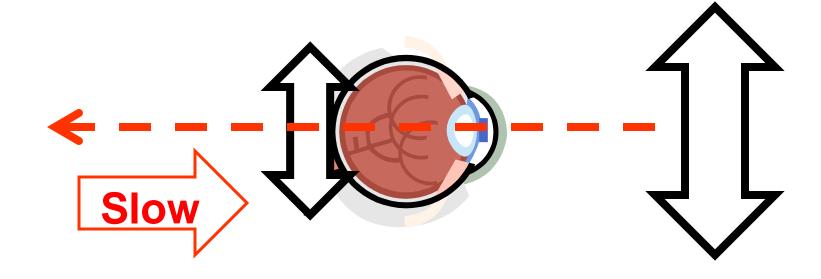
1. Detection of rotation

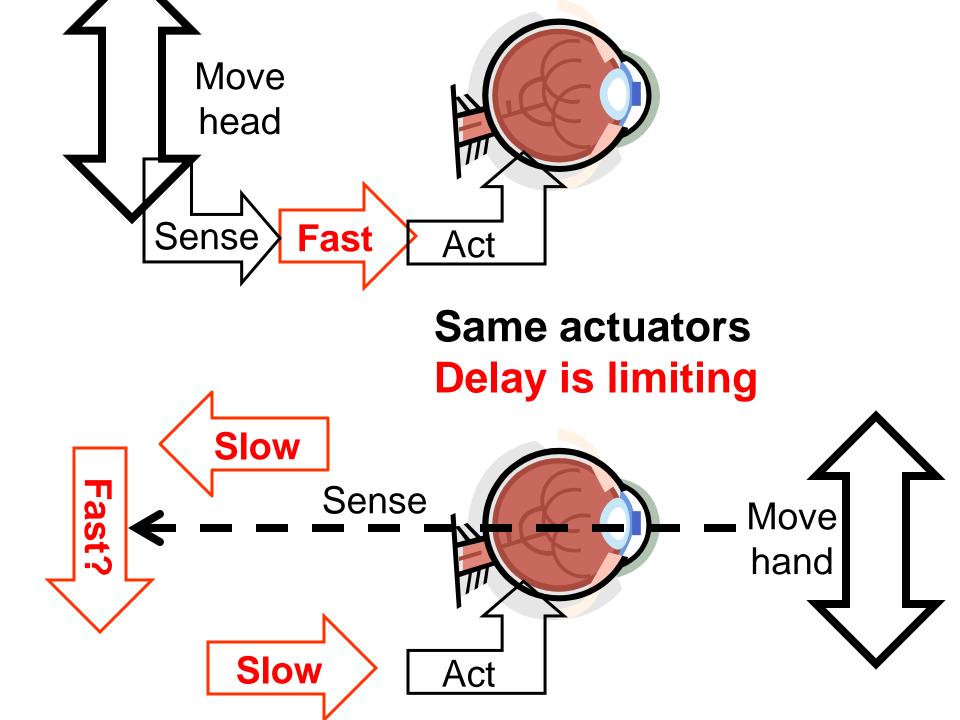




3. Compensating eye movement

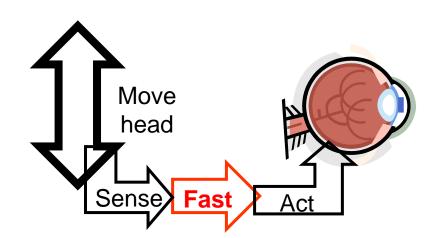






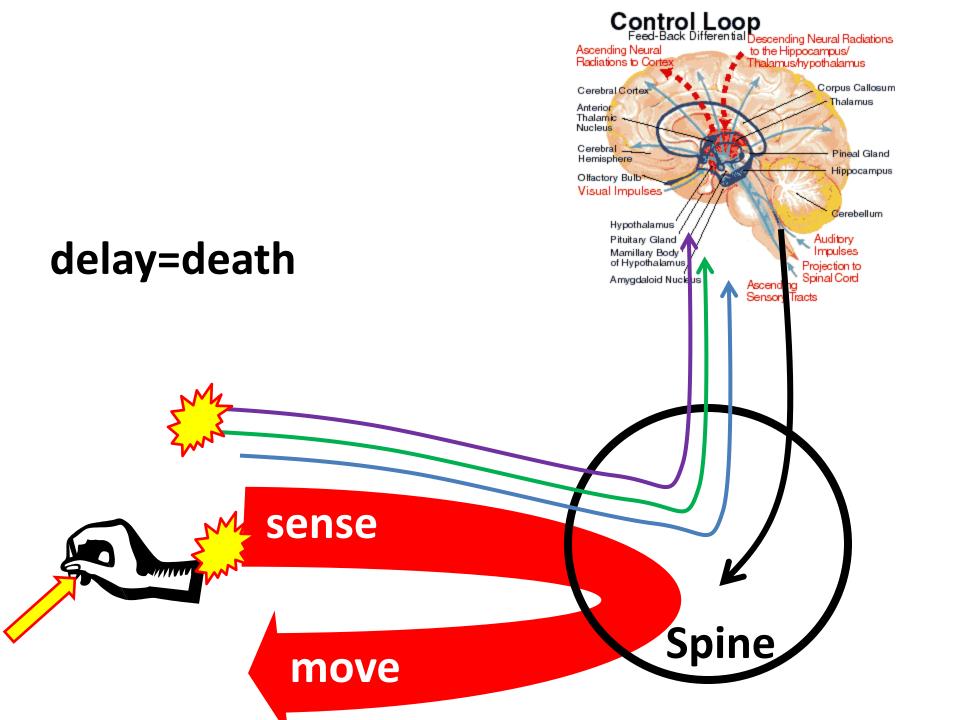
Versus standing on one leg

- Eyes open vs closed
- Contrast
 - young surfers
 - old football players



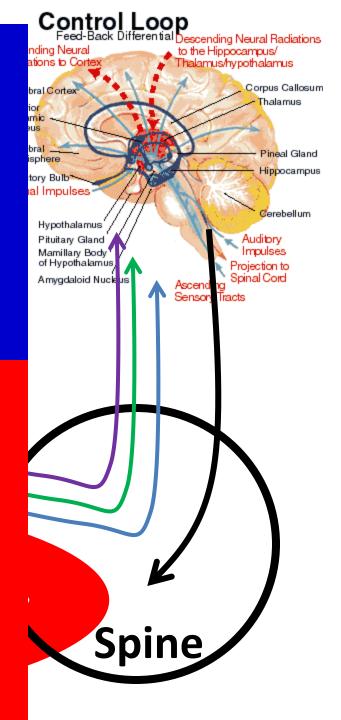
Slow Sense Move hand

Same actuators



Reflect

Reflex





Reflect

Control Loop
Feed-Back Differential Descending Neural Radiations
Inding Neural to the Hippocampus/
mushypothalamus

Corpus Callosum

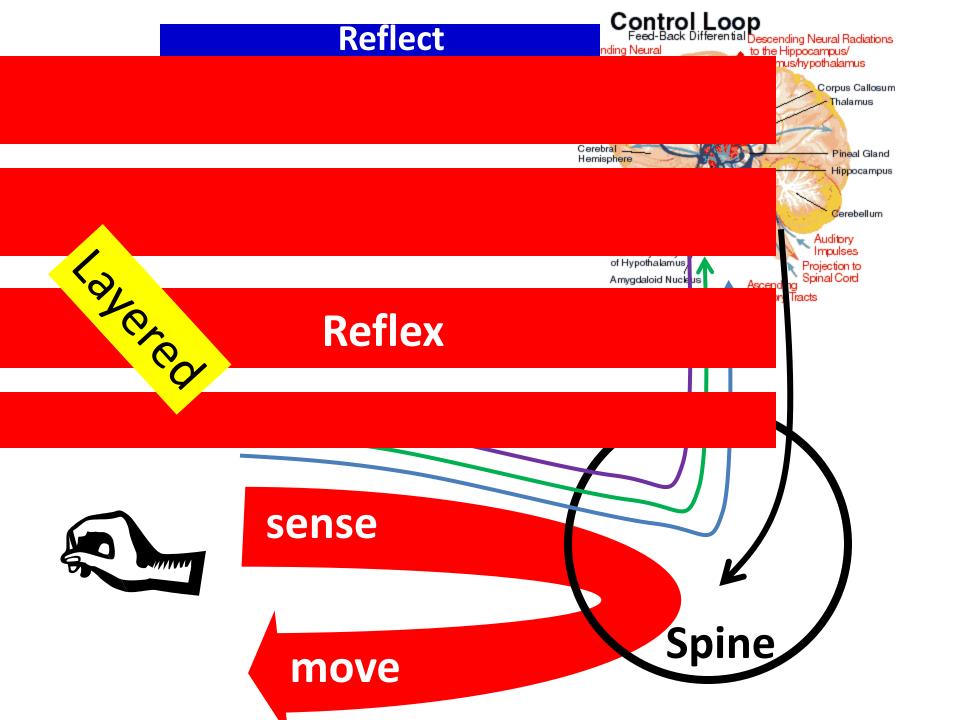
Pineal Gland Hippocampus

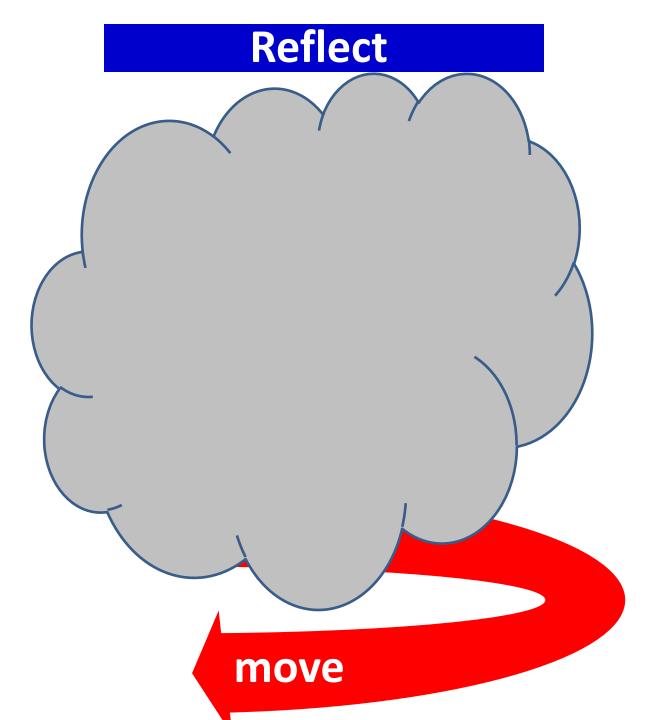
Cerebellum

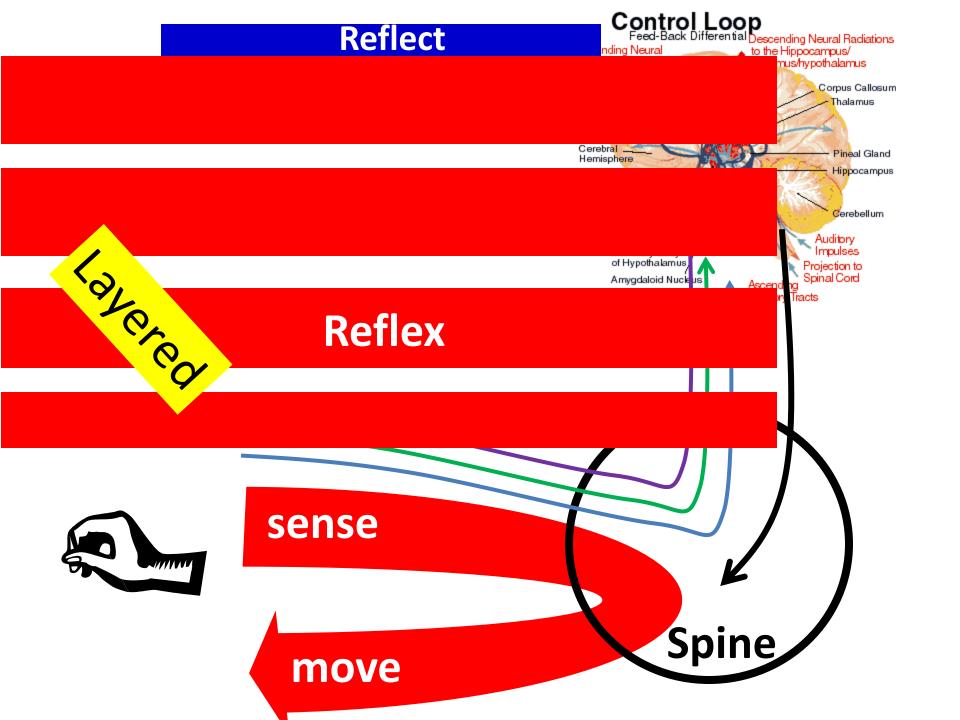
Auditory Impulses

Projection to Spinal Cord

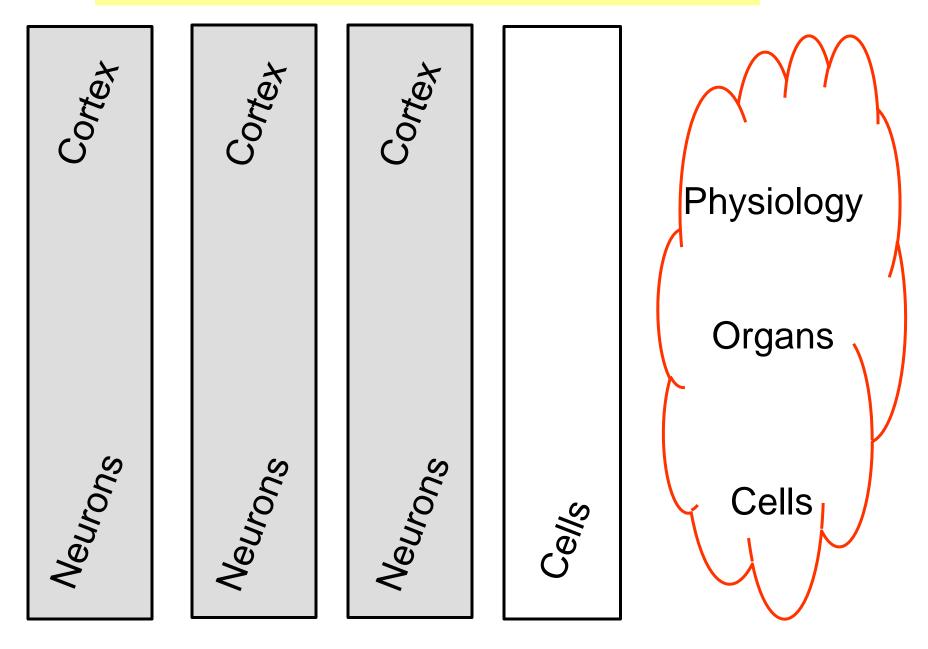
Reflex

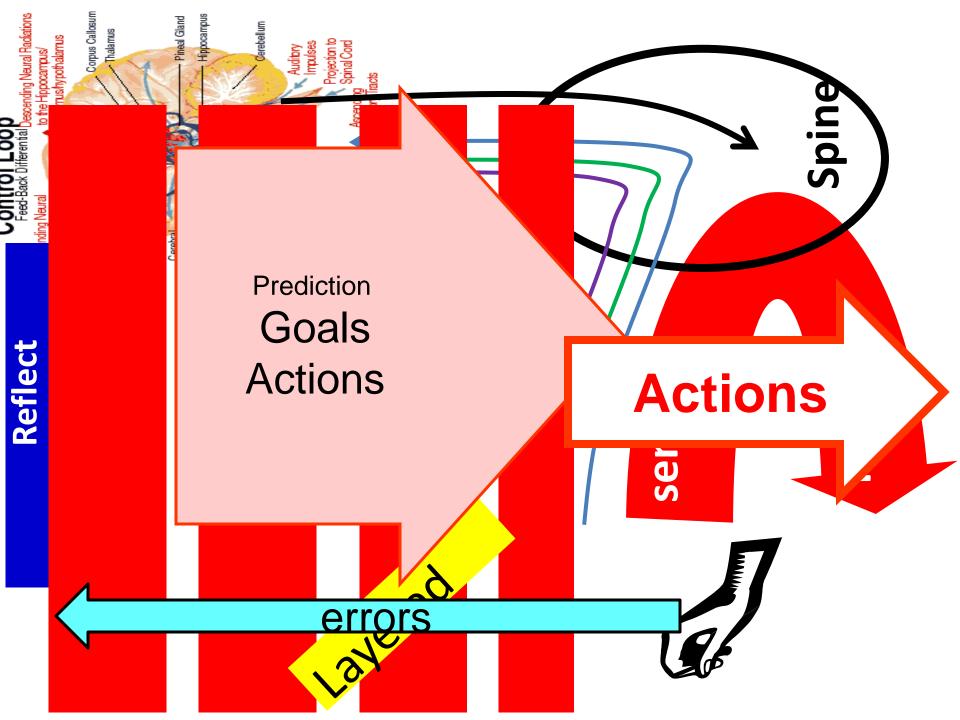




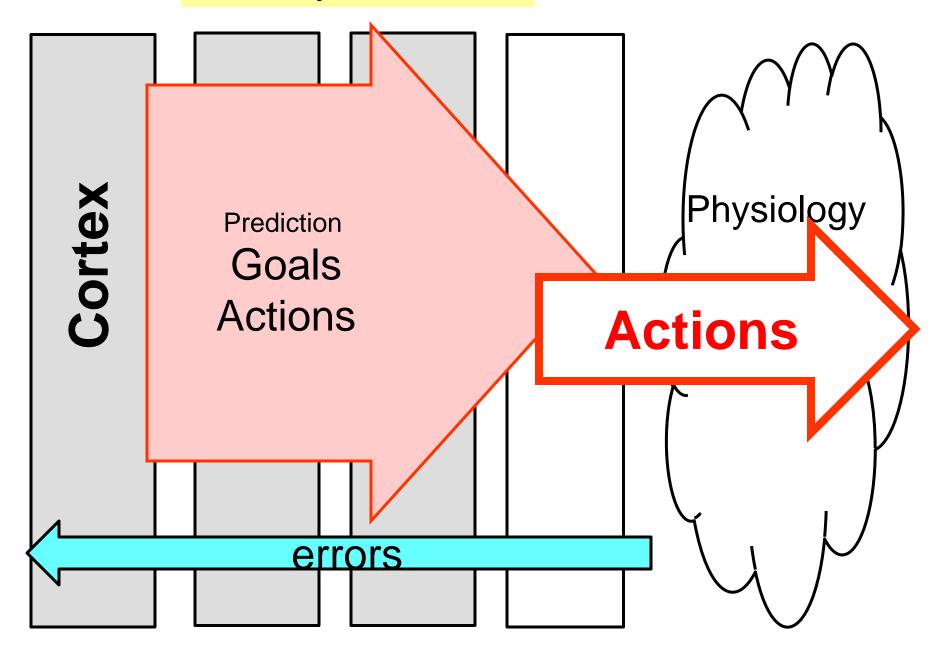


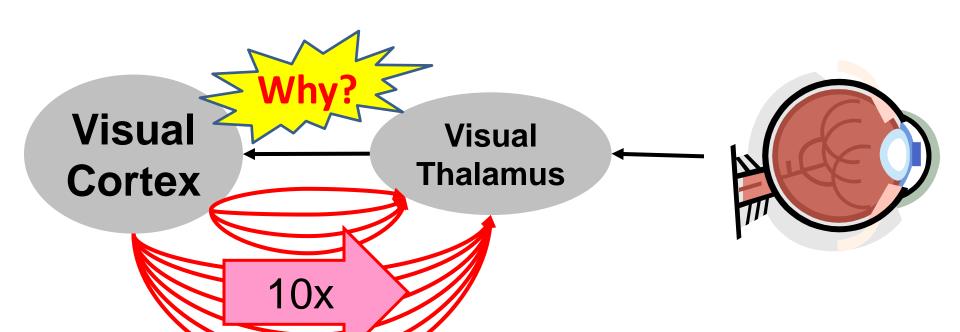
Layered architectures (cartoon)

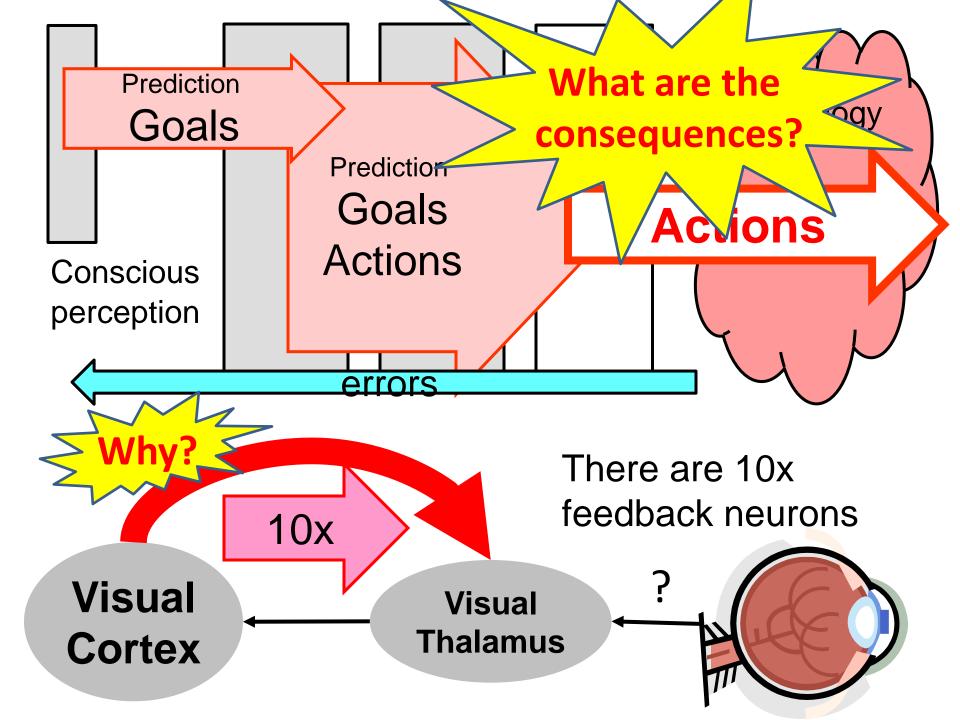




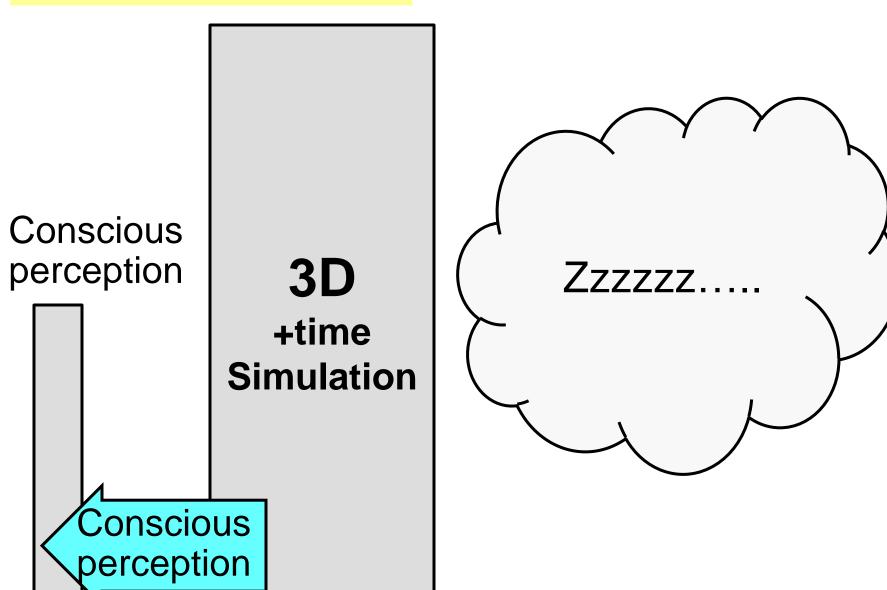
Meta-layers cartoon

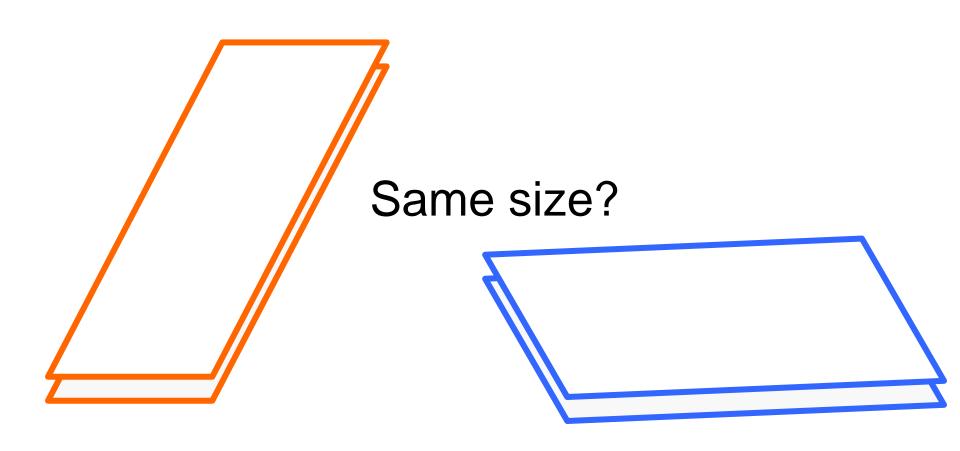


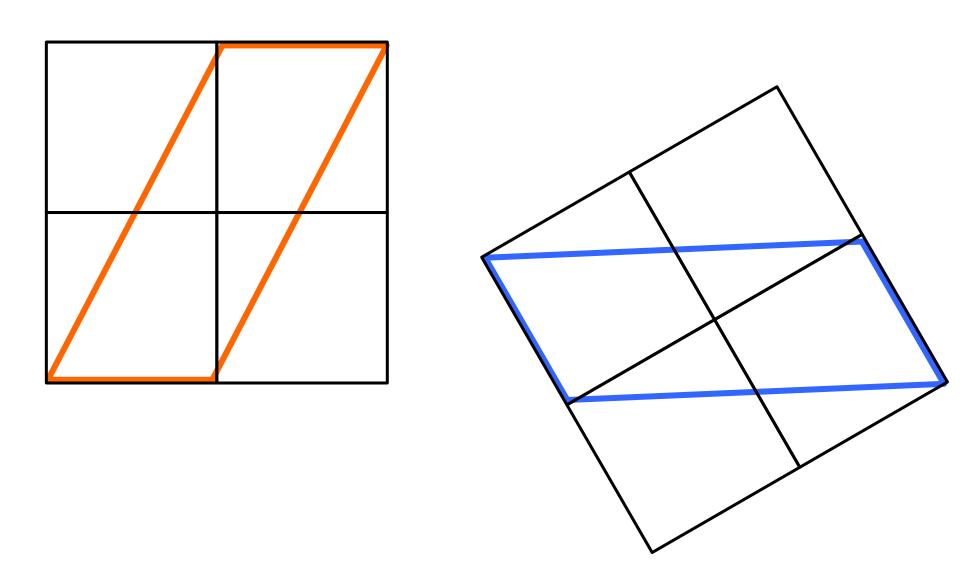


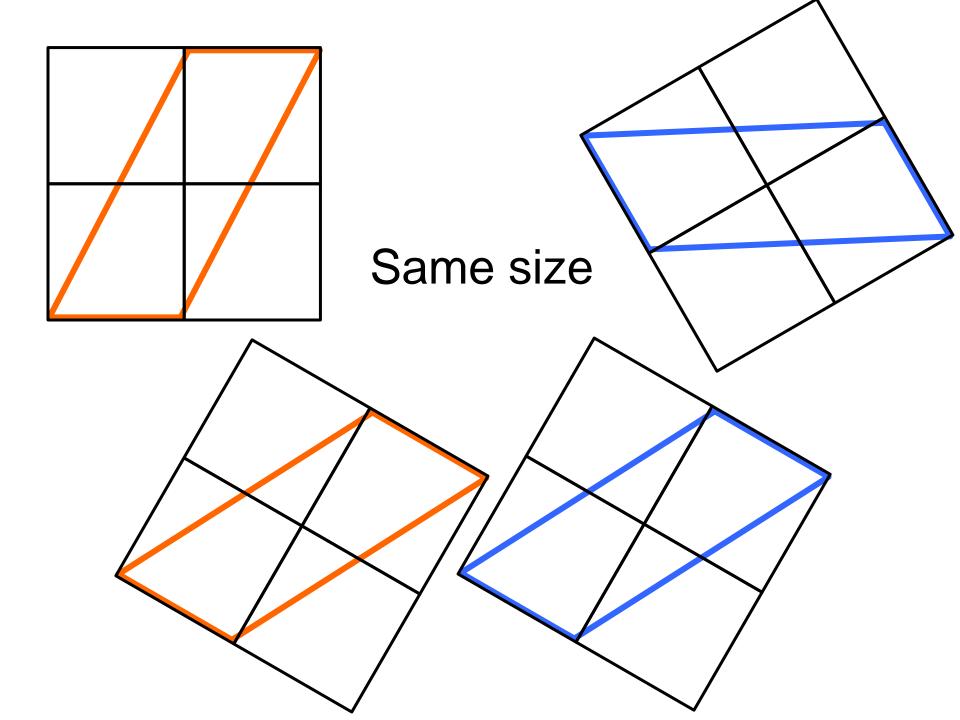


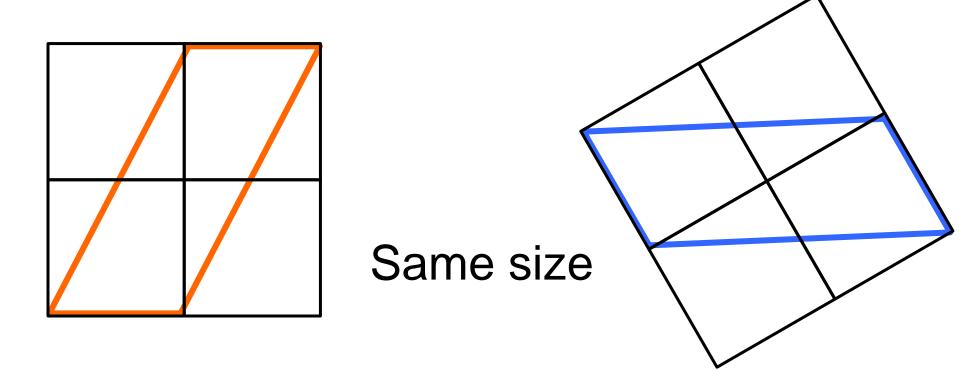
Seeing is *dreaming*

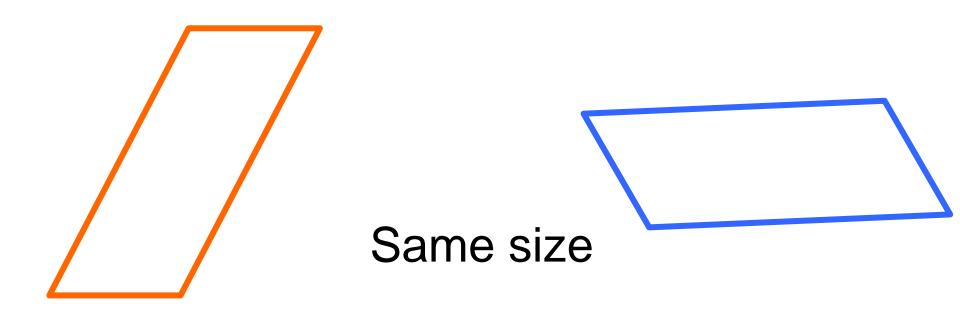






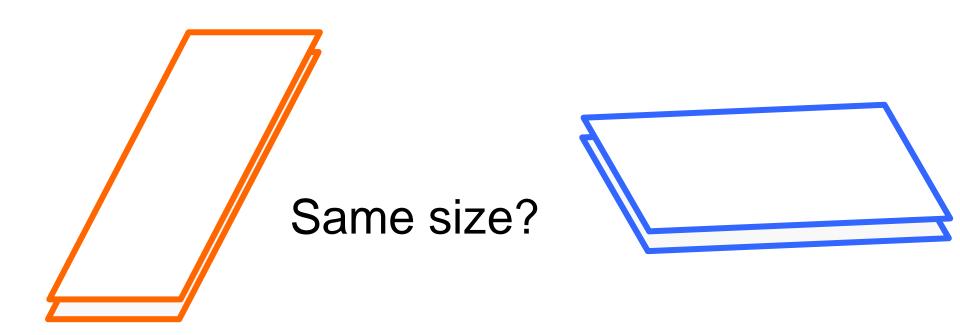






Toggle between this slide and the ones before and after

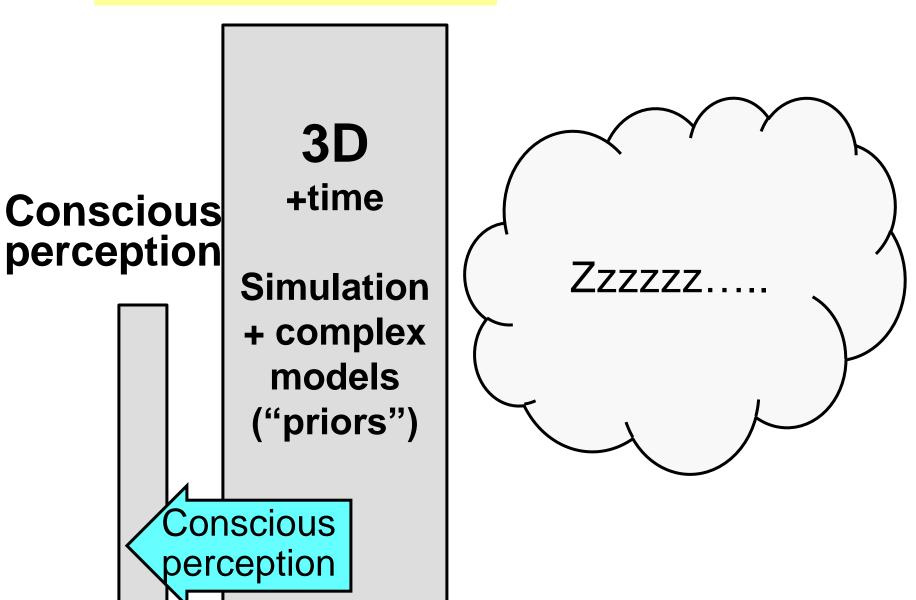
Even when you "know" they are the same, they appear different

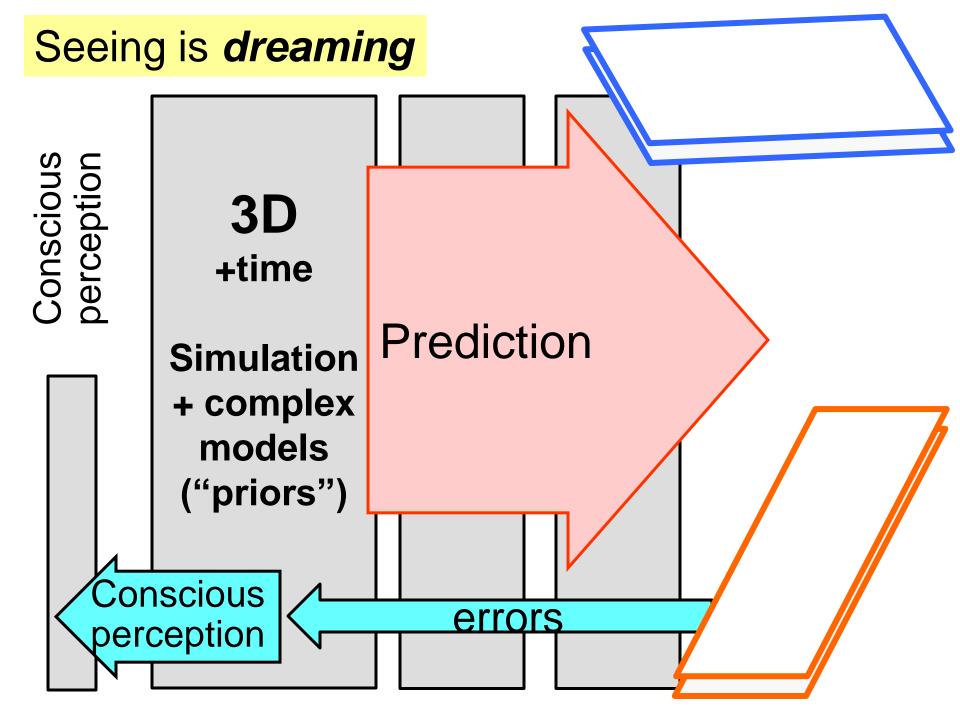


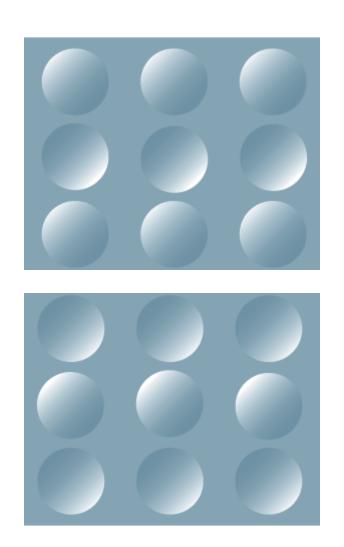
Vision: evolved for complex simulation and control, not 2d static pictures

Even when you "know" they are the same, they appear different

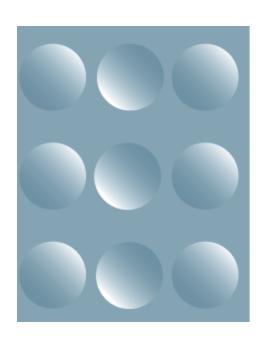
Seeing is *dreaming*

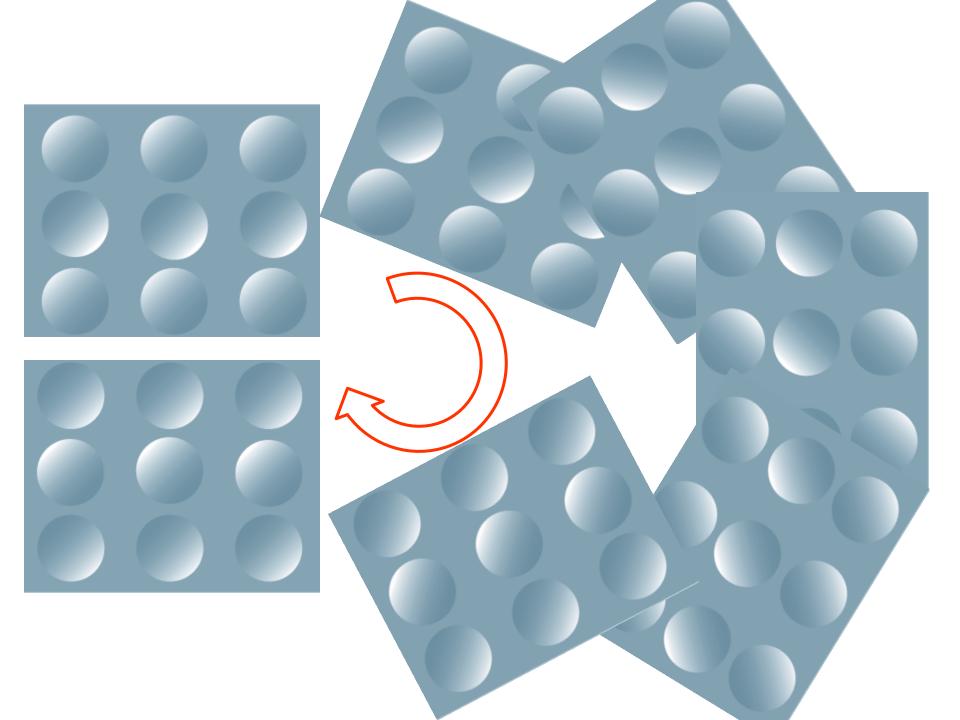


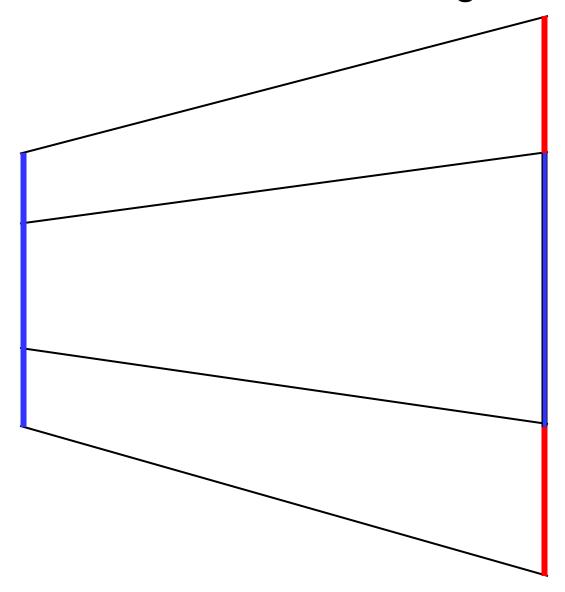


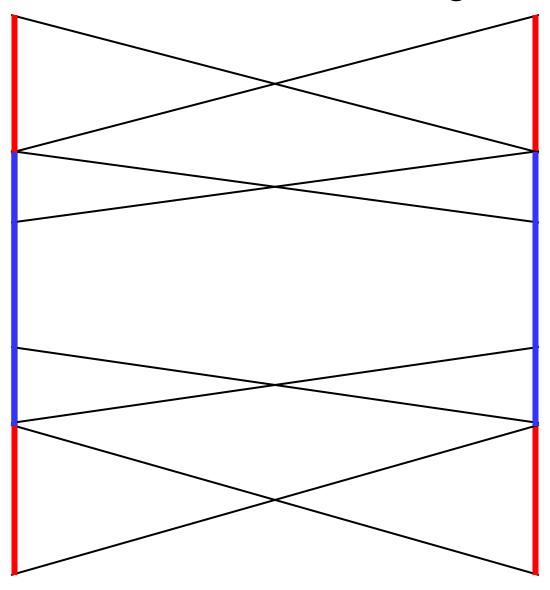


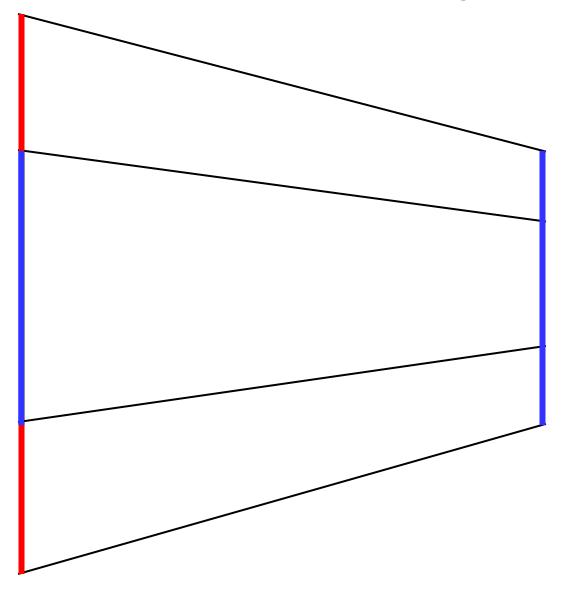
Inferring shape from shading

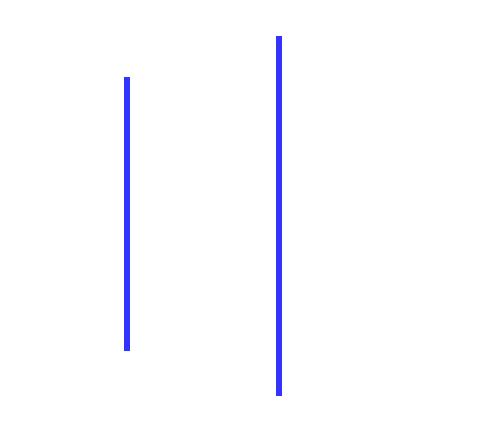


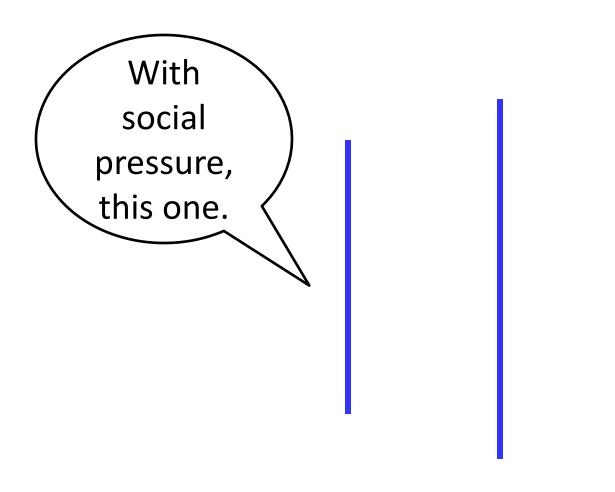












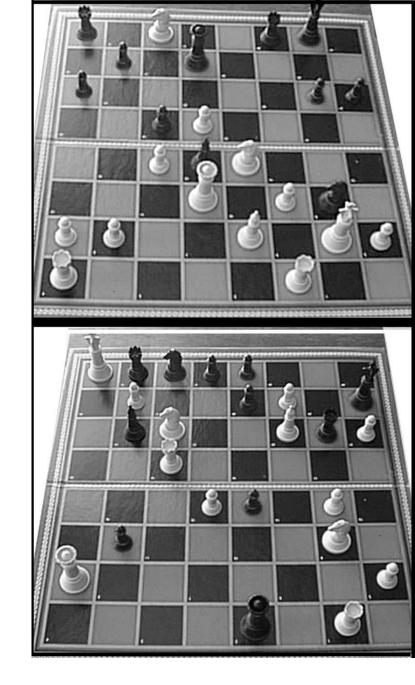
Standard social psychology experiment.



Chess experts

- can reconstruct entire chessboard with < ~ 5s inspection
- can recognize 1e5 distinct patterns
- can play multiple games
 blindfolded and simultaneous
- are no better on random boards

(Simon and Gilmartin, de Groot)



Specialized Face Learning Is Associated with Individual Recognition in Paper Wasps



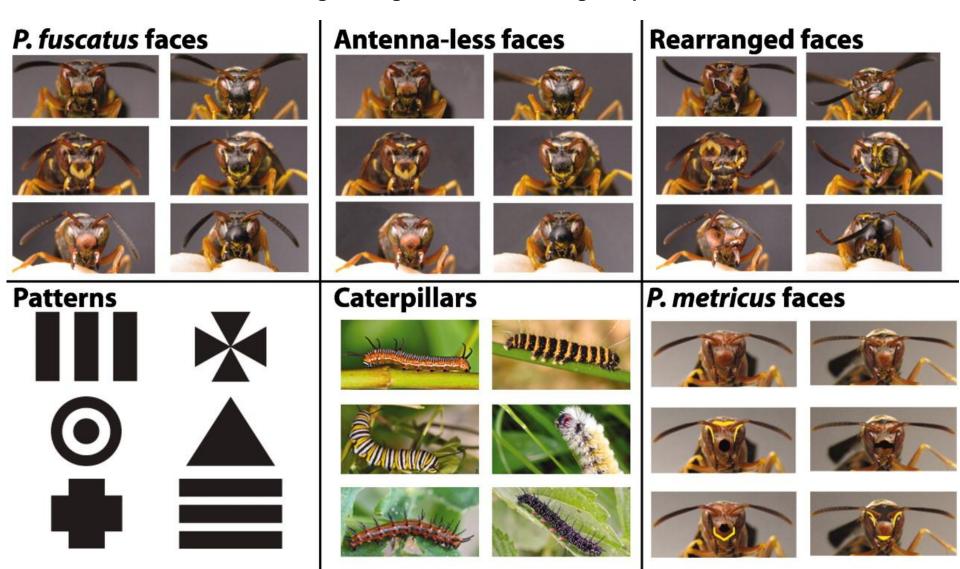
Michael J. Sheehan* and Elizabeth A. Tibbetts

We demonstrate that the evolution of facial recognition in wasps is associated with specialized face-learning abilities. *Polistes fuscatus* can differentiate among normal wasp face images more rapidly and accurately than nonface images or manipulated faces. A close relative lacking facial recognition, *Polistes metricus*, however, lacks specialized face learning. Similar specializations for face learning are found in primates and other mammals, although *P. fuscatus* represents an independent evolution of specialization. Convergence toward face specialization in distant taxa as well as divergence among closely related taxa with different recognition behavior suggests that specialized cognition is surprisingly labile and may be adaptively shaped by species-specific selective pressures such as face recognition.

When needed, even wasps can do it.

- *Polistes fuscatus* can differentiate among normal wasp face images more rapidly and accurately than nonface images or manipulated faces.
- *Polistes metricus* is a close relative lacking facial recognition and specialized face learning.
- Similar specializations for face learning are found in primates and other mammals, although *P. fuscatus* represents an independent evolution of specialization.
- Convergence toward face specialization in distant taxa as well as divergence among closely related taxa with different recognition behavior suggests that specialized cognition is surprisingly labile and may be adaptively shaped by species-specific selective pressures such as face recognition.

Fig. 1 Images used for training wasps.





weak fragile slow



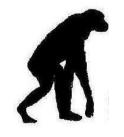
Human evolution

hands feet skeleton muscle skin

All very different.

gut

long helpless childhood

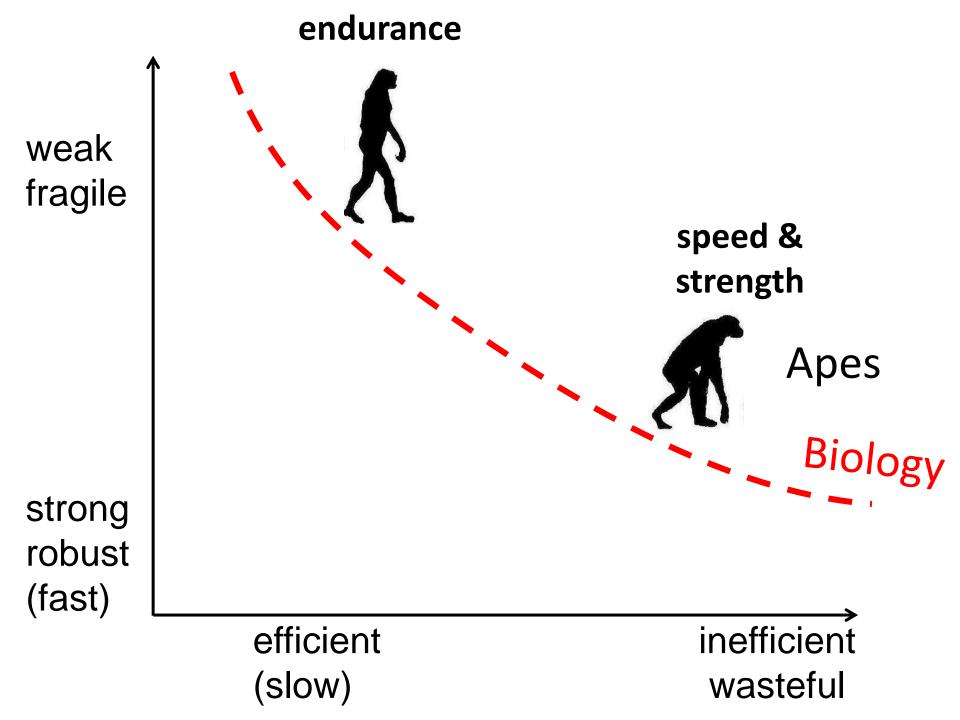


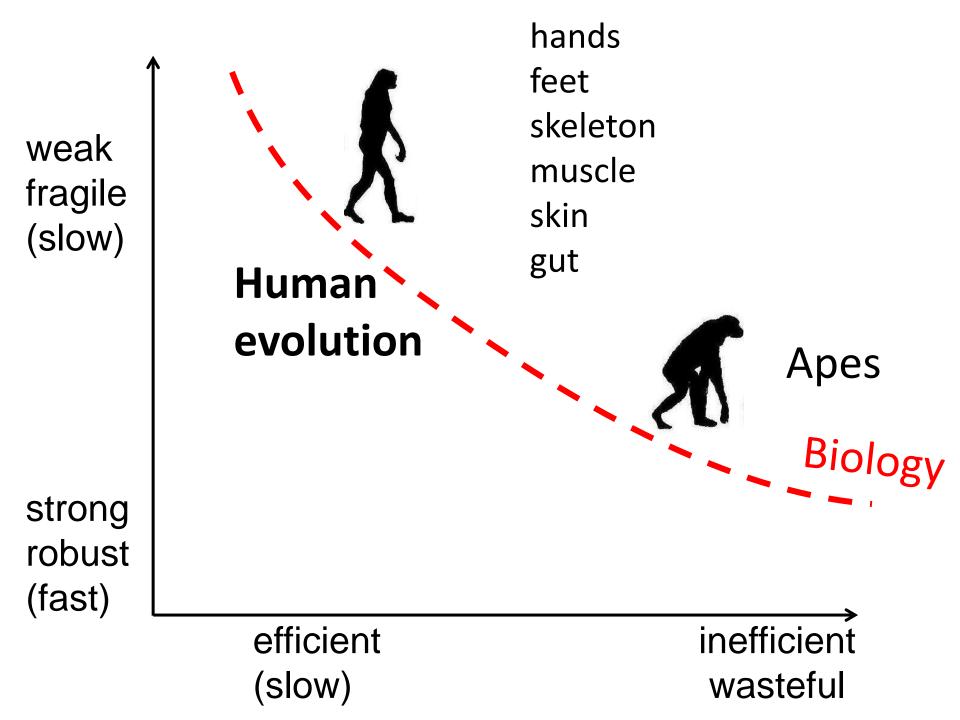
Apes

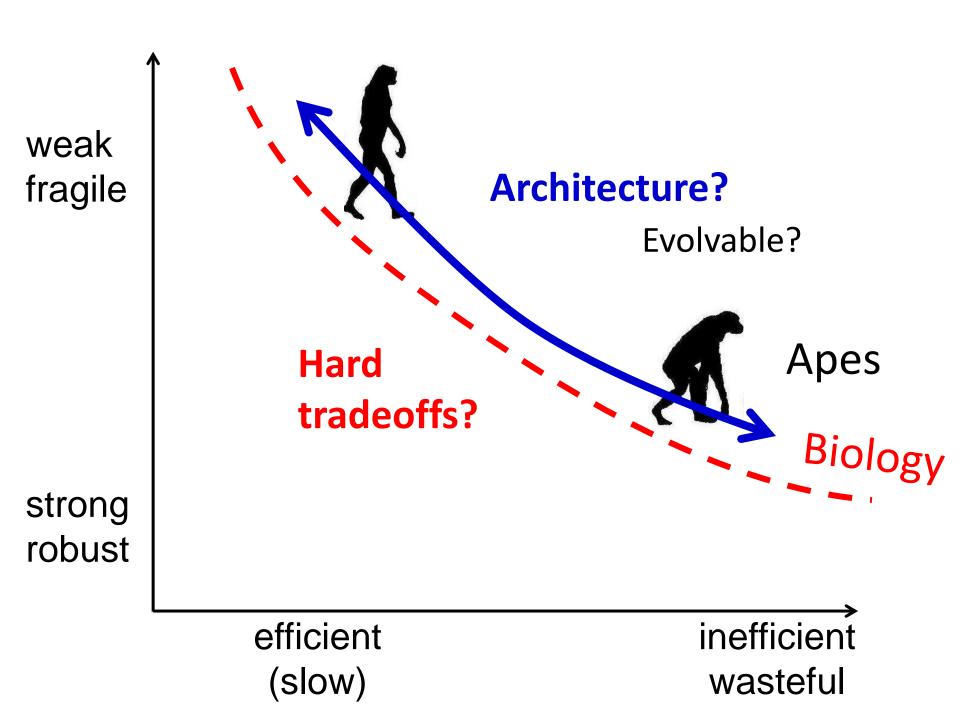
strong robust fast

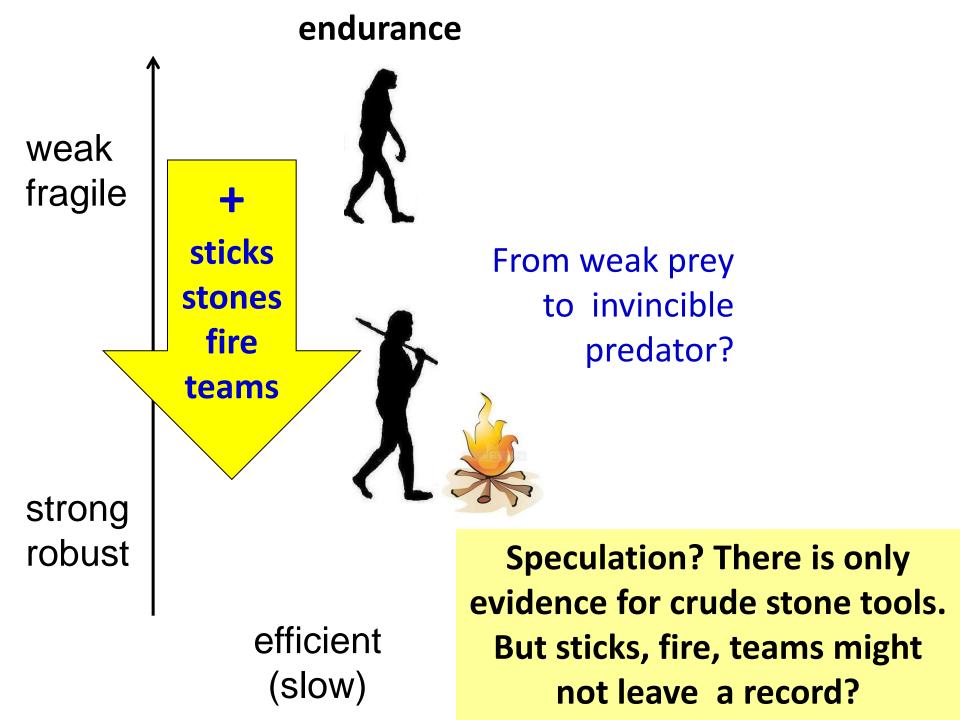
How is this progress?

Homo Erectus? hands Roughly feet modern skeleton weak muscle fragile Very skin fragile gut This much seems pretty consistent among experts regarding circa 1.5-2Mya strong So how did H. Erectus robust survive and expand globally? inefficient efficient wasteful (slow)











Speculation? With only evidence for crude stone tools. But sticks and fire might not leave a record?

sticks stones fire teams



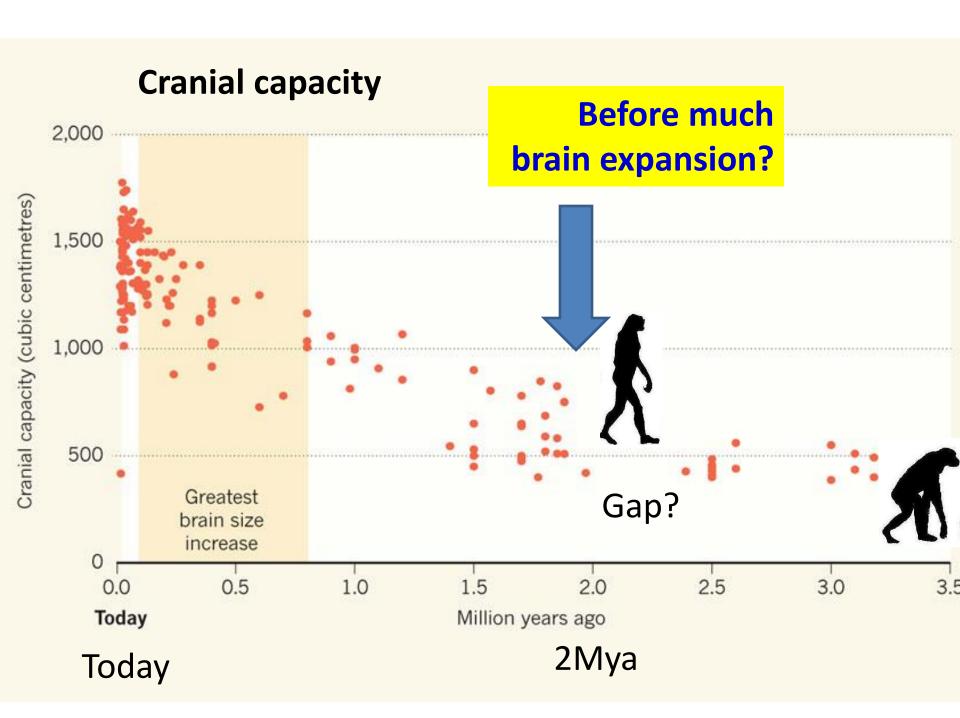
From weak prey to invincible predator

strong robust

Before much brain expansion?

efficient (slow)

Plausible but speculation?



K

hands feet skeleton muscle skin gut Key point:
Our physiology,
technology,
and brains
have coevolved

sticks strong stones robust fire

t cks nes

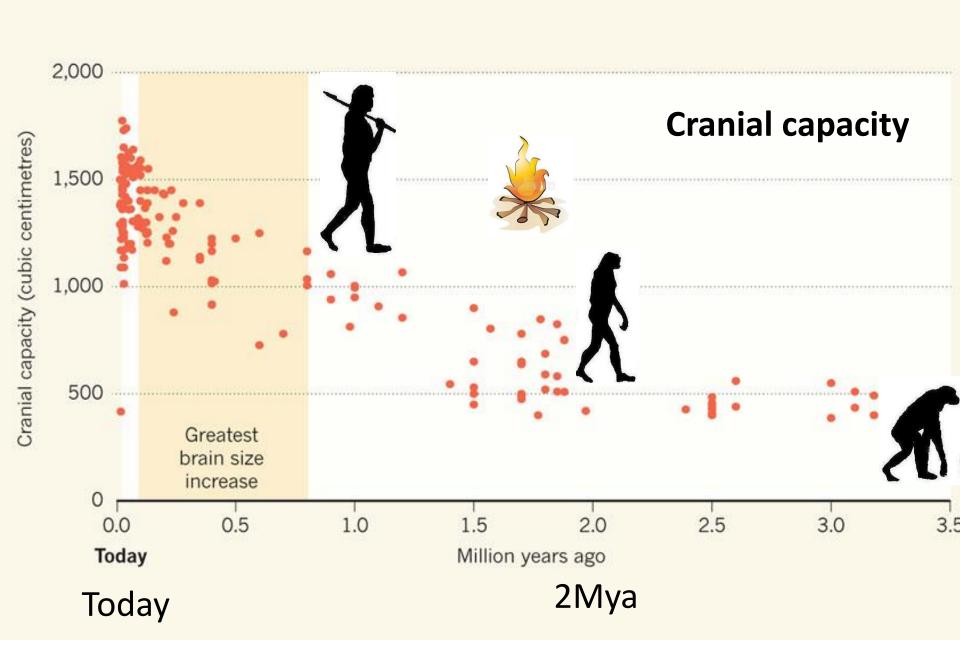
From weak prey to invincible predator

Probably true no matter what

Before much brain expansion?

efficient (slow)

Huge implications.





hands feet skeleton muscle skin gut Key point needing more discussion:
The evolutionary challenge of big brains is homeostasis, not basal metabolic load.

+
sticks
stones
fire

From weak prey to invincible predator

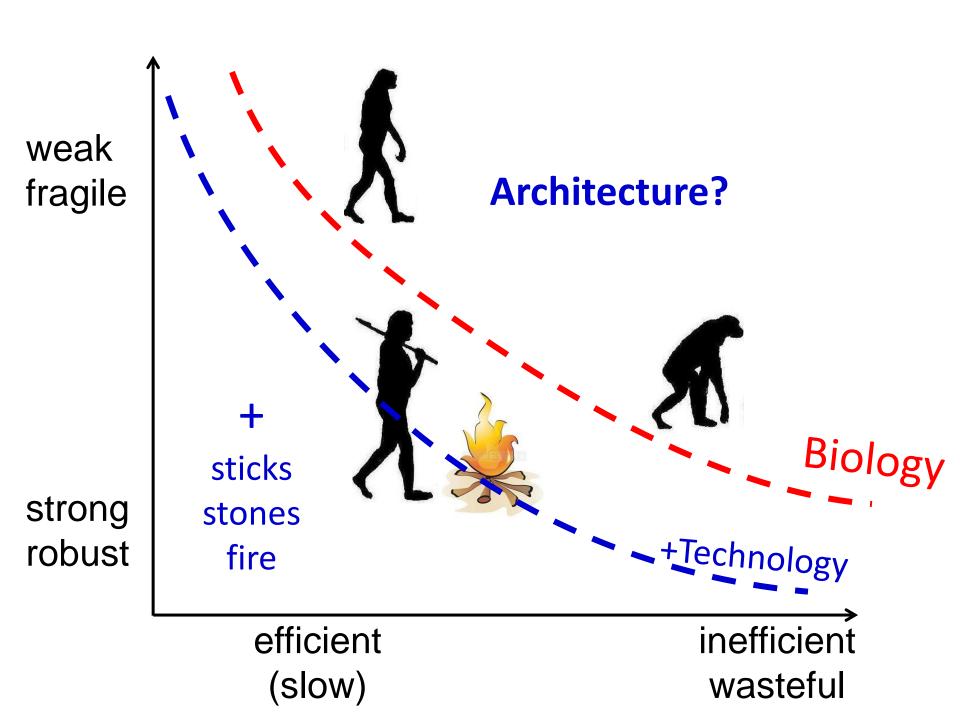
Before much brain expansion?

efficient (slow)

Huge implications.

Fundamental

strong robust



K

hands feet skeleton muscle skin gut

T



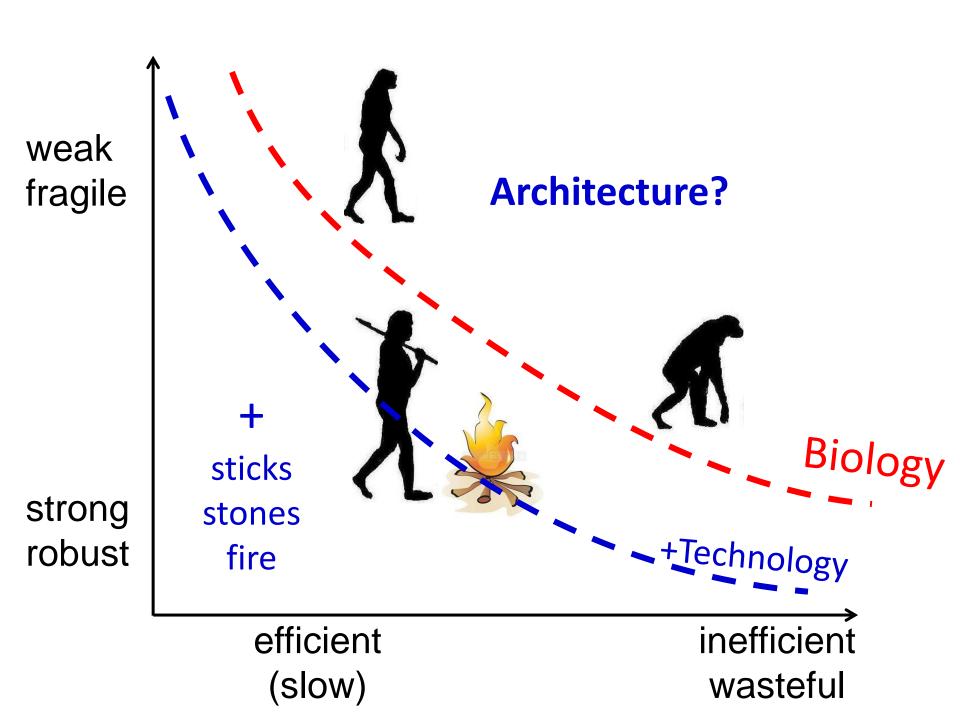
From weak prey to invincible predator

strong robust

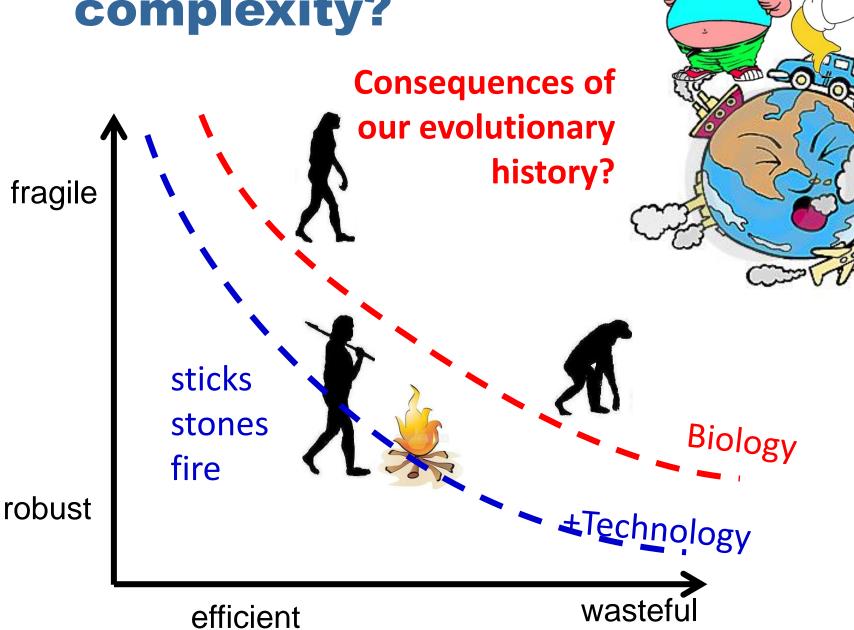
sticks stones fire

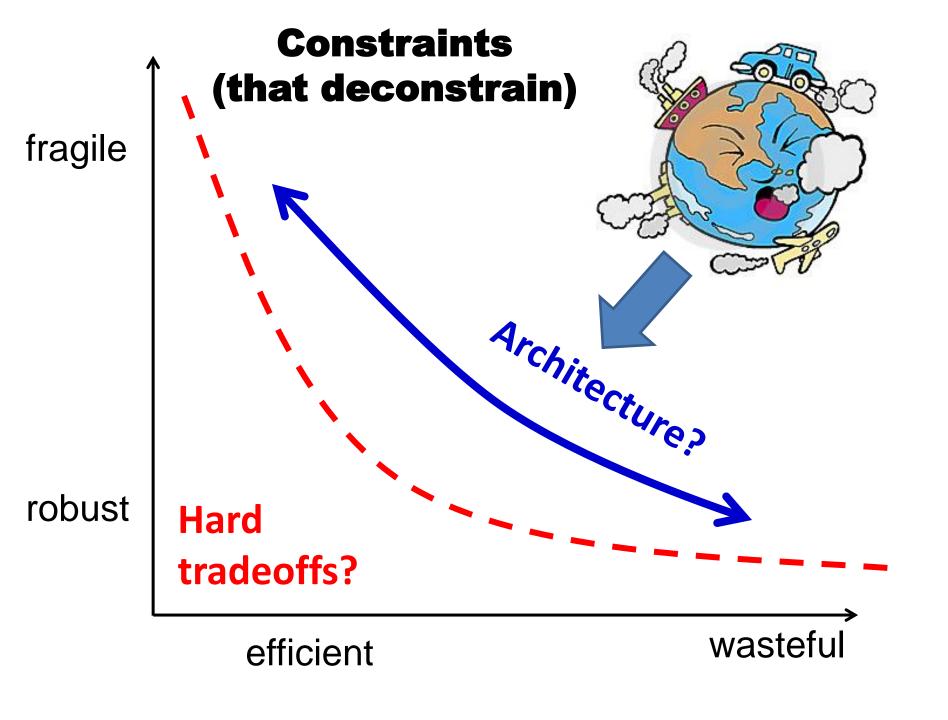
efficient (slow)

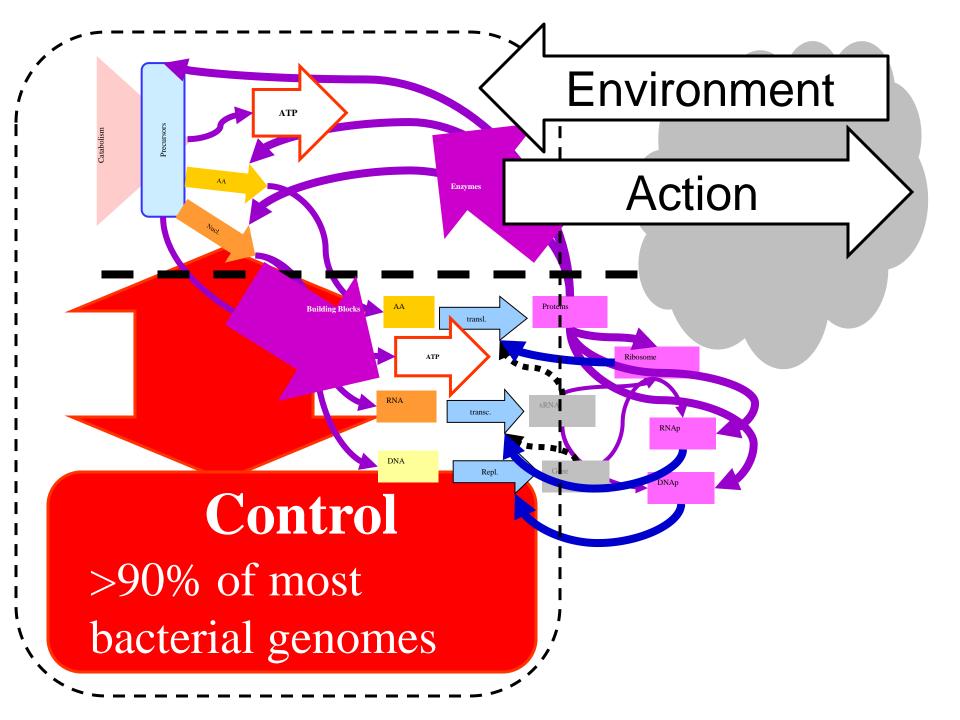
Before much brain expansion?

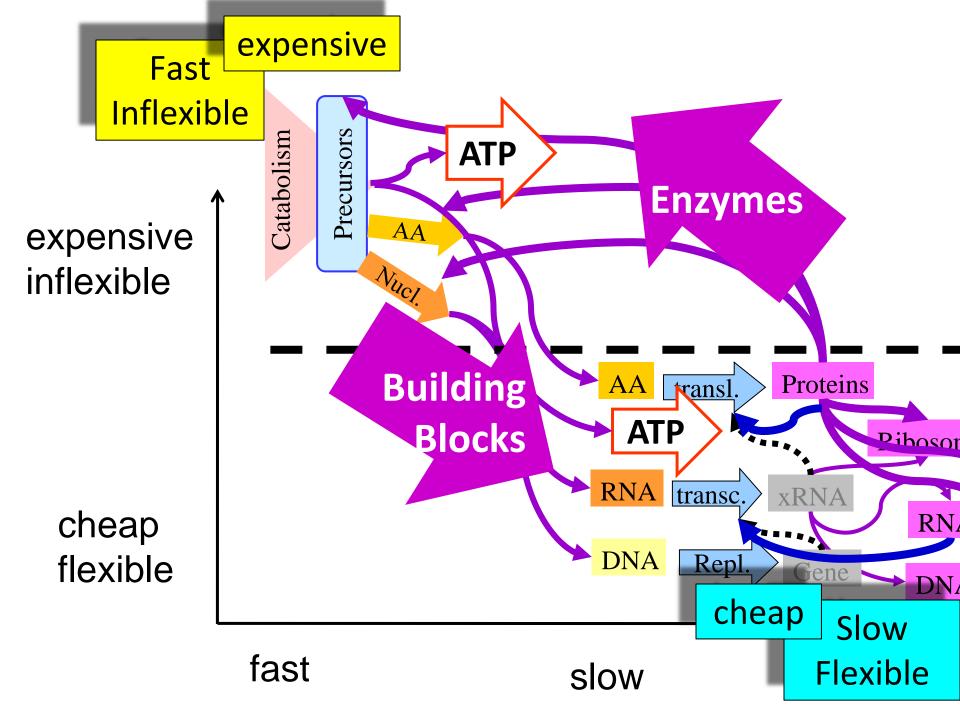


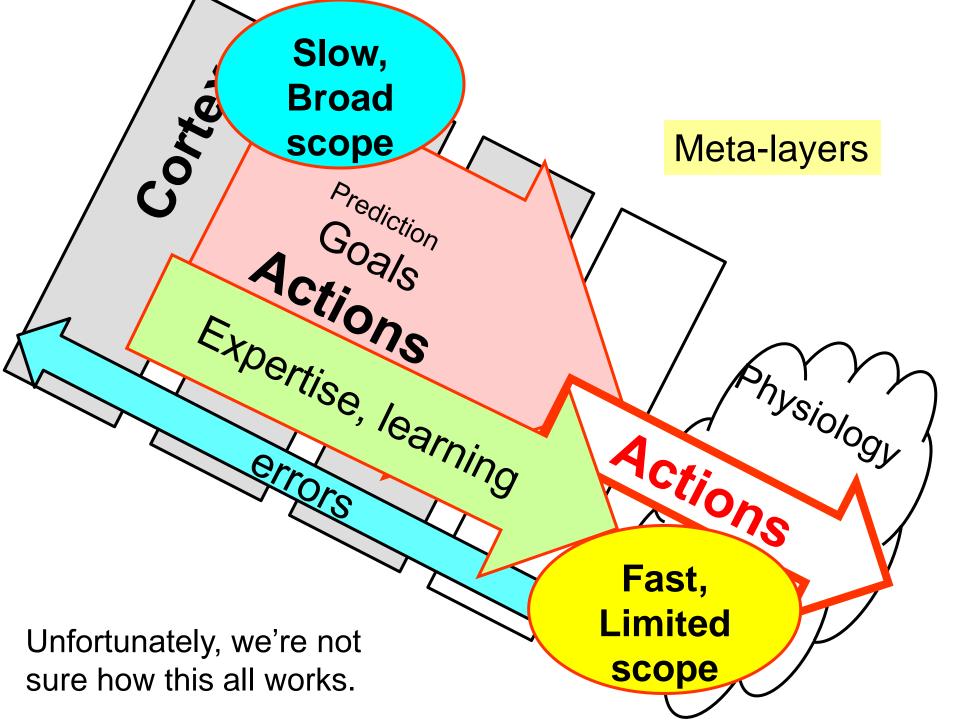
Human complexity?

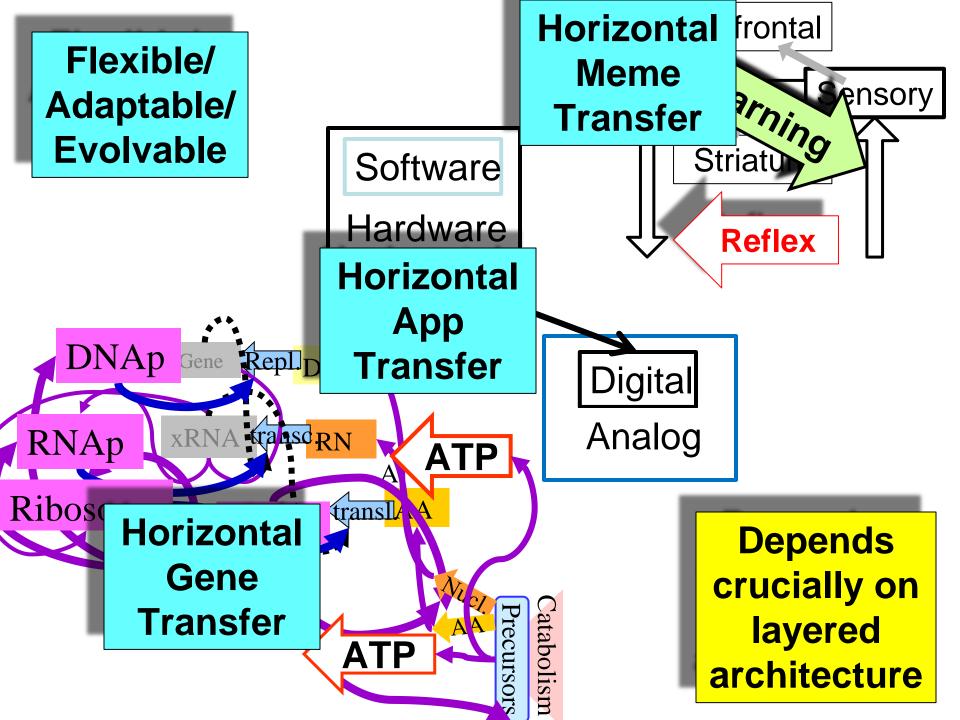












"New sciences" of "complexity" and "networks"?



Science as

- Pure fashion
- Ideology
- Political
- Evangelical
- Nontech trumps tech

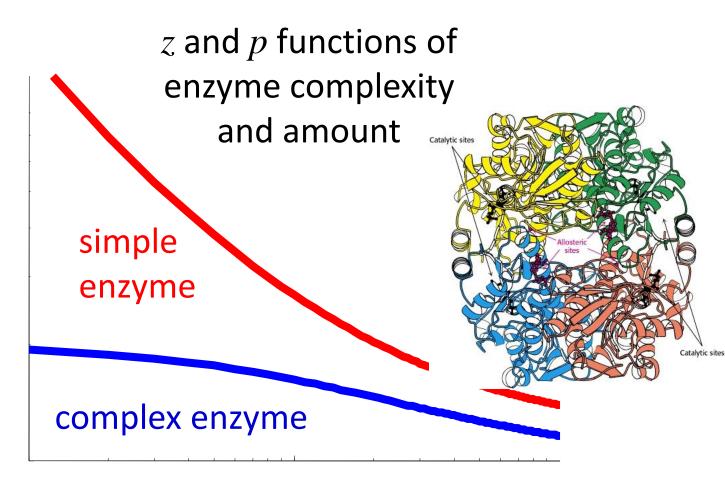
- Edge of chaos
- Self-organized criticality
- Scale-free "networks"
- Creation "science"
- Intelligent design
- Financial engineering
- Risk management
- "Merchants of doubt"
- ...

Theorem!

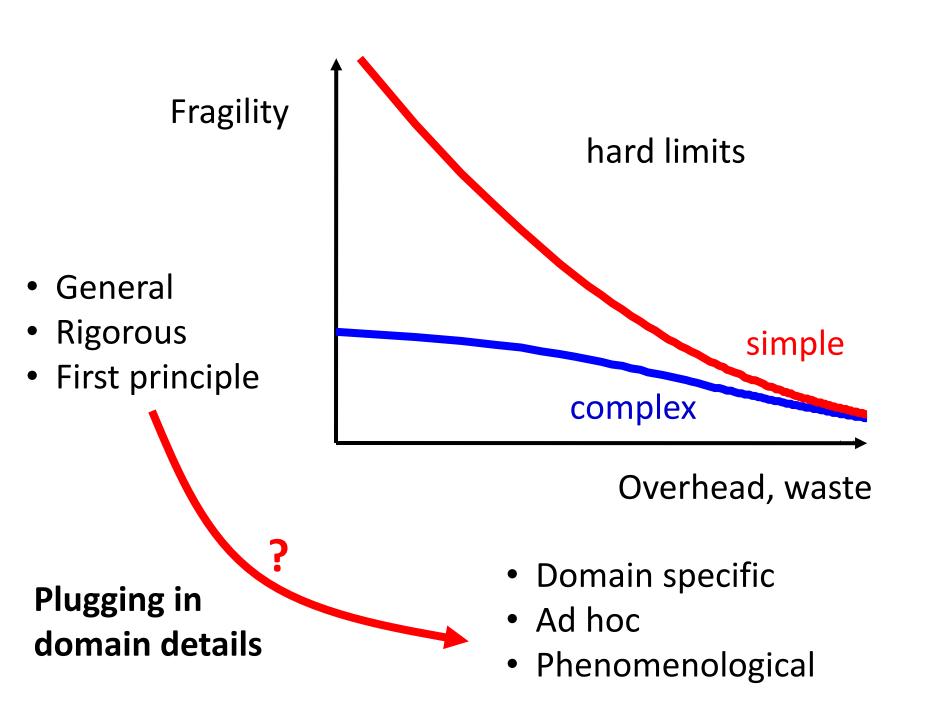
$$\frac{1}{\pi} \int_{0}^{\infty} \ln |S(j\omega)| \left(\frac{z}{z^{2} + \omega^{2}}\right) d\omega \ge \ln \left|\frac{z + p}{z - p}\right|$$



$$\ln \left| \frac{z+p}{z-p} \right|$$



Enzyme amount



ControlWienerCommsBode
Kalmanrobust controlShannon

- General
- Rigorous
- First principle

- Fundamental multiscale physics
- Foundations, origins of
 - noise
 - dissipation
 - amplification
 - catalysis

Carnot

Boltzmann

Heisenberg

What I'm not going to talk much about

- It's true that most "really smart scientists" think almost everything in these talks is nonsense
- Why they think this
- Why they are wrong
- Time (not space) is our problem, as usual
- Don't have enough time for what is true, so have to limit discussion of what isn't
- No one ever changes a made up mind (almost)
- But here's the overall landscape

Control

Comms

Complex networks

Compute

"New sciences" of

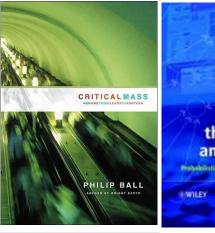
Stat physics

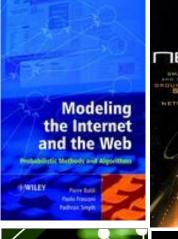
"New sciences" of complexity and networks edge of chaos, self-organized criticality, scale-free,...

Carnot

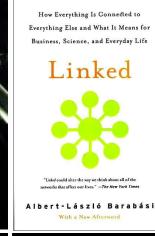
Boltzmann

Heisenberg



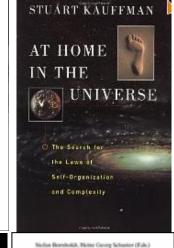


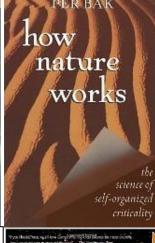


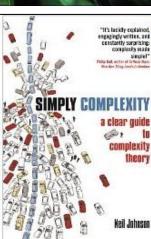


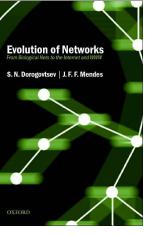
The Structure and Dynamics of

NETWORKS

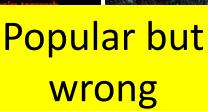


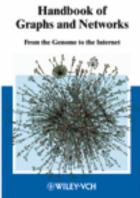


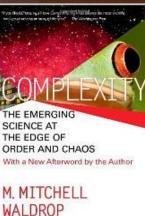


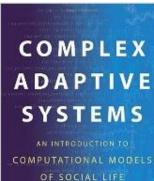


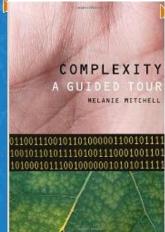


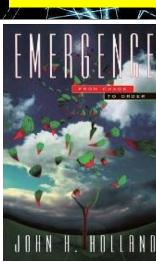




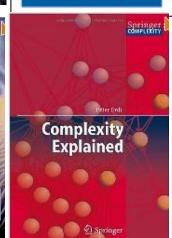


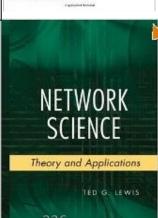












WILEY

Even small amounts can create bewildering complexity

Fragile

- Scale
- Dynamics
- Nonlinearity
- Nonequlibrium
- Open
- Feedback
- Adaptation
- Intractability
- Emergence

•

Robust

- Scale
- Dynamics
- Nonlinearity
- Nonequlibrium
- Open
- Feedback
- Adaptation
- Intractability
- Emergence

• . . .

Fragile

- Scale
- Dynamics
- Nonlinearity
- Nonequlibrium
- Open
- Feedback
- Adaptation
- Intractability
- Emergence

•

Robust complexity

- Scale
- Dynamics
- Nonlinearity
- Nonequlibrium
- Open
- Feedback
- Adaptation
- Intractability
- Emergence
- ...

- Resources
- Controlled
- Organized
- Structured
- Extreme
- Architected

•

- These words have lost much of their original meaning, and have become essentially meaningless synonyms
- e.g. nonlinear ≠ not linear
- Can we recover these words?
- Idea: make up a new word to mean "I'm confused but don't want to say that"
- Then hopefully we can take these words back (e.g. nonlinear = not linear)

Fragile complexity

- Scale
- Dynamics
- Nonlinearity
- Nonequlibrium
- Open
- Feedback
- Adaptation
- Intractability
- Emergence
- •

New words

Emergulent

Emergulence at the edge of chaocritiplexity

Fragile complexity

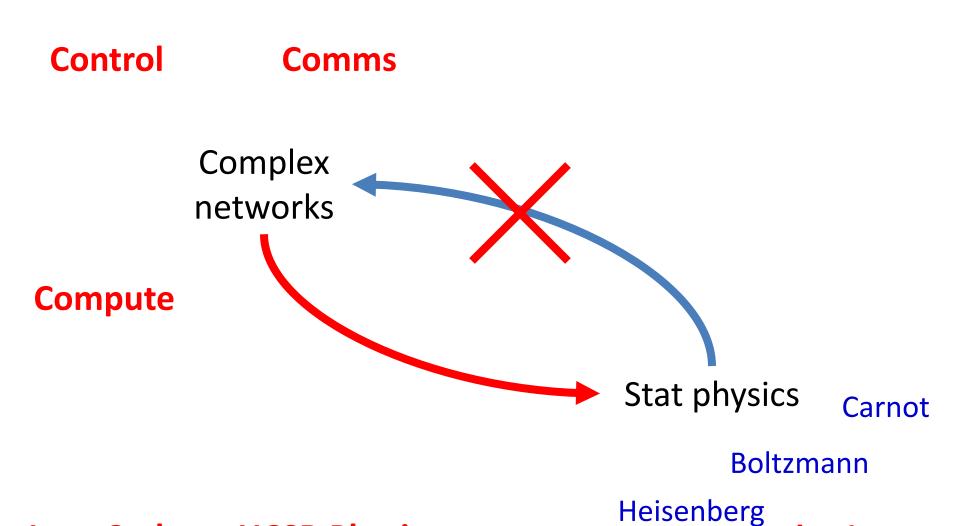
- Scale
- Dynamics
- Nonlinearity
- Nonequlibrium
- Open
- Feedback
- Adaptation
- Intractability
- Emergence
- ...

Complex networks doesn't work

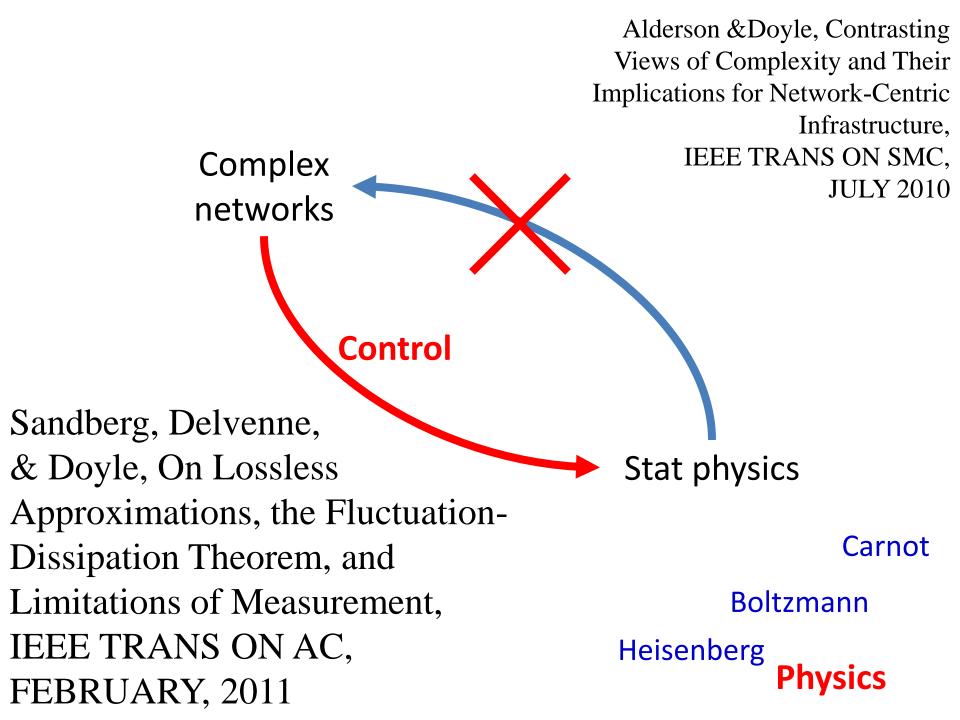
Alderson & Doyle, Contrasting Views of Complexity and Their Implications for **Network-Centric** Infrastructure, IEEE TRANS ON SMC, **JULY 2010**

Stat physics

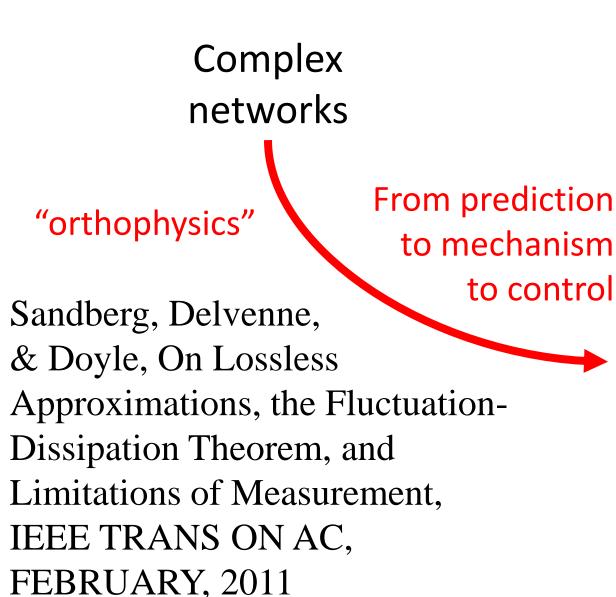
"New sciences" of complexity and networks edge of chaos, self-organized criticality, scale-free,...



Jean Carlson, UCSB Physics



"The last 70 years of the 20th century will be viewed as the dark ages of theoretical physics." (Carver Mead)





Stat physics, fluids, QM

Boltzmann

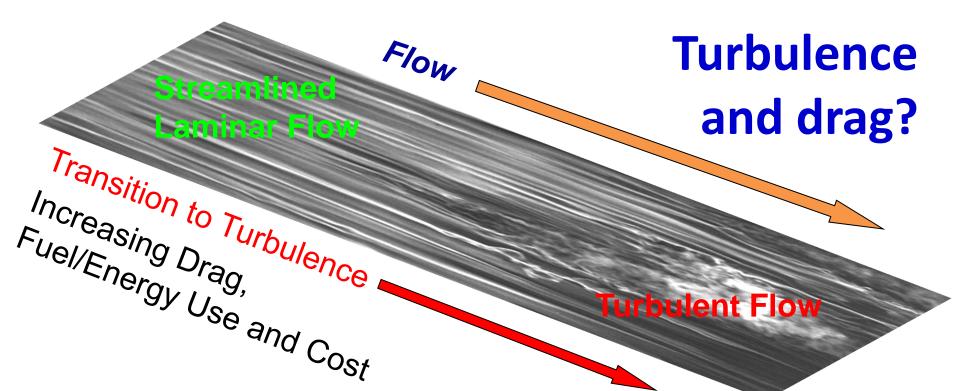
Heisenberg

doi:10.1017/S0022112010003861

J. Fluid Mech (2010)

A streamwise constant model of turbulence in plane Couette flow

D. F. GAYME¹†, B. J. McKEON¹, A. PAPACHRISTODOULOU², B. BAMIEH³ AND J. C. DOYLE¹



Physics of Fluids (2011)

PHYSICS OF FLUIDS 23, 065108 (2011)

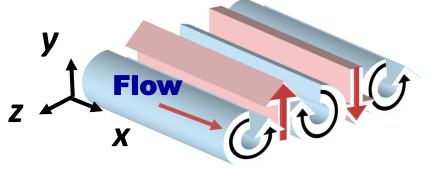
Amplification and nonlinear mechanisms in plane Couette flow

Dennice F. Gayme, Beverley J. McKeon, Bassam Bamieh, Antonis Papachristodoulo and John C. Doyle

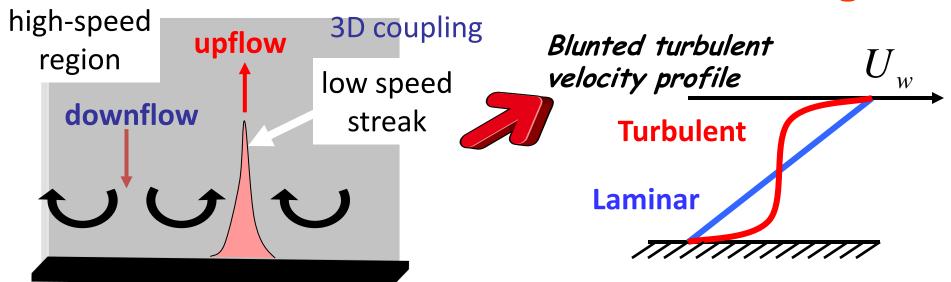
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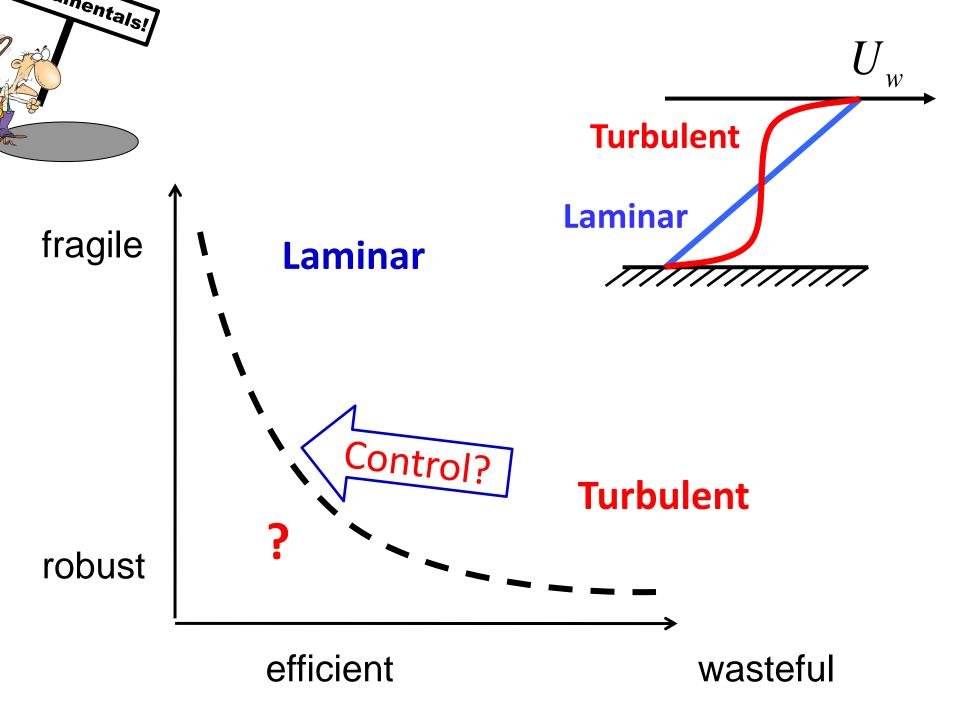
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Coherent structures and turbulent drag





Existing design frameworks

- Sophisticated components
- Poor integration
- Limited theoretical framework

